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Embracing Relational Abundance

REFERENCE: Michael Buchler, "Reconsidering Klumpenhouwer Networks," *Music Theory Online* 13.2

ABSTRACT: This brief essay addresses some concerns raised by Michael Buchler in "Reconsidering Klumpenhouwer Networks" (MTO 13.2) regarding the alleged promiscuity of K-nets and their use in music analyses.

Received August 2007

[1] In his provocative article "Reconsidering Klumpenhouwer Networks" (MTO 13.2), Michael Buchler offers readers a useful analogy comparing "network structures" to "modeling clay" [par. 46]. In Buchler's hands this is cast as a dangerous similarity, but in contrast I'm excited to take a seat at the potter's wheel and throw some clay in this brief response to his essay. As with many of Buchler's observations, his analogy is equally applicable to all we do as music analysts, rather than a critique specific to "K-nets and their analytical deployment" [par. 1]. Acknowledging at the outset that K-nets "are elegant structures," Buchler goes on to state that they open "Pandora's Box of relational permissiveness" and that "clearly, the more ways that it is possible to draw equivalent relations, the less significant those relations become" [par. 2]. The alleged clarity eludes me, so I'll take a more extreme position and suggest no relations are inherently significant, that is, I propose that all relations—common or rare—are comparably context dependent. I would reformulate Buchler's criticism to state that the relational abundance generated by K-nets further emphasizes that musicality, whatever that means in a given context, is in the hands and ears of the analyst rather than the theoretical apparatus itself.⁽¹⁾ Of course, this is nothing new; it's true for all of our interpretive work and all of our analytical models.

[2] Shifting analogies, performing music analysis is like storytelling. For example, despite his graceful precision, I don 抉 read David Lewin 抯 work for his mathematical proofs of abstract relations. Instead, I read Lewin 沮 essays because he was a gifted raconteur, a writer who spun compelling tales about specific musical passages, with the ability to alter my understanding of the selected music in a meaningful and permanent way.⁽²⁾ A convincing analysis forges a narrative pathway through a musical passage, and individual relations or transformations only gain meaning in the context of the story. I might even suggest that relations, as well as our desire to create them, are merely a byproduct of the temporal nature of music. From this perspective, Buchler's repeated emphasis on "relatedness" as a central problem in K-net analyses, particularly the greater abstraction of potential relatedness, is off target. I will directly address some of his criticisms of K-net mechanics in the next section, but first I must note that when these abstract relations have no intrinsic meaning, the only remaining analytical benchmark is how persuasive we find any individual narrative. Again, musical relevance as the measure for our analyses is not K-net specific; it applies to all our endeavors. We are writing analytical fictions about musical gestures as they unfold in time and/or space.

[3] Although Buchler's primary concern with K-nets is their potential promiscuity, he only compares them to the canonical operators transposition and inversion. Furthermore, he does so in terms of the abstract equivalence classes generated by those very operations, thus stacking the deck against K-nets. A good example is his defamatory characterization of [026]: "once [026] comes to the party, every other trichord enjoys at least one mutual relation" [par 36]. While the metaphor is entertaining, [026] can never come to the analytical party, only a member of [026] can occur in a musical work. In the literature under examination, transformations occur among pcsets, generally not set classes. In that practical context, K-net promiscuity is not nearly the serious problem suggested by Buchler. In the puritanical world of canonical transforms, $\{0,2,6\}$ can only have relations with twenty-three of the remaining possible 4,094 pcsets; that \Re less than 1% of the population.⁽³⁾ This inability to communicate with other pcsets creates glaring problems of fragmentation and gaps in many post-tonal analyses.⁽⁴⁾ In the more social circle of K-nets, $\{0,2,6\}$

can have relations with approximately 3.5% of the population, or up to 10.5% if one is willing to explore the multiple configurations afforded by *double emploi*.⁽⁵⁾ In other words, a K-net {0,2,6} is still rather discerning in rejecting 90–96% of its potential suitors, and only against Buchler's backdrop of canonical set classes does a K-net {0,2,6} seem promiscuous. It's not freely partying with *all* the other 4,094 pcsets!

[4] Buchler is also careless in distinguishing "split" and "dual" transformations throughout his essay.⁽⁶⁾ While most readers will understand that he's using the terms as synonyms, with the word split referring to the act of parsing posets into two subsets, it's important to be careful about this seemingly minor distinction. If we're splitting pcsets to better describe the musical surface, one of Buchler's frequent pleas, what prevents us from splitting them into as many subsets as necessary to match the literal lines (registral, etc.) in the musical score? The answer is nothing, but that would be a virtual Bacchanalia, with all posets potentially having relations with all the others.⁽⁷⁾ Buchler provides an informal proof that any K-net partitions into exactly two T-sets [par. 17], and he then consistently limits himself to two subsets and dual transpositions in his analyses. As he demonstrates in his own proof, it is specifically the structure of K-nets that motivates and models this otherwise arbitrary constraint.⁽⁸⁾ The discriminating power of K-nets and dual transformations—allowing many times more relations than the canonical operators, yet filtering out most relations (90–96%)—is located at a comfortable place on the exclusivity-promiscuity continuum for many of us, thus yielding the large body of analytic literature in question.

[5] I agree with Buchler that 揹 ual transpositions or inversions?present 揳 simpler musical scenario?than K-nets [par. 19], and that many K-net analyses and abstractions would benefit by their inclusion.⁽⁹⁾ However, I disagree that "network-internal I_n values are unnecessary" [pars. 12 and 15]. Buchler's reasons for this statement are accurate; internal I_n arrows aren't necessary to recognize isography [par. 12] or calculate hyper transformations [par. 15], but they're still necessary for the unity of the musical sonorities participating in these transformations. Even when we hear the independent paths of two subsets in a dual transformation, we very often hear the

supersets as single, unified musical "objects," particularly in homorhythmic contexts. A good example would be Catherine Nolan's analysis of Webern's Das Augenlicht that Buchler champions as a successful use of K-nets [pars. 53?5].⁽¹⁰⁾ Is there anyone among us that doesn't hear the chorale sonorities in Buchler's Figure 24 (Nolan's Example 1a) as unified chords? If we only trace the paths of the independent T-sets, we emphasize the horizontal dimension at the expense of the vertical; it's an old, familiar problem. Furthermore, if we do eliminate the In arrows, then how and why are we relating the two internal T-sets? Do we only hear the separate, completely independent linear streams in such cases? If so, then what exactly do Buchler's vertical lines mean in his Figures 5, 6, 11, and so on? He declines to tell us.⁽¹¹⁾

[6] Let's "reconsider" one of Buchler's examples—the celli passage from the end of Lutoslawski's Symphony No. 4-to imagine an alternative reading. Depending on one's perspective, the narrative I present below will support Buchler's arguments, my own, or ideally, both. Figure 1 reproduces his example [Figure 14]. Listening to this passage, I immediately notice its saturation with ic5s, as well as the contour pattern (<013245>) that Buchler emphasizes. However, these sounds don't lead me to hear his three motivic hexachords, but rather the six component trichords defined by that contour. I also notice that almost all six are quartal harmonies, or members of sc [027], but I don't necessarily hear them as transpositions of one another. Instead, the contour pattern highlights the semitones between the paired trichords. I summarize this initial aural impression in Figure 2.



(click to enlarge and listen)

Figure 2. An initial aural impressi

[7] While Buchler "intuitively" prefers "simple transformations" whenever possible [par. 29], I don't particularly hear the progressions c3–c4 and c5–c6 as T_6 (or I_0 and I_2 respectively), despite the ability to interpret them in that manner. I hear them as T_1 ish as shown by the arrows in my figure. If I want a model that emphasizes the T_1 s in these motions, then the remaining tones—first and last, lowest and highest—must leapfrog around the T_1 dyad pairs, yielding the dual transpositions shown in Figure 3, which best captures what I hear happening within Buchler's three motives. If we continue the narrative to link the motives by undoing the registral permutations shown in Figure 3, we arrive at Figure 4.⁽¹²⁾ Imagining his motives 2 and 3 as a dual T_7/T_7 particularly disturbs Buchler, but the mappings in the smaller stages of my Figure 4, T_1/T_4 followed by T_6/T_3 in the paired trichords, illustrate why one might interpret it this way. Furthermore, it shows what's similar about T_2/T_0 and T_7/T_7 in this particular musical circumstance.

Figure 3. Dual transpositions modeling Buchler's three motives





(click to enlarge)

[8] Figure 5 illustrates these motions K-net in form. Each row in the figure is one of Buchler's motives, the and hyper-transforms



(click to enlarge)

Figure 5. K-nets modeling all six trichords

within each row are the dual transpositions between my trichords. As a music theorist, I can't help notice but the correspondence between the T₅s that saturate this entire passage and the $< T_5 > s$ that define Buchler's motives 2 and 3 (c3-c4 and c5–c6) in this model. Are they the same thing? Well, yes and They're both no. transpositions of five semitones, but the objects being transposed are different; one is a literal pitch and the other is an inversional wedge. One might think of it as a transposition of an expectation. For example, we may expect the singleton



(click to enlarge)

in c4 to be D[#] to balance the semitone climb of the dyad, but instead we get its T₅ transform, G[‡], and that's what the $\langle T5 \rangle$ represents. Buchler's surface criticisms of hyper-transformations are well worth discussing, but perhaps the more cogent question is: can we musically justify this underlying expectation for inversional balance? I 抣 l leave any further of discussion this topic for other respondents, and instead return to my reading of the celli passage.⁽¹³⁾

[9] Playing the role of Buchler's fatally flawed K-net analyst, I blindly fall victim to the elegant seduction of $\langle T_5 \rangle$. I'm powerless to prevent myself from producing Figure 6. The upper nodes in this supernetwork, the Figure 6. An irresistible supernetwork

<T-sets>, keep the two final two motives intact and emphasize the isography between the primary interval of the passage, T_5 , and the dual transposition, T_1/T_4 or $\langle T_5 \rangle$, that generates these two motives. Networks c1 and c2 must be inverted to create the negative isography shown in the figure, but this still keeps the first motive intact, as it doesn't affect the T_1 surface mapping that generates the motive.⁽¹⁴⁾ Finally, though my reinterpretation of this passage may convincingly seem to support Buchler's complaints regarding K-net promiscuity and malleability, the middleground network in Figure 6 is actually quite an exclusive structure. If we've traveled through the celli passage until the final trichord, c6, there are only twelve posets that can complete this <<T₅>> network, and that's already a more exclusive group than many of our canonical set classes, but if we wish to retain the T_1 -ness that defines our motive and still complete this isographic supernetwork, c6 is the sole pcset capable of that accomplishment.⁽¹⁵⁾ However, this interpretation may be too far down the road of abstraction for some readers.



(click to enlarge)

[10] I thoroughly enjoyed Buchler's essay and firmly believe all of our ideas should receive this kind of intense public scrutiny. His clear explanation of K-nets and dual transformations are an excellent primer on these concepts, and I plan to make it required reading in several courses. I find myself agreeing with many of his proposed refinements in K-net practice, such as including dual transformation labels, and further distinguishing among types of isography ("consistent, grand," etc.) [par. 30]. He also successfully highlights many problem areas in K-net practice, such as repeating and omitting tones [pars. 52 and 65], and perceptual difficulties, such as hearing $\langle I_n \rangle$ [par. 56]. On the other hand, I don't always agree with Buchler's subsequent conclusions. I'm not ready to dump internal In arrows, <In>, or even recursion yet, though I'm always willing to revisit the question. As I hope my brief analysis illustrates, supernetworks can fall out of an analysis; they're not always the result of the difficult and manipulative search portrayed in Buchler's essay [pars. 64-65]. Rather than fearing the proliferation of possibilities afforded by K-nets and their alleged promiscuity, we should embrace this relational abundance and use it as justification for further exploration.