

## Tree and Grid factors of General Point processes

Adam Timar, *Indiana University*

### Abstract

We study isomorphism invariant point processes of  $\mathbb{R}^d$ ; whose groups of symmetries are almost surely trivial. We define a 1-ended, locally finite tree factor on the points of the process, that is, a mapping of the point configuration to a graph on it that is measurable and equivariant with the point process. This answers a question of Holroyd and Peres. The tree will be used to construct a factor isomorphic to  $\mathbb{Z}^n$ . This perhaps surprising result (that any  $d$  and  $n$  works) solves a problem by Steve Evans. The construction, based on a connected clumping with  $2^i$  vertices in each clump of the  $i$ 'th partition, can be used to define various other factors.

Full text: [PDF](#) | [PostScript](#)

Pages: 53-59

Published on: April 21, 2004

### Bibliography

1. K. S. Alexander. Percolation and minimal spanning forests in infinite graphs. *Ann. Probab.* 23 (1995), 87-104. [Math. Review 96c:60114](#)
2. I. Benjamini, O. Schramm. Percolation in the hyperbolic plane. *J. Amer. Math. Soc.* 14 (2001), 487-507. [Math. Review 2002h:82049](#)
3. P. A. Ferrari, C. Landim, H. Thorisson. Poisson trees, succession lines and coalescing random walks. Preprint. Math. Review number not available.
4. A. E. Holroyd, Y. Peres. Trees and matchings from point processes. *Elect. Comm. in Probab.* , 8 (2003), 17-27. Math. Review number not available.

### Research Support Tool

[Capture Cite](#)  
[View Metadata](#)  
[Printer Friendly](#)

▼ [Context](#)

[Author Address](#)

▼ [Action](#)

[Email Author](#)  
[Email Others](#)