# New Impossible Differential Attacks of Reduced-Round Camellia-192 and Camellia-256 ${ }^{\star}$ 

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#### Abstract

Camellia is a block cipher selected as a standard by ISO/IEC, which has been analyzed by a number of cryptanalysts. In this paper, we propose several 6 -round impossible differential paths of Camellia with the $F L / F L^{-1}$ layer in the middle of them. With the impossible differential and a well-organized precomputational table, impossible differential attacks on 11-round Camellia-192 and 12-round Camellia-256 are given, the time complexity of which are $2^{184.8}$ and $2^{248.7}$ respectively. An impossible differential attack on 15 -round Camellia- 256 without $F L / F L^{-1}$ layers and whitening is also be given, which is about 64 times faster than exhaustive search. To the best of our knowledge, these are the best cryptanalytic results of Camellia-192/-256 with $F L / F L^{-1}$ layers and Camellia256 without $F L / F L^{-1}$ layers to date.


Key words: Camellia Block Cipher, Cryptanalysis, Impossible Differential Path, Impossible Differential Attack.

## 1 Introduction

Block cipher Camellia is proposed by NTT and Mitsubishi in 2000 [1]. Its block size is 128 bits and it supports 128 -, 192- and 256 -bit key sizes with 18,24 and 24 rounds respectively. Camellia was selected as an e-government recommended cipher by CRYPTREC [5] and recommended in NESSIE [15] block cipher portfolio. Then it was selected as an international standard by ISO/IEC.

The structure of Camellia is Feistel structure with $F L / F L^{-1}$ layers inserted every 6 rounds. The $F L$ and $F L^{-1}$ functions are keyed linear functions which are designed to provide nonregularity across rounds [1]. In the past years, Camellia has attracted the attention of the cryptanalytic community. The square-type attacks are efficient to attack Camellia, which can be used to analysis 9-round Camellia-128 and 10-round Camellia-256 [11. Furthermore, Hatano et al. used the higher order differential attack to analysis the last 11 rounds Camellia-256 with complexity $\left.2^{255.6} \quad 7\right]$.

There are a number of results on the simple versions of Camellia which exclude the $F L / F L^{-1}$ layers and whitening being given in recent years [10|13|6|19|14|18|16|17]. Among them, the impossible differential attacks [3] are most efficient [17|13|14]18]. Since the existence of $F L / F L^{-1}$ layers will probably destroy the impossibility, non of the impossible differential paths in these attacks includes the $F L / F L^{-1}$ layers. In this paper, we present 6 -round impossible differential paths with $F L / F L^{-1}$ layers in the middle, which turn out to be first impossible differential paths with $F L / F L^{-1}$ layers. Due to one of these impossible differential paths and a precomputational table that is carefully consturcted, we propose impossible differential attacks on 11-round Camellia-192 and 12-round Camellia-256 with complexity $2^{184.8}$ and $2^{248.7}$ respectively.

[^0]For the attacks of Camellia-256 without $F L / F L^{-1}$ layers and whitening, the 14 -round attack in [13] was pointed out to be incorrect by [20]. Later Mala et al. [14] pointed out a flaw in [20] and showed that the time complexities of the 12 -round Camellia-128 and 16-round Camellia-256 attack were more than exhaustive search. As a result, the best analysis of Camellia-256 without $F L / F L^{-1}$ layers and whitening dated back to [12], which was a 13 -round attack with complexity $2^{211.7}$. By carefully using the subkey relations and one of the 8 -round impossible differential paths without $F L / F L^{-1}$ layers proposed in [18], we also present an impossible differential attack on 15 -round Camellia-256 without $F L / F L^{-1}$ layers and whitening, and the complexity is about $2^{248.4}$ encryptions.

The rest of this paper is organized as follows. We give some notations and a brief description of Camellia in Section 2. Some properties and 6-round impossible differential paths with $F L / F L^{-1}$ layers of Camellia are given in Section33. Section 4 describes the impossible differential attacks on reduced-round Camellia with $F L / F L^{-1}$ layers and whitening. The impossible differential attack on 15 -round Camellia-256 without $F L / F L^{-1}$ layers and whitening is illustrated in Section 5 . Finally, we conclude the paper in Section 6.

## 2 Preliminaries

Some notions used in this paper and a simple description of the Camellia algorithm are given in this section.

### 2.1 Notations

$L^{r-1}, L^{\prime r-1}$ : the left half of the 128 -bit $r$-th round input
$R^{r-1}, R^{r-1}$ : the right half of the 128 -bit $r$-th round input
$\Delta L^{r-1}$ : the difference of $L^{r-1}, L^{\prime r-1}$
$\Delta R^{r-1}$ : the difference of $R^{r-1}, R^{r-1}$
$S^{r}, S^{\prime r}$ : the output value of the S -box of the $r$-th round
$\Delta S^{r}$ : the output difference of the S-box of the $r$-th round
$k^{r}$ : the 64 -bit $r$-th round subkey,
$A_{i}$ : the $i$-th byte of a 64 -bit value $A(i=1, \ldots, 8)$
$B \lll j$ : left rotation of $B$ by $j$ bits
$X_{L(64)}$ : the left half of a 128 -bit word $X$
$X_{R(64)}$ : the right half of a 128 -bit word $X$
$Y_{L(32)}$ : the left half of a 64 -bit word $Y$
$Y_{R(32)}$ : the right half of a 64 -bit word $Y$
$\|$ : the cascade of two words

### 2.2 The Camellia Algorithm

Camellia 1 is a 128 -bit block cipher with Feistel structure. It has 18 rounds for 128 -bit key, and 24 rounds for 192-/256-bit key. We give the encryption procedure of Camellia-192/-256 as follows, see Fig. 1 .
Encryption Procedure. The input of the encryption procedure is a 128 -bit plaintext $M$, and 64 -bit subkeys $k^{w i}(i=1, \ldots, 4), k^{r}(r=1, \ldots, 24)$ and $k l^{j}(j=1, \ldots, 6)$. First $M$ is XORed with $k^{w 1}$ and $k^{w 2}$ to get two 64 -bit intermediate value $L^{0}$ and $R^{0}: L^{0} \| R^{0}=M \oplus\left(k^{w 1} \| k^{w 2}\right)$. Then the following operations are carried out for $i=1$ to 24 , expect for $r=6,12$ and 18:

$$
L^{r}=R^{r-1} \oplus F\left(L^{r-1}, k^{r}\right), R^{r}=L^{r-1} .
$$



Fig. 1. Camellia-192/-256

For $r=6,12$ and 18, do the following:

$$
\begin{aligned}
L^{\prime r} & =R^{r-1} \oplus F\left(L^{r-1}, k^{r}\right), R^{\prime r}=L^{r-1} . \\
L^{r} & =F L\left(L^{\prime r}, k l^{2 r / 6-1}\right), R^{r}=F L^{-1}\left(R^{\prime r}, k l^{2 r / 6}\right) .
\end{aligned}
$$

Finally the 128 -bit ciphertext $C$ is computed as: $C=\left(R^{24} \| L^{24}\right) \oplus\left(k^{w 3} \| k^{w 4}\right)$.
The $F L$ function is defined as: $\left(X_{L(32)}\left\|X_{R(32)}, k l_{L(32)}\right\| k l_{R(32)}\right) \mapsto\left(Y_{L(32)} \| Y_{R(32)}\right)$, where:

$$
\begin{aligned}
Y_{R(32)} & =\left(\left(X_{L(32)} \cap k l_{L(32)}\right) \lll 1\right) \oplus X_{R(32)}, \\
Y_{L(32)} & =\left(Y_{R(32)} \cup k l_{R(32)}\right) \oplus X_{L(32)} .
\end{aligned}
$$

The $F L^{-1}$ function is the inverse of $F L$ function, and $F L$ and $F L^{-1}$ are linear as long as the key is fixed [2].

The round function $F$ is composed of the key-addition layer, S-box layer and linear transformation $P$. In the key-addition layer, the input of the round function is XORed with the subkey. There are $48 \times 8$ S-boxes $S_{1}, S_{2}, S_{3}, S_{4}$ used in the S-box layer, and each S-box is used twice. Finally, the linear transformation $P:\left(\{0,1\}^{8}\right)^{8} \rightarrow\left(\{0,1\}^{8}\right)^{8}$ maps $\left(z_{1}, \ldots, z_{8}\right) \rightarrow\left(y_{1}, \ldots, y_{8}\right) . P$ function and its inverse function $P^{-1}$ are:

$$
\begin{array}{ll}
y_{1}=z_{1} \oplus z_{3} \oplus z_{4} \oplus z_{6} \oplus z_{7} \oplus z_{8} & z_{1}=y_{2} \oplus y_{3} \oplus y_{4} \oplus y_{6} \oplus y_{7} \oplus y_{8} \\
y_{2}=z_{1} \oplus z_{2} \oplus z_{4} \oplus z_{5} \oplus z_{7} \oplus z_{8} & z_{2}=y_{1} \oplus y_{3} \oplus y_{4} \oplus y_{5} \oplus y_{7} \oplus y_{8} \\
y_{3}=z_{1} \oplus z_{2} \oplus z_{3} \oplus z_{5} \oplus z_{6} \oplus z_{8} & z_{3}=y_{1} \oplus y_{2} \oplus y_{4} \oplus y_{5} \oplus y_{6} \oplus y_{8} \\
y_{4}=z_{2}^{\oplus} z_{3} \oplus z_{4}^{\oplus} z_{5} \oplus z_{6} \oplus z_{7} & z_{4}=y_{1} \oplus y_{2} \oplus y_{3} \oplus y_{5}^{\oplus} y_{6} \oplus y_{7} \\
y_{5}=z_{1}^{\oplus} z_{2} \oplus z_{6} \oplus z_{7} \oplus z_{8} & z_{5}=y_{1} \oplus y_{2} \oplus y_{5} \oplus y_{7}^{\oplus} y_{8} \\
y_{6}=z_{2}^{\oplus} z_{3} \oplus z_{5} \oplus z_{7} \oplus z_{8} & z_{6}=y_{2} \oplus y_{3} \oplus y_{5} \oplus y_{6} \oplus y_{8} \\
y_{7}=z_{3} \oplus z_{4} \oplus z_{5} \oplus z_{6} \oplus z_{8} & z_{7}=y_{3} \oplus y_{4} \oplus y_{5} \oplus y_{6} \oplus y_{7} \\
y_{8}=z_{1} \oplus z_{4} \oplus z_{5} \oplus z_{6} \oplus z_{7} & z_{8}=y_{1} \oplus y_{4} \oplus y_{6} \oplus y_{7} \oplus y_{8}
\end{array}
$$

Key Schedule. For Camellia-256, the 256 -bit main key $K=K_{L} \| K_{R}$, where $K_{L}$ and $K_{R}$ are 128 bits. And for Camellia-192, the 192-bit main key $K=K_{L} \| K_{R L(64)}$ and $K_{R R(64)}=\overline{K_{R L(64)}}$. Using $K_{L}$ and $K_{R}$, the key schedule algorithm first calculate $K_{A}$ and $K_{B}$, which is described in


Fig. 2. The Calculation of $K_{A}$ and $K_{B}$

Fig. 2. Where $F$ is the round function of Camellia and $C_{i}(1 \leq i \leq 6)$ are constants used as the keys. Then the subkeys $k^{w i}(i=1, \ldots, 4), k^{r}(r=1, \ldots, 24)$ and $k l^{j}(j=1, \ldots, 6)$ are derived from rotating $K_{L}, K_{R}, K_{A}$ or $K_{B}$. For details of Camellia, we refer to [1].

It can be known from Fig. 2 that, if $K_{B}$ and $K_{R}$ are known, $K_{A}$ is known. Therefore, one can get $K_{L}$ using the relation between $K_{L}$ and $K_{A}$ described in [14], Section 3.2. So once $K_{B}$ and $K_{R}$ are known, $K$ can be computed.

## 3 Properties and 6-Round Impossible Differential Paths of Camellia with $\boldsymbol{F L} / \boldsymbol{F} L^{-1}$ Functions

In this section, we first give some useful properties of Camellia and then propose several impossible differential paths.

Property 1 For a 3-round Camellia structure, if the input difference is of the form $\Delta L^{i}=$ $(0, a, 0,0,0,0,0,0), \Delta R^{i}=(0,0,0,0,0,0,0,0)$, then:
$\Delta L^{i+1}=(0, b, b, b, b, b, 0,0), \Delta S^{i+2}=\left(0, b_{2}, b_{3}, b_{4}, b_{5}, b_{6}, 0,0\right)$,
$\Delta L^{i+2}=\Delta R^{i+3}=P\left(a, b_{2}, b_{3} \oplus a, b_{4} \oplus a, b_{5} \oplus a, b_{6} \oplus a, 0,0\right)$,
and $\Delta S_{l}^{i+3}=\left(P^{-1}\left(\Delta L^{i+3}\right)\right)_{l}$, for $l=1,3,4, \ldots, 8$, where a, $b, b_{2}, b_{3}, b_{4}, b_{5}, b_{6}$ are non-zero bytes.
Property 2 The necessary conditions of $\Delta L^{i+3}=(0, a, 0,0,0,0,0,0)$ and $\Delta R^{i+3}=(0,0,0,0,0$, $0,0,0)$ are:
$\Delta L^{i+1}=(0, b, b, b, b, b, 0,0), \Delta S^{i+2}=\left(0, b_{2}, b_{3}, b_{4}, b_{5}, b_{6}, 0,0\right)$,
$\Delta L^{i}=P\left(a, b_{2}, b_{3} \oplus a, b_{4} \oplus a, b_{5} \oplus a, b_{6} \oplus a, 0,0\right)$,
and $\Delta S_{l}^{i+1}=\left(P^{-1}\left(\Delta R^{i}\right)\right)_{l}$, for $l=1,3,4, \ldots, 8$, where $a, b, b_{2}, b_{3}, b_{4}, b_{5}, b_{6}$ are non-zero bytes.
To better describe the properties, we also illustrate them in Fig. 3. Actually, the proofs of the properties are similar and the proof Property 1 is given as an example.

Proof. Apparently, $\Delta S^{i+1}$ is of the form $(0, b, 0,0,0,0,0,0)$, where $b$ an is unknown non-zero byte. And $\Delta L^{i+1}=(0, b, b, b, b, b, 0,0)$ as $P$ function is linear. After the key-addition layer and


Fig. 3. Properties of 3-round Camellia

S-box layer, it can be obtained that $\Delta S^{i+2}=\left(0, b_{2}, b_{3}, b_{4}, b_{5}, b_{6}, 0,0\right)$, where $b_{2}, b_{3}, b_{4}, b_{5}$ and $b_{6}$ are unknown non-zero bytes.

Since $\Delta L^{i+2}=\Delta S^{i+2} \oplus \Delta L^{i}$ and $P^{-1}\left(\Delta L^{i}\right)=(a, 0, a, a, a, a, 0,0)$,

$$
\Delta L^{i+2}=P\left(a, b_{2}, b_{3} \oplus a, b_{4} \oplus a, b_{5} \oplus a, b_{6} \oplus a, 0,0\right)
$$

Finally, because $\Delta S^{i+3}=P^{-1}\left(\Delta L^{i+1} \oplus \Delta L^{i+3}\right), P^{-1}\left(\Delta L^{i+1}\right)=(0, b, 0,0,0,0,0,0)$ and $P^{-1}$ function is linear,

$$
\Delta S_{l}^{i+3}=\left(P^{-1}\left(\Delta L^{i+3}\right)\right)_{l}, \text { for } l=1,3,4, \ldots, 8
$$

Property 3 (from [9]) Let $x, x^{*}$ be 32-bit values, and $x^{\prime}=x \oplus x^{*}$, then the differential properties of $A N D$ and $O R$ operations are:

$$
\begin{aligned}
& (x \cap k) \oplus\left(x^{*} \cap k\right)=\left(x \oplus x^{*}\right) \cap k=x^{\prime} \cap k \\
& (x \cup k) \oplus\left(x^{*} \cup k\right)=(x \oplus k \oplus(x \cap k)) \oplus\left(x^{*} \oplus k \oplus\left(x^{*} \cap k\right)\right)=x^{\prime} \oplus\left(x^{\prime} \cap k\right)
\end{aligned}
$$

Property 4 Let $M=\left(m_{1}, m_{2}, m_{3}, m_{4}, m_{5}, m_{6}, m_{7}, m_{8}\right)$ be the input difference of $F L$ function, and $N=\left(n_{1}, n_{2}, n_{3}, n_{4}, n_{5}, n_{6}, n_{7}, n_{8}\right)$ be the the output difference of $F L$, where $n_{l}, m_{l}(l=$ $1, \ldots, 8)$ are arbitrary 8-bit values. Then if $n_{i}=0(i \in\{5,6,7,8\}), n_{i-4}=m_{i-4}$.

Proof. Let us denote the subkey used for AND operation as $k_{L}$ and the subkey used for OR operation as $k_{R}$. By Property 3, the following equations must hold:

$$
\begin{array}{r}
\left(\left(M_{L} \cap k_{L}\right) \lll 1\right) \oplus M_{R}=N_{R} \\
M_{L} \oplus N_{R} \oplus\left(N_{R} \cap k_{R}\right)=N_{L} \tag{1}
\end{array}
$$

Then if $n_{i}=0(i \in\{5,6,7,8\})$, it can be deduced from Equation (1) that $n_{i-4}=m_{i-4}$.

Impossible Differential. Now we demonstrate that the 6 -round differential in Fig. 4 is impossible. The input difference is

$$
((0,0,0,0,0,0,0,0) ;(0, a, 0,0,0,0,0,0))
$$

where $a$ is arbitrary non-zero byte. The output difference of the first round is

$$
((0, a, 0,0,0,0,0,0) ;(0,0,0,0,0,0,0,0))
$$



Fig. 4. 6-round impossible differential path with the $F L / F L^{-1}$ layer in the middle

Then by Property 1, the output differences of the second and third round are

$$
((0, b, b, b, b, b, 0,0) ;(0, a, 0,0,0,0,0,0)) \text { and }\left(\left(c_{1}, c_{2} \oplus a, c_{3}, c_{4}, c_{5}, c_{6}, c_{7}, c_{8}\right) ;(0, b, b, b, b, b, 0,0)\right)
$$

with probability 1 , as long as

$$
\left(c_{1}, c_{2}, c_{3}, c_{4}, c_{5}, c_{6}, c_{7}, c_{8}\right)=P\left(0, b_{2}, b_{3}, b_{4}, b_{5}, b_{6}, 0,0\right),
$$

where $b, b_{2}, b_{3}, b_{4}, b_{5}, b_{6}$ are unknown non-zero bytes, $\left(0, b_{2}, b_{3}, b_{4}, b_{5}, b_{6}, 0,0\right)$ is evolved from $(0, b, b, b, b, b, 0,0)$ after the $S$-box layer and $c_{l}(l=1, . ., 8)$ are unknown bytes.

Similarly, in the backward direction, we know that for arbitrary non-zero byte $e$, if the output difference of the sixth round is

$$
((0, e, 0,0,0,0,0,0) ;(0,0,0,0,0,0,0,0)),
$$

then the input difference of the forth round is

$$
\left((0, d, d, d, d, d, 0,0) ;\left(f_{1}, f_{2} \oplus e, f_{3}, f_{4}, f_{5}, f_{6}, f_{7}, f_{8}\right)\right)
$$

where $d$ is an unknown non-zero byte and $f_{l}(l=1, . ., 8)$ are unknown bytes.
Now the input and output differences of the $F L$ function are determined. It can be deduced from Property 4 that $c_{3}=d$ and $c_{4}=d$, which means $c_{3}=c_{4}$. But this implies $b_{4}=0$ as

$$
\begin{aligned}
& c_{3}=b_{2} \oplus b_{3} \oplus b_{5} \oplus b_{6}, \\
& c_{4}=b_{2} \oplus b_{3} \oplus b_{4} \oplus b_{5} \oplus b_{6},
\end{aligned}
$$



Fig. 5. Impossible Differential Attacks on 11-round Camellia-192 and 12-round Camellia-256 with whitening and $F L / F L^{-1}$
which contradict $b_{4} \neq 0$. (By the input and output difference of $F L^{-1}$ function, we can also deduce another contradiction that $\left.d_{4}=0 \nLeftarrow d_{4} \neq 0\right)$. As a result, the differential

$$
((0,0,0,0,0,0,0,0) ;(0, a, 0,0,0,0,0,0)) \xrightarrow{6-\text { round }}((0, e, 0,0,0,0,0,0) ;(0,0,0,0,0,0,0,0))
$$

is impossible.
Actually, there are three more 6 -round impossible differential paths with the $F L / F L^{-1}$ layer in the middle, which are:

$$
\begin{aligned}
& ((0,0,0,0,0,0,0,0) ;(a, 0,0,0,0,0,0,0)) \stackrel{\substack{6-\text { round }}}{\text { rond }}((e, 0,0,0,0,0,0,0) ;(0,0,0,0,0,0,0,0)) \\
& ((0,0,0,0,0,0,0,0) ;(0,0, a, 0,0,0,0,0)) \xrightarrow{6-\text { round }}((0,0, e, 0,0,0,0,0) ;(0,0,0,0,0,0,0,0)) \\
& ((0,0,0,0,0,0,0,0) ;(0,0,0, a, 0,0,0,0)) \stackrel{6-\text { rond }}{\nrightarrow \longrightarrow}((0,0,0, e, 0,0,0,0) ;(0,0,0,0,0,0,0,0))
\end{aligned}
$$

## 4 Impossible Differential Attack on Camellia with $\boldsymbol{F L} / \boldsymbol{F} L^{-1}$ functions and whitening

In this section, we present impossible differential attacks on 11-round Camellia-192 and 12-round Camellia-256 using the impossible differential in Section 3 .

### 4.1 Impossible Differential Attack on 11-Round Camellia-192

We add 3 rounds on the top and 2 rounds on the bottom of the 6 -round impossible differential path to analysis 11-round Camellia-192, see Fig. 5 in the left. Denote $k^{a}=k^{w 1} \oplus k 1, k^{b}=$ $k^{w 2} \oplus k^{2}, k^{c}=k^{w 1} \oplus k^{3}, k^{d}=k^{w 4} \oplus k^{10}$ and $k^{e}=k^{w 3} \oplus k^{11}$. The attack is started by carrying
out a precomputation.
Precomputation. A precomputational table $H$ for round 2-3 is set up here, which contains the all possible pairs that can follow the differential in rounds 2-3 and their corresponding subkeys $k^{b}, k_{2}^{c}$. This table can also be used for rounds $10-11$, as in the backward direction, the differences are the same as that of rounds 2-3. The table is constructed as follows:

For every $\left(L^{1}, g, k^{b}, L_{2}^{2}, a, k_{2}^{c}\right)$, compute $L^{\prime 1}=L^{1} \oplus(0, g, g, g, g, g, 0,0), T=F\left(L^{1}, k^{b}\right), T^{\prime}=$ $F\left(L^{\prime 1}, k^{b}\right), \Delta T=T \oplus T^{\prime}$ and sieve the ones satisfying $S\left(L_{2}^{2} \oplus k_{2}^{c}\right) \oplus S\left(L_{2}^{2} \oplus a \oplus k_{2}^{c}\right)=g$, where $g$ and $a$ are non-zero bytes. There are $2^{160}\left(L^{1}, g, k^{b}, L_{2}^{2}, a, k_{2}^{c}\right)$, and $2^{152}$ of which remain after the sieve. Then insert $\left(k^{b}, k_{2}^{c}\right)$ into the row indexed by ( $L^{1}, g, \Delta T \oplus a, L_{2}^{2} \oplus T_{2}$ ). Because there are only $2^{40} \Delta T$ which lead to $2^{48} \Delta T \oplus a$, there are $2^{128}$ rows in $H$ and each row contains $2^{24}$ 72 -bit subkeys $\left(k^{b}, k_{2}^{c}\right)$. Consequently, the memory complexity of the table is about $2^{155.2}$ bytes and the time complexity of the precomputation is less than $2^{161}$ one round encryptions.

Data Collection. Choose $2^{n}$ structures of plaintexts, and each structure contains plaintexts with the following form:

$$
\left(P\left(y_{1}, y_{2}, y_{3}, y_{4}, y_{5}, y_{6}, \alpha, \beta\right) ;\left(x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}, x_{8}\right)\right)
$$

where $y_{i}(i=1, \ldots, 6)$ and $x_{j}(j=1, \ldots, 8)$ take all possible values and $\alpha, \beta$ are fixed in each structure. As a result, there are $2^{112}$ plaintexts in each structure and we can get $2^{n} \times 2^{112 \times 2-1}=$ $2^{n+223}$ plaintext pairs totally. For each of the pairs, $\Delta\left(P^{-1}\left(L^{0}\right)\right)_{7}=0, \Delta\left(P^{-1}\left(L^{0}\right)\right)_{8}=0$.

Encrypt the plaintexts in each structure to get the corresponding ciphertexts, and keep the pairs whose ciphertext differences satisfy the following form by birthday birthday:

$$
\left((0, h, h, h, h, h, 0,0) ; P\left(e, h_{2}, e \oplus h_{3}, e \oplus h_{4}, e \oplus h_{5}, e \oplus h_{6}, 0,0\right)\right),
$$

where $e, h, h_{2}, h_{3}, h_{4}, h_{5}$ and $h_{6}$ are non-zero bytes. So there are $2^{n+223-72}=2^{n+151}$ pairs remaining.

Key Recovery. In the key recovery procedure, we use Property 2 and the precomputational table to discard the wrong keys.

1. Individually guess $k_{l}^{a}(l=1,3, \ldots, 8)$ and check whether the equation $\triangle S_{l}^{1}=\left(P^{-1}\left(\triangle R^{0}\right)\right)_{l}$ holds. About $2^{n+151} \times 2^{-56}=2^{n+95}$ pairs will be kept. Next guess $k_{2}^{a}$, so ( $L^{1}, L^{\prime 1}$ ) can be computed.
2. Initialize a table $\Gamma_{1}$ of $2^{72}$ all possible values $\left(k^{b}, k_{2}^{c}\right)$, for each of the remaining $2^{n+95}$ pairs, access the row ( $L^{1}, \Delta L_{2}^{1}, \Delta R^{1}, R_{2}^{1}$ ) in table $H$. Then for each value in the row, remove the corresponding value from $\Gamma_{1}$.
3. Initialize a table $\Gamma_{2}$ of $2^{72}$ all possible values ( $k^{e}, k_{2}^{d}$ ), for each of the remaining $2^{n+95}$ pairs, access the row ( $L^{11}, \Delta L_{2}^{11}, \Delta L^{12}, L_{2}^{12}$ ) in table $H$. Then for each value in the row, remove the corresponding value from $\Gamma_{2}$.
4. If neither $\Gamma_{1}$ nor $\Gamma_{2}$ is empty, output the 208-bit value ( $k^{a}, k^{b}, k_{2}^{c}, k_{2}^{d}, k^{e}$ ), otherwise go to Step 1 and try another guess. The main key can be recovered when ( $k^{a}, k^{b}, k_{2}^{c}, k_{2}^{d}, k^{e}$ ) is obtained, which will be described as follows.
The following equations are deduced from Table 3 in [1]:

$$
\begin{align*}
k^{a} & =\left(K_{L} \lll 0\right)_{L} \oplus\left(K_{B} \lll 0\right)_{L},  \tag{2}\\
k^{b} & =\left(K_{L} \lll 0\right)_{R} \oplus\left(K_{B} \lll 0\right)_{R},  \tag{3}\\
k^{c} & =\left(K_{L} \lll 0\right)_{L} \oplus\left(K_{R} \ll 15\right)_{L},  \tag{4}\\
k^{e} & =\left(K_{B} \ll 111\right)_{L} \oplus\left(K_{A} \lll 45\right)_{L},  \tag{5}\\
k^{d} & =\left(K_{B} \lll 111\right)_{R} \oplus\left(K_{L} \lll 45\right)_{R} . \tag{6}
\end{align*}
$$

We guess every possible value of $K_{L}$, for each guess $K_{B}$ can be calculated by Equations (2) and (3), then sieve this ( $K_{L}, K_{B}$ ) pair by Equation (6). For the ( $K_{L}, K_{B}$ ) that satisfy Equation (6), further compute 64 bits of $K_{A}$ by Equation (5). By the key schedule of Camellia-192, $K_{R}$ can be fully determined by $K_{B}$ and the 64 bits of $K_{A}$. Equation (4) will reduce the keys by a factor of $2^{8}$. So we get about $2^{128} \times 2^{-8} \times 2^{-8}=2^{112}\left(K_{L}, K_{R}\right)$ and the right $K=K_{L} \| K_{R}$ can be obtained by trial encryption.

Complexity. We choose $n=9$, then the data complexity is $2^{121}$ chosen plaintexts. Step 2 discards $2^{24}$ wrong $\left(k^{b}, k_{2}^{c}\right)$ and $2^{24}$ wrong $\left(k^{e}, k_{2}^{d}\right)$ are removed in Step 3 . For each pair remained after Step 1, $\frac{2^{48}}{2^{144}}=2^{-96}$ of wrong $\left(k^{b}, k_{2}^{c}, k_{2}^{d}, k^{e}\right)$ are removed. Consequently, the number of remaining wrong 208-bit value ( $k^{a}, k^{b}, k_{2}^{c}, k_{2}^{d}, k^{e}$ ) after analyzing all the pairs is $2^{64} \times 2^{144} \times(1-$ $\left.2^{-96}\right)^{2^{104}} \approx 0$.

The complexity of Step 1 is about $2 \times\left(\sum_{i=1}^{7} 2^{128-8(i-1)} \times 2^{8 i}\right) \times \frac{1}{8}+2 \times 2^{64} \times 2^{104} \approx 2^{169}$ one round encryptions, equivalent to $2^{165.7}$ encryptions. There are $2^{24}$ values in $H$, so in Step 2, $2^{24}$ memory access to $H$ and $2^{24}$ memory access to $\Gamma_{1}$ are needed for each pair, which result in $2^{64} \times 2^{104} \times\left(2^{24}+2^{24}\right)=2^{193}$ memory access. As one memory access is equivalent to one XOR operation and there are 52 XOR operations in one round Camellia, the complexity of Step 2 is about $2^{193} \times \frac{1}{52} \times \frac{1}{11} \approx 2^{183.8} 11$-round encryptions. The complexity of Step 3 is the same as Step 2. The complexity of Step 4 is about $2^{128}$ XOR operations, so the time complexity is about $2^{184.8}$ encryptions and the memory complexity is about $2^{155}$ bytes.

Obviously, this attack is applicable to 11-round Camellia-256 as well, furthermore, the attack can be extended to 12 -round Camellia-256, see the next subsection.

### 4.2 Impossible Differential Attack on 12-Round Camellia-256

We add an additional round on the bottom of the 11-round attack, and give an attack on 12round Camellia-256, see Fig. 5 in the right. The choice of plaintexts is the same as the 11-round attack, and the ciphertext pairs are sieved by the difference:

$$
\left(P\left(e, h_{2}, e \oplus h_{3}, e \oplus h_{4}, e \oplus h_{5}, e \oplus h_{6}, 0,0\right) ;(?, ?, ?, ?, ?, ?, ?, ?)\right),
$$

where $e, h, h_{2}, h_{3}, h_{4}, h_{5}, h_{6}$ are non-zero values and "?" stands for any bytes. After the sieve, about $2^{216}$ pairs remain.

Denote the equivalent subkeys $k^{a}=k^{w 1} \oplus k 1, k^{b}=k^{w 2} \oplus k^{2}, k^{c}=k^{w 1} \oplus k^{3}, k^{d}=k^{w 3} \oplus k^{10}$, $k^{e}=k^{w 4} \oplus k^{11}$ and $k^{f}=k^{w 4} \oplus k^{12}$. In the key recovery phase, one step is added before the key recovery of the 11-round attack:

- Individually guess $k_{l}^{f}(l=1,3, \ldots, 8)$ and check whether the equation $\triangle S_{l}^{12}=\left(P^{-1}\left(\triangle L^{13}\right)\right)_{l}$ holds. Next guess $k_{2}^{f}$, so $\left(L^{11}, L^{\prime 11}\right)$ can be computed.
The other steps are pretty similar to the 11 -round attack, and the complexity is $2^{248.7}$ encryptions that determined by the memory access for each pair and $2^{155}$ bytes' memory .


## 5 Impossible Differential Cryptanalysis of 15-round Camellia-256 without $\boldsymbol{F L} / \boldsymbol{F} L^{-1}$ layers and whitening

In this section, we give an improved impossible differential attack on Camellia-256 by using the 8 -round impossible differential path without $F L / F L^{-1}$ layer in Fig. 7, which was proposed in [18]. By adding 4 rounds on the top and 3 rounds on the bottom, we can attack 15 -round Camellia-256 without $F L / F L^{-1}$ layers and whitening, see Fig. 6.


Fig. 6. Impossible Differential Attack on 15-round Camellia-256 without $F L / F L^{-1}$ layers and whitening

The Attack. As mentioned in Section 2, there are four $8 \times 8$ S-boxes used in Camellia, for each S-box the average chance of a input/output differential pair to be counted in the differential table is $1 / 2$. This property can be used for early abort by checking whether the counted value of an a input/output differential pair in the corresponding differential table is non-zero.

In the following, we elaborate the attack procedure step by step to make it explicit.

## Data Collection.

1. For $2^{122}$ known plaintexts, encrypt them and insert them into a hash table indexed by the 7 -th and 8 -th bytes of $P^{-1}\left(\Delta R^{15}\right)$. Since by Property 1 , the right half of ciphertexts must have the form

$$
\Delta R^{15}=\Delta L^{14}=P\left(i, j_{2}, j_{3} \oplus i, j_{4} \oplus i, j_{5} \oplus i, j_{6} \oplus i, 0,0\right)
$$

by birthday attack, we can get $2^{243} \times 2^{-16}=2^{227}$ pairs that the 7 -th and 8 -th bytes of $P^{-1}\left(\Delta R^{15}\right)$ are 0.
2. Set up the differential tables for the 4 S -boxes of Camellia. For the remaining pairs, individually check whether $\Delta L_{l}^{14}$ and $\left(P^{-1}\left(\Delta R^{15}\right)\right)_{l}(l=1,3, \ldots, 8)$ is a possible input/output pair in the corresponding differential table. If not, discard the pair. We know that each check will discard about $1 / 2$ of the pairs, then number of the remaining pairs is about $2^{220}$.

Key Recovery. We give in Table 2 the corresponding positions of $k^{1}, k^{2}$ and $k^{15}$ in $K_{B}$, and the corresponding positions of $k^{3}, k^{14}, k_{2}^{4}$ and $k_{2}^{13}$ in $K_{R}$. We can see that, there are close relations among the subkeys, i.e., there are common bits in some of the subkeys, which can be used to reduced the complexity of the attack. We also illustrate the process below in Table 3 in the Appendix, in which the first column is the step, the second column denotes the key bits guessed in the step, the third column means the key bits known till the step, the forth column is the
subkey bytes used in the step and the last column denotes the values can be calculated in the step.

1. (a) Property 2 implies that $\Delta L^{1}=P\left(a, z_{2}, z_{3} \oplus a, z_{4} \oplus a, z_{5} \oplus a, z_{6} \oplus a, 0,0\right)$ is needed to get the input difference of the impossible differential, which deduce $\Delta S^{1}=P^{-1}\left(\Delta L^{1} \oplus \Delta R^{0}\right)$. So for the remaining pairs, we guess $k_{l}^{1}(l=7,8)\left(K_{B}: 49 \sim 64\right)$ one by one, and discard the pairs that do not satisfy $\Delta S_{l}^{1}=\left(P^{-1}\left(\Delta R^{0}\right)\right)_{l}$. The remaining pairs are about $2^{204}$.
(b) Guess bits $65 \sim 68$ of $K_{B}$, then $k_{1}^{15}\left(K_{B}: 61 \sim 68\right)$ is known, discard the pairs that do not satisfy $\Delta S_{1}^{15}=\left(P^{-1}\left(\Delta L^{15}\right)\right)_{1}$, then there are $2^{204} \times 2^{-7}=2^{197}$ pairs remaining.
Then for $l=5,6$, we individually guess $k_{l}^{15}\left(K_{B}: 93 \sim 108\right)$ and check whether $\Delta S_{l}^{15}=$ $\left(P^{-1}\left(\Delta L^{15}\right)\right)_{l}$. There are $2^{197} \times 2^{-7} \times 2^{-7}=2^{183}$ pairs satisfying.
(c) Now $k_{5}^{2}\left(K_{B}: 97 \sim 104\right)$ is known. We further guess $k_{1}^{1}, k_{2}^{1}$ and $k_{6}^{1}\left(K_{B}: 1 \sim 16,41 \sim\right.$ 48) to get the values of $\left(L_{5}^{1}, L_{5}^{\prime 1}\right)$. In the meanwhile, we keep the values of $\left(S_{1}^{1}, S_{1}^{\prime 1}\right)$, $\left(S_{2}^{1}, S_{2}^{\prime 1}\right),\left(S_{6}^{1}, S_{6}^{\prime 1}\right),\left(S_{7}^{1}, S_{7}^{\prime 1}\right)$ and $\left(S_{8}^{1}, S_{8}^{\prime 1}\right)$ under the subkey guess until the end of Step 4 (the memory is freed by then). Partially encrypt ( $L_{5}^{1}, L_{5}^{\prime 1}$ ) through round 2, and keep only the pairs such that $\Delta S_{5}^{2}=\left(P^{-1}\left(\Delta R^{1}\right)\right)_{5}$ holds. The number of remaining pairs is $2^{183} \times 2^{-8}=2^{175}$.
2. (a) Guess $k_{7}^{15}\left(K_{B}: 109 \sim 116\right)$, check whether $\Delta S_{7}^{15}=\left(P^{-1}\left(\Delta L^{15}\right)\right)_{7}$. This step will discard $2^{-7}$ of the pairs, and $2^{175-7}=2^{168}$ pairs will be kept. Furthermore, $k_{6}^{2}\left(K_{B}: 105 \sim 112\right)$ is known at this moment.
(b) Guess $k_{3}^{1}\left(K_{B}: 17 \sim 24\right)$ and $k_{5}^{1}\left(K_{B}: 33 \sim 40\right)$ simultaneously, we can calculate $\left(S_{3}^{1}, S_{3}^{\prime 1}\right)$ and $\left(S_{5}^{1}, S_{5}^{\prime 1}\right)$, followed by $\left(L_{6}^{1}, L_{6}^{\prime 1}\right)$ and $\Delta S_{6}^{2}$. Discard the pairs that don't satisfy $\Delta S_{6}^{2}=\left(P^{-1}\left(\Delta R^{1}\right)\right)_{6}$, the remaining pairs will be $2^{168-8}=2^{160}$.
3. (a) Guess $k_{4}^{15}\left(K_{B}: 85 \sim 92\right)$, calculate $\left(L_{4}^{1}, L_{4}^{\prime 1}\right)$ and detect whether $\Delta S_{4}^{15}=\left(P^{-1}\left(\Delta L^{15}\right)\right)_{4}$. The number of pairs that meet this condition will be $2^{159-7}=2^{152}$.
(b) Guess bits $81 \sim 84$ of $K_{B}$, then $k_{3}^{2}\left(K_{B}: 81 \sim 88\right)$ is known, discard the pairs that do not satisfy $\Delta S_{3}^{2}=\left(P^{-1}\left(\Delta R^{1}\right)\right)_{3}$, the number of pairs kept is about $2^{152-7}=2^{145}$.
(c) Since $k_{4}^{2}\left(K_{B}: 89 \sim 96\right)$ is known, we guess $k_{4}^{1}\left(K_{B}: 25 \sim 32\right)$, now the whole $k^{1}$ is known. Then we partially encrypt round $1 \sim 2$ and keep the pairs whose $\Delta S_{4}^{2}=\left(P^{-1}\left(\Delta R^{1}\right)\right)_{4}$. The remaining pairs is about $2^{145-8}=2^{137}$.
4. (a) Guess bits $117 \sim 120$ of $K_{B}$, then $k_{7}^{2}\left(K_{B}: 113 \sim 120\right)$ is known, check whether $\Delta S_{7}^{2}=$ $\left(P^{-1}\left(\Delta R^{1}\right)\right)_{7}$. This operation will discard $2^{-8}$ of the pairs and $2^{137-8}=2^{129}$ pairs will remain.
(b) Guess bits $121 \sim 124$ of $K_{B}$, then $k_{8}^{15}\left(K_{B}: 117 \sim 124\right)$ is known, detect whether $\Delta S_{8}^{15}=\left(P^{-1}\left(\Delta L^{15}\right)\right)_{8}$, if not, discard the pair.
(c) Then guess bits $125 \sim 128$ of $K_{B}$, we know $k_{8}^{2}\left(K_{B}: 121 \sim 128\right)$ now, detect whether $\Delta S_{8}^{2}=\left(P^{-1}\left(\Delta R^{1}\right)\right)_{8}$ is satisfied, if not, discard the pair. After this step, the number of remaining pairs will be $2^{129-7-8}=2^{114}$.
(d) For the remaining pairs, guess bits $69 \sim 72$ of $K_{B}$, then we can check whether $\Delta S_{1}^{2}=$ $\left(P^{-1}\left(\Delta R^{1}\right)\right)_{1}$ as we know $k_{1}^{2}\left(K_{B}: 65 \sim 72\right)$. The number of remaining pairs after discarding will be $2^{114-8}=2^{106}$.
(e) Guess bits $77 \sim 80$ of $K_{B}$, then $k_{3}^{15}\left(K_{B}: 77 \sim 84\right)$ is known. Discard the pairs that don't satisfy $\Delta S_{3}^{15}=\left(P^{-1}\left(\Delta L^{15}\right)\right)_{3}$. About $2^{106-7}=2^{99}$ pairs will be kept.
(f) Guess bits $73 \sim 76$ of $K_{B}$, note that the whole $K_{B}$ is known, so are $k^{2}$ and $k^{15}$. Now $L^{13}$ and $L^{\prime 13}$ can be calculated.
5. From Property 1 and Fig. 6 we know, if a pair follows the path in Fig. 6, it must satisfy $\Delta S_{l}^{14}=\left(P^{-1}\left(\Delta L^{14}\right)\right)_{1} \oplus\left(P^{-1}\left(\Delta L^{14}\right)\right)_{l}(l=3, \ldots, 6)$ and $\Delta S_{2}^{14}=\left(P^{-1}\left(\Delta L^{14}\right)\right)_{2}$. Therefore we do the following:
(a) We further guess $k_{2}^{14}\left(K_{R}: 5 \sim 12\right)$, partially decrypt round 15 and round 14 to discard the pairs which do not satisfy $\Delta S_{2}^{14}=\left(P^{-1}\left(\Delta L^{14}\right)\right)_{2}$. After this procedure, the number of remaining pairs is $2^{99-8}=2^{91}$.
(b) Individually guess $k_{l}^{14}(l=3, \ldots, 6)\left(k_{R}: 13 \sim 44\right)$ and keep the pairs which satisfy $\Delta S_{l}^{14}=\left(P^{-1}\left(\Delta L^{14}\right)\right)_{1} \oplus\left(P^{-1}\left(\Delta L^{14}\right)\right)_{l}$. There are $2^{91-8 \times 4}=2^{59}$ pairs being kept.
6. (a) Guess bits $45 \sim 47$ of $k_{R}$, now $k_{2}^{3}, k_{3}^{3}$, and $k_{4}^{3}\left(K_{R}: 24 \sim 47\right)$ are known. Detect if $\Delta S_{2}^{3}=\left(P^{-1}\left(\Delta R^{2}\right)\right)_{2}, \Delta S_{3}^{3}=\left(P^{-1}\left(\Delta R^{2}\right)\right)_{1} \oplus\left(P^{-1}\left(\Delta R^{2}\right)\right)_{3}$, and $\Delta S_{4}^{3}=\left(P^{-1}\left(\Delta R^{2}\right)\right)_{1} \oplus$ $\left(P^{-1}\left(\Delta R^{2}\right)\right)_{4}$. The number of remaining pairs is $2^{59-8 \times 3}=2^{35}$.
(b) Individually guess $k_{l}^{3}(l=5,6) \quad\left(k_{R}: 48 \sim 63\right)$ and keep the pairs that satisfy $\Delta S_{l}^{3}=$ $\left(P^{-1}\left(\Delta R^{2}\right)\right)_{1} \oplus\left(P^{-1}\left(\Delta R^{2}\right)\right)_{l}$. There are $2^{35-8 \times 2}=2^{19}$ pairs being kept.
7. Guess $k_{1}^{14}\left(K_{R}: 125 \sim 128,1 \sim 4\right)$ (now the whole $k^{14}$ is known) and $k_{2}^{13}\left(K_{R}: 69 \sim 76\right)$, keep the pairs that meet $\Delta S_{2}^{13}=\Delta L_{2}^{13}$. The number of remaining of pairs will be $2^{19-8}=2^{11}$.
8. Guess the rest 8 bits of $k^{3}\left(K_{R}: 64 \sim 68,77 \sim 79\right)$, now the whole $k^{3}\left(K_{R}: 16 \sim 79\right)$ are known. We further guess $k_{2}^{4}\left(K_{R}: 88 \sim 95\right)$ and check if there is a pair satisfy $\Delta S_{2}^{4}=\Delta L_{2}^{2}$. If there is a pair satisfy this, then discard the key guess and try another. Otherwise for every 219-bit key guess, exhaustively search the rest 37 bits of $K_{R}$ to calculate $K_{A}$, and use the relation of $K_{A}$ and $K_{L}$ to recover $K_{L}$.

The Complexity. In Step 1 of data collecting phase, encrypting $2^{122}$ plaintexts needs $2^{122}$ 15 -round encryptions. The computation of the 7 -th and 8 -th bytes of $P^{-1}\left(\Delta R^{16}\right)$ is less then $2 / 8$ one round encryption, so the complexity of computing the 7 -th and 8-th bytes of $P^{-1}\left(\Delta R^{16}\right)$ is at most $2^{122} \times \frac{1}{4} \times \frac{1}{15} \approx 2^{116.1} 15$-round encryptions. So the complexity of Step 1 is about $2^{122}+2^{116.1} \approx 2^{122}$ encryptions. The complexity of Step 2 in data collecting phase is at most $2 \times 2^{227} \times \frac{1}{8} \times \frac{1}{15} \approx 2^{221.1}$ encryptions and $2^{225}$ bytes to store the pairs.

Below we elaborate the complexity of each step in the key-recovery phase.

1. (a) The complexity for computing $\left(P^{-1}\left(\Delta R^{0}\right)\right)_{l}, \Delta S_{1}^{1}(l=7,8)$ and detecting whether they are equal is about $1 / 8$ one round encryption. So the complexity of this step is about $2 \times 2 \times 2^{8} \times 2^{220} \times \frac{1}{8} \times \frac{1}{15} \approx 2^{223.1}$ encryptions.
(b) Similarly, the time complexity of Step 1 (b) is about $2 \times 2^{20} \times 2^{204} \times \frac{1}{8} \times \frac{1}{15}+2 \times 2^{28} \times$ $2^{197} \times \frac{1}{8} \times \frac{1}{15}+2 \times 2^{36} \times 2^{190} \times \frac{1}{8} \times \frac{1}{15} \approx 2^{220.6}$.
(c) Partially encrypt round 1 and round 2 to check whether $\Delta S_{5}^{2}=P^{-1}\left(\Delta R^{1}\right)_{5}$ is about one round encryption. So the complexity is about $2 \times 2^{60} \times 2^{183} \times \frac{1}{15} \approx 2^{240.1}$ encryptions.
2. (a) Similar to Step 1 (a), this step needs about $2 \times 2^{68} \times 2^{175} \times \frac{1}{8} \times \frac{1}{15} \approx 2^{237.1}$ encryptions.
(b) Calculating $\left(L_{6}^{1}, L_{6}^{\prime 1}\right)$ needs about $2 / 8$ one round encryptions (knowing $\left(S_{2}^{1}, S_{2}^{\prime 1}\right),\left(S_{7}^{1}, S_{7}^{\prime 1}\right)$ and $\left(S_{8}^{1}, S_{8}^{\prime 1}\right)$ ). Therefore, the complexity of this step is about $2 \times 2^{84} \times 2^{168} \times \frac{3}{8} \approx 2^{251.6}$, equivalent to $2^{247.7} 15$-round encryptions.
3. The complexity of this step can be calculated as follows:
(a) $2 \times 2^{92} \times 2^{160} \times \frac{2}{8} \times \frac{1}{15} \approx 2^{247.1}$.
(b) $2 \times 2^{96} \times 2^{152} \times \frac{2}{8} \times \frac{1}{15} \approx 2^{243.1}$.
(c) $2 \times 2^{104} \times 2^{145} \times \frac{2}{8} \times \frac{1}{15} \approx 2^{244.1}$.
4. The complexity of this step can be computed in the following:
(a) $2 \times 2^{108} \times 2^{137} \times \frac{2}{8} \times \frac{1}{15} \approx 2^{240.1}$.
(b) $2 \times 2^{112} \times 2^{129} \times \frac{3}{8} \times \frac{1}{15} \approx 2^{237.7}$.
(c) $2 \times 2^{116} \times 2^{122} \times \frac{3}{8} \times \frac{1}{15} \approx 2^{234.7}$.
(d) $2 \times 2^{120} \times 2^{114} \times \frac{2}{8} \times \frac{1}{15} \approx 2^{229.1}$.
(e) $2 \times 2^{124} \times 2^{106} \times \frac{1}{15} \approx 2^{227.1}$.
(f) $2 \times 2^{128} \times 2^{99} \times \frac{1}{15} \approx 2^{224.1}$
5. (a) The complexity of this step is about $2 \times 2^{136} \times 2^{99} \approx 2^{236.1}$ one round encryptions, that is about $2^{232.1}$ encryptions.
(b) The complexity of the each operation in this step is about one round encryption, so the complexity of is about: $2 \times \sum_{i=0}^{3}\left(2^{144+8 \times i} \times 2^{91-8 \times i} \times \frac{1}{15}\right) \approx 2^{234.1}$.
6. (a) The complexity of this step is about $2 \times \frac{1}{15} \times 2^{171} \times\left(2^{59}+2^{51}+2^{43}\right) \approx 2^{227.1}$.
(b) The complexity of this step is about $2 \times \frac{1}{15} \times\left(2^{179} \times 2^{35}+2^{187} \times 2^{27}\right) \approx 2^{212.1}$.
7. This step requires $2 \times 2^{203} \times 2^{19} \times \frac{1}{15} \approx 2^{219.1}$ encryptions.
8. In step 8 , we expect $2^{219} \times\left(1-2^{-8}\right)^{2^{11}} \approx 2^{207.7}$ of the key guess remained. So about $2^{207.7+37}=2^{244.7}$ trail encryptions are request to recover the whole key. The complexity of this step is thus $2 \times 2^{219} \times\left[1+\left(1-2^{-8}\right)+\ldots+\left(1-2^{-8}\right)^{2^{11}}\right] \times \frac{1}{15}+2^{244.7} \approx 2^{244.7}$. As a result, the time complexity is dominated by Step 2(b) and Step 3(a), the total complexity is about $2^{247.7}+2^{247.1} \approx 2^{248.4} 15$-round encryptions.

## 6 Conclusion

In this paper, we present several 6-round impossible differential paths with $F L / F L^{-1}$ layers in the middle, which lead to impossible differential attacks on 11-round Camellia-192 and 12-round Camellia-256 with $F L / F L^{-1}$ layers and whitening. Then an impossible differential cryptanalysis of 15 -round Camellia- 256 without $F L / F L^{-1}$ layers and whitening is given by carefully using the subkey relation and a 8-round impossible differential without $F L / F L^{-1}$ layer proposed in [18]. A summary of the previous attacks and our analysis of Camellia is given in Table 1 .

Table 1. Summary of the attacks on Camellia

| Block Size | \#Rounds | $F L / F L^{-1}$ | Attack Type | Data | Time | Source |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Camellia-128 | 8 | $\times$ | Truncated DC | $2^{83.6} \mathrm{CP}$ | $2^{55.6}$ | 10 |
|  | 9 | $\sqrt{ }$ | Square Attack | $2^{48} \mathrm{CP}$ | $2^{122}$ | [11] |
|  | 9 | $\times$ | Collision Attack | $2^{113.6} \mathrm{CP}$ | $2^{121}$ | 19 |
|  | 9 | $\times$ | Square Attack | $2^{66} \mathrm{CP}$ | $2^{84.8}$ | [6] |
|  | 11 | $\times$ | Impossible DC | $2^{118} \mathrm{CP}$ | $2^{126} \mathrm{MA}$ | 12 |
|  | 12 | $\times$ | Impossible DC | $2^{116.3} \mathrm{CP}$ | $2^{116.6}$ | 14 |
| $\begin{gathered} \hline \text { Camellia-192 } \\ /-256 \end{gathered}$ | 10 | $\checkmark$ | Square Attack | $2^{48} \mathrm{CP}$ | $2^{210}$ | [1] |
|  | last 11 rounds | $\checkmark$ | Higher Order DC | $2^{93} \mathrm{CC}$ | $2^{255.6}$ | [7] |
|  | 11 | $\sqrt{ }$ | Impossible DC | $2^{121} \mathrm{CP}$ | $2^{184.8}$ | this paper |
|  | 12 | $\sqrt{ }$ | Impossible DC | $2^{121} \mathrm{CP}$ | $2^{248.7}$ | this paper |
|  | 12 |  | Impossible DC | $2^{120} \mathrm{CP}$ | $2^{181}$ | 18 |
|  | 12 | $\times$ | Linear Attack | $22^{119} \mathrm{KP}$ | $2^{247}$ | 16 |
|  | 12 | $\times$ | Square Attack | $2^{66} \mathrm{CP}$ | $2^{249.6}$ | [6] |
|  | 13 | $\times$ | Impossible DC | $2^{120} \mathrm{CP}$ | $2^{211.7}$ | 12 |
|  | 15 | $\times$ | Impossible DC | $2^{122} \mathrm{KP}$ | $2^{248.4}$ | this paper |

$\overline{\mathrm{KP}: ~ k n o w n ~ p l a i n t e x t ; ~ C P: ~ c h o s e n ~ p l a i n t e x t ; ~ C C: ~ c h o s e n ~ c i p h e r t e x t ; ~}$

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## A 8-Round Impossible Differential Path without $\boldsymbol{F L} / \boldsymbol{F} \boldsymbol{L}^{-1}$ Layer



Fig. 7. 8-round Impossible Differential Path without $F L / F L^{-1}$ layer

B The process of key recovery attack on 15 -round Camellia- 256 without $\boldsymbol{F L} / \boldsymbol{F} L^{-1}$ layers and whitening

Table 2. Corresponding bit positions of the subkeys in $K_{B}$ and $K_{R}$

| Subkey <br> bytes | Bit positions <br> in $K_{B}$ | Subkey <br> bytes | Bit positions <br> in $K_{B}$ | Subkey <br> bytes | Bit positions <br> in $K_{R}$ | Subkey <br> bytes | Bit positions <br> in $K_{R}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $k_{1}^{1}$ | $1 \sim 8$ | $k_{5}^{2}$ | $97 \sim 104$ | $k_{1}^{3}$ | $16 \sim 23$ | $k_{1}^{14}$ | $125 \sim 128,1 \sim 4$ |
| $k_{2}^{1}$ | $9 \sim 16$ | $k_{6}^{2}$ | $105 \sim 112$ | $k_{2}^{3}$ | $24 \sim 31$ | $k_{1}^{14}$ | $5 \sim 12$ |
| $k_{3}^{1}$ | $17 \sim 24$ | $k_{7}^{2}$ | $113 \sim 120$ | $k_{3}^{3}$ | $32 \sim 39$ | $k_{3}^{14}$ | $13 \sim 20$ |
| $k_{1}^{1}$ | $25 \sim 32$ | $k_{8}^{2}$ | $121 \sim 128$ | $k_{4}^{3}$ | $40 \sim 47$ | $k_{1}^{14}$ | $21 \sim 28$ |
| $k_{5}^{1}$ | $33 \sim 40$ | $k_{1}^{15}$ | $61 \sim 68$ | $k_{5}^{3}$ | $48 \sim 55$ | $k_{5}^{14}$ | $29 \sim 36$ |
| $k_{6}^{1}$ | $41 \sim 48$ | $k_{2}^{15}$ | $69 \sim 76$ | $k_{6}^{3}$ | $56 \sim 63$ | $k_{6}^{14}$ | $37 \sim 44$ |
| $k_{7}^{1}$ | $49 \sim 56$ | $k_{3}^{15}$ | $77 \sim 84$ | $k_{7}^{3}$ | $64 \sim 71$ | $k_{7}^{14}$ | $45 \sim 52$ |
| $k_{8}^{1}$ | $57 \sim 64$ | $k_{4}^{15}$ | $85 \sim 92$ | $k_{8}^{3}$ | $72 \sim 79$ | $k_{8}^{14}$ | $53 \sim 60$ |
| $k_{1}^{2}$ | $65 \sim 72$ | $k_{5}^{15}$ | $93 \sim 100$ | $k_{2}^{4}$ | $88 \sim 95$ | $k_{2}^{13}$ | $69 \sim 76$ |
| $k_{2}^{2}$ | $73 \sim 80$ | $k_{6}^{15}$ | $101 \sim 108$ |  |  |  |  |
| $k_{3}^{2}$ | $81 \sim 88$ | $k_{7}^{15}$ | $109 \sim 116$ |  |  |  |  |
| $k_{4}^{2}$ | $89 \sim 96$ | $k_{8}^{15}$ | $117 \sim 124$ |  |  |  |  |

Table 3. The process of key recovery in Section 5

| Step | Key bits guessed in this step | Key bits guessed until this step | Subkeys bytes used in this step | Intermediate values can be calculated |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | $K_{B}: 49 \sim 64$ | $K_{B}: 49 \sim 64$ | $k_{7}^{1}, k_{8}^{1}$ | $S_{7}^{1}, S_{8}^{1}, S_{7}^{\prime 1}, S_{8}^{\prime 1}$ |
| 1(b) | $\begin{gathered} K_{B}: 65 \sim 68, \\ 93 \sim 108 \end{gathered}$ | $\begin{gathered} K_{B}: 49 \sim 68, \\ 93 \sim 108 \\ \hline \end{gathered}$ | $k_{1}^{15}, k_{5}^{15}, k_{6}^{15}$ | $\begin{gathered} S_{1}^{15}, S_{5}^{15}, S_{6}^{15}, S_{1}^{115}, \\ S_{5}^{115}, S_{6}^{\prime 15} \\ \hline \end{gathered}$ |
| 1(c) | $\begin{gathered} K_{B}: 1 \sim 16, \\ 41 \sim 48 \end{gathered}$ | $\begin{array}{c\|} \hline K_{B}: 1 \sim 16, \\ 41 \sim 68,93 \sim 108 \\ \hline \end{array}$ | $k_{1}^{1}, k_{2}^{1}, k_{6}^{1}, k_{5}^{2}$ | $\begin{gathered} S_{1}^{1}, S_{1}^{\prime 1}, S_{2}^{1}, S_{2}^{\prime 1}, S_{6}^{1}, S_{6}^{\prime 1}, \\ L_{5}^{1}, L_{5}^{\prime 1}, S_{5}^{2}, S_{5}^{\prime 2} \end{gathered}$ |
| 2(a) | $K_{B}: 109 \sim 116$ | $\begin{array}{c\|} K_{B}: 1 \sim 16, \\ 41 \sim 68,93 \sim 116 \\ \hline \end{array}$ | $k_{7}^{15}$ | $S_{7}^{15}, S_{7}^{\prime 15}$ |
| 2(b) | $\begin{gathered} K_{B}: 17 \sim 24 \\ 33 \sim 40 \end{gathered}$ | $K_{B}: 1 \sim 24$ <br> $33 \sim 68,93 \sim 116$ | $k_{3}^{1}, k_{5}^{1}, k_{6}^{2}$ | $\begin{aligned} & S_{3}^{1}, S_{3}^{\prime 1}, S_{5}^{1}, S_{5}^{\prime 1}, \\ & L_{6}^{1}, L_{6}^{\prime 1}, S_{6}^{2}, S_{6}^{\prime 2} \end{aligned}$ |
| 3(a) | $K_{B}: 85 \sim 92$ | $\begin{array}{c\|} K_{B}: 1 \sim 24 \\ 33 \sim 68,85 \sim 116 \\ \hline \end{array}$ | $k_{4}^{15}$ | $S_{4}^{15}, S_{4}^{\prime 15}$ |
| 3(b) | $K_{B}: 81 \sim 84$ | $\begin{array}{c\|} \hline K_{B}: 1 \sim 24 \\ 33 \sim 68,81 \sim 116 \end{array}$ | $k_{3}^{2}$ | $S_{3}^{2}, S_{3}^{\prime 2}$ |
| 3(c) | $K_{B}: 25 \sim 32$ | $\begin{gathered} K_{B}: 1 \sim 68, \\ \quad 81 \sim 116 \end{gathered}$ | $k_{4}^{1}, k_{4}^{2}$ | $L^{1}, L^{\prime 1}, S_{4}^{2}, S_{4}^{\prime 2}$ |
| 4(a) | $K_{B}: 117 \sim 120$ | $\begin{gathered} \hline K_{B}: 1 \sim 68, \\ 81 \sim 120 \end{gathered}$ | $k_{7}^{2}$ | $S_{7}^{2}, S_{7}^{\prime 2}$ |
| 4(b) | $K_{B}: 121 \sim 124$ | $\begin{gathered} K_{B}: 1 \sim 68, \\ 81 \sim 124 \end{gathered}$ | $k_{8}^{15}$ | $S_{8}^{15}, S_{8}^{\prime 15}$ |
| 4(c) | $K_{B}: 125 \sim 128$ | $\begin{gathered} \hline K_{B}: 1 \sim 68, \\ 81 \sim 128 \end{gathered}$ | $k_{8}^{2}$ | $S_{8}^{2}, S_{8}^{\prime 2}$ |
| 4(d) | $K_{B}: 69 \sim 72$ | $\begin{gathered} K_{B}: 1 \sim 72, \\ 81 \sim 128 \end{gathered}$ | $k_{1}^{2}$ | $S_{1}^{2}, S_{1}^{\prime 2}$ |
| 4(e) | $K_{B}: 77 \sim 80$ | $\begin{gathered} K_{B}: 1 \sim 72, \\ 77 \sim 128 \end{gathered}$ | $k_{3}^{15}$ | $S_{3}^{15}, S_{3}^{115}$ |
| 4(f) | $K_{B}: 73 \sim 76$ | $K_{B}: 1 \sim 128$ | $k_{2}^{15}$ | $L^{13}, L^{113}$ |
| 5(a) | $K_{R}: 5 \sim 12$ | $\begin{gathered} K_{B}: 1 \sim 128 \\ K_{R}: 5 \sim 12 \end{gathered}$ | $k_{2}^{14}$ | $S_{2}^{14}, S_{2}^{\prime 14}$ |
| 5(b) | $K_{R}: 13 \sim 44$ | $\begin{gathered} K_{B}: 1 \sim 128 \\ K_{R}: 5 \sim 44 \end{gathered}$ | $k_{3}^{14}, k_{4}^{14}, k_{5}^{14}, k_{6}^{14}$ | $\begin{aligned} & S_{3}^{14}, S_{3}^{\prime 14}, S_{4}^{14}, S_{4}^{\prime 14}, \\ & S_{5}^{14}, S_{5}^{114}, S_{6}^{14}, S_{6}^{114} \end{aligned}$ |
| 6(a) | $K_{R}: 45 \sim 47$ | $\begin{gathered} K_{B}: 1 \sim 128 \\ K_{R}: 5 \sim 47 \end{gathered}$ | $k_{2}^{3}, k_{3}^{3}, k_{4}^{3}$ | $S_{2}^{3}, S_{2}^{\prime 3}, S_{3}^{3}, S_{3}^{\prime 3}, S_{4}^{3}, S_{4}^{\prime 3}$ |
| 6(b) | $K_{R}: 48 \sim 63$ | $\begin{gathered} K_{B}: 1 \sim 128 \\ K_{R}: 5 \sim 63 \end{gathered}$ | $k_{5}^{3}, k_{6}^{3}$ | $S_{5}^{3}, S_{5}^{\prime 3}, S_{6}^{3}, S_{6}^{\prime 3}$ |
| 7 | $\begin{gathered} K_{R}: 125 \sim 128, \\ \quad 1 \sim 4,69 \sim 76 \end{gathered}$ | $K_{B}: 1 \sim 128$ $K_{R}: 1 \sim 63$, $69 \sim 76,125 \sim 128$ | $k_{1}^{14}, k_{7}^{14}, k_{8}^{14}, k_{2}^{13}$ | $R^{13}, R^{113}, S_{2}^{13}, S_{2}^{\prime 13}$ |
| 8 | $\begin{array}{c\|} K_{R}: 64 \sim 68 \\ 77 \sim 79,88 \sim 95 \end{array}$ | $\begin{gathered} K_{R}: 1 \sim 79 \\ 88 \sim 95,125 \sim 128 \end{gathered}$ | $k_{1}^{3}, k_{7}^{3}, k_{8}^{3}, k_{2}^{4}$ | $S_{2}^{4}, S_{2}^{\prime \prime}$ |


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