A universal forgery of Hess's second ID-based signature against the known-message attack

Jung Hee Cheon

Information and Communications University (ICU), Taejon, Republic of Korea jhcheon@icu.ac.kr, http://vega.icu.ac.kr/jhcheon

March, 3rd. 2002

Abstract. In this paper we propose a universal forgery attack of Hess's second ID-based signature scheme against the known-message attack.

Keywords: ID-based signature, Elliptic curve, Bilinear maps

Recently, several ID-based signature schemes based on binary maps on elliptic curves were proposed [CC02,Hes02,Pat02,SOK01]. In [Hes02], he proposed two ID-based signature schemes and provided a formal proof for the first scheme, but only sketch of proof for the second scheme. In this paper, we propose a universal forgery attack of Hess's second ID-based signature scheme against the known-message attack.

First, we introduce Hess's second ID-based signature scheme.

Let (G, +) and (V, \cdot) be groups of prime order ℓ and $e: G \times G \to V$ be a bilinear non-degenerate pairing. We further assume two hash functions $H: \{0, 1\}^* \to G \setminus \{0\}$ and $h: \{0, 1\}^* \times G \to \mathbb{F}^*_l$.

1. **Setup**. The TA picks a random element $P \in G \setminus \{0\}$ and a secret integer $t \in \mathbb{F}_l^*$. The TA then compute

$$Q_{TA} = tP$$

and publishes (P, Q_{TA}) . The value t is stored by the TA.

- 2. **Extract**. Given an identity ID of a user, the algorithm computes his public key $Q_{ID} = H(ID)$ and his private key $S_{ID} = tQ_{ID}$.
- 3. Sign. To sign a message m the signer picks a random integer $k \in \mathbb{F}_l^*$ and then compute
 - (a) r = kP
 - (b) v = h(m, r)
 - (c) $u = (v/k)S_{ID}$
- 4. Verify. On receiving a message m and signature (u,r) the verifier computes:
 - (a) v = h(m, r)
 - (b) Accept the signature if and only if $e(u,r) = e(Q_{ID}, Q_{TA})^v$.

This completes the description of the second ID-based signature scheme. That this verification equation holds for a valid signature follows from the following algebra:

$$e(u,r) = e((v/k)S_{ID}, kP) = e(S_{ID}, P)^v = e(Q_{ID}, Q_{TA})^v.$$

Now, we give a universal forgery attack of the above ID-based signature scheme against the known-message attack.

Assume we have a valid signature (u, r) of a message m. For arbitrary message m', compute v' = h(m', r) and v = h(m, r). Also, we compute $u' = (v'/v)u = (v'/k)S_{ID}$. Then (u', r) is a valid signature of m' since

$$e(u',r) = e((v'/k)S_{ID}, kP) = e(S_{ID}, P)^{v'} = e(Q_{ID}, Q_{TA})^{v'}$$

and v' = h(m', r).

References

- [CC02] J. Cha and J. Cheon, An Identity-Based Signature from Gap Diffie-Hellman Groups, Available from http://eprint.iacr.org, 2002.
- [Hes02] F. Hess, Exponent group signature schemes and efficient identity based signature schemes based on pairings, Available from http://eprint.iacr.org, 2002.
- [Pat02] K. Paterson, ID-based signatures from pairings on elliptic curves, Available from http://eprint.iacr.org, 2002.
- [SOK01] R. Sakai, K. Ohgishi, and M. Kasahara, Cryptosystems based on pairing, Proc. of SCIS '00, Okinawa, Japan, Jan. pp. 26-28, 2001.