On Fractional Fields indexed by Metric Spaces

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Abstract

We define and build H-fractional α-stable fields indexed by a metric space (E,d). We mainly apply these results to spheres, hyperbolic spaces and real trees

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