Integral criteria for transportation cost inequalities

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Abstract

Abstract. In this paper, we provide a characterization of a large class of transportation-cost inequalities in terms of exponential integrability of the cost function under the reference probability measure. Our results completely extend the previous works by Djellout, Guillin and Wu cite{DGW03} and Bolley and Villani cite{BV03}.

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Published on: June 12, 2006

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