One more approach to the convergence of the empirical process to the Brownian bridge

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Abstract

A theorem of Donsker asserts that the empirical process converges in distribution to the Brownian bridge. The aim of this paper is to provide a new and simple proof of this fact.

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