

Stability of fragments and study of
participant-spectator matter at peak center-of-mass
energy

Sukhjit Kaur

House No. 465, Sector-1B, Nasrali, Mandi Gobindgarh-147301, Punjab, India

June 9, 2011

Electronic address: sukhjitk85@gmail.com

We simulate the central reactions of nearly symmetric, and asymmetric systems, for the energies at which the maximum production of IMFs occurs ($E_{c.m.}^{peak}$). This study is carried out by using hard EOS along with cugnon cross section and employing MSTB method for clusterization. We study the various properties of fragments. The stability of fragments is checked through persistence coefficient, gain term and binding energy. The information about the thermalization and stopping in heavy-ion collisions is obtained via relative momentum, anisotropy ratio, and rapidity distribution. We find that for a complete stopping of incoming nuclei very heavy systems are required. The mass dependence of

various quantities (such as average and maximum central density, collision dynamics as well as the time zone for hot and dense nuclear matter) is also presented. In all cases (i.e., average and maximum central density, collision dynamics as well as the time zone for hot and dense nuclear matter) a power law dependence is obtained.

1 Introduction

Heavy-ion collisions at intermediate energies offer an opportunity of producing nuclear systems under the extreme conditions of temperature and density. At high excitation energies, the colliding nuclei compress each other as well as heat the matter [1–3]. This leads to the destruction of initial correlations, as a result the matter becomes homogeneous and one can have global stopping. The global stopping is defined as the randomization of one-body momentum space or memory loss of the incoming momentum. The degree of stopping, however, may vary drastically with incident energies, mass of colliding nuclei and colliding geometry. The degree of stopping has also been linked with the thermalization (equilibrium) in heavy-ion collisions. More the initial memory of nucleons is lost, better it is stopped.

The fragmentation of colliding nuclei into several pieces of different sizes is a complex phenomenon. This may be due to the interplay of correlations and fluctuations emerging in a collision. Several studies, in literature, have been made to check the fragmentation pattern. Fragmentation pattern has been found to depend on the size of the colliding nuclei, incident energy as well as impact parameter [1, 4–6]. Dhawan *et al.* [7] studied the degree of stopping reached in intermediate energy heavy-ion collisions. They found

that degree of stopping decreases with increase in impact parameter as well as at very high energies. They suggested that the light charged particles (LCPs) ($2 \leq A \leq 4$), can be used as a barometer for studying the stopping in heavy-ion collisions. As lighter fragments mostly originate from midrapidity region whereas intermediate mass fragments (IMFs) originate from surface of colliding nuclei and can be viewed as remnants of the spectator matter. On the other hand, Sood and Puri [8] studied the thermalization achieved in heavy-ion collisions in terms of participant-spectator matter. They found that participant-spectator matter depends crucially on the collision dynamics as well as history of the nucleons and important changes in the momentum space occur due to the binary nucleon-nucleon collisions experienced during the high dense phase. The collisions push the colliding nucleons into midrapidity region responsible for the formation of participant matter. This ultimately leads to thermalization in heavy-ion collisions. Vermani *et al.* [8] used rapidity distribution of nucleons to characterize the stopping and thermalization of the nuclear matter. They found that nearly full stopping is achieved in heavier systems like $^{197}\text{Au}+^{197}\text{Au}$ whereas in lighter systems a larger fraction of particles is concentrated near target and projectile rapidities, resulting in a broad Gaussian shape. The lighter systems, therefore, exhibit larger transparency effect, i.e., less stopping. Puri *et al.* [9] studied the non-equilibrium effects and thermal properties of heavy-ion collisions. They found that the heavier masses are found to be equilibrated more than the lighter systems.

Recently, Sisan *et al.* [10] studied the emission of IMFs from central collisions of nearly symmetric systems using a 4π -array set up, where they found that the multiplicity of IMFs shows a rise and fall with increase in the beam energy. They observed that $E_{c.m.}^{max}$ (the energy at which the maximum production of IMFs occurs) increases linearly with the

system mass, whereas a power-law ($\propto A^\tau$) dependence was reported for peak multiplicity of IMFs with power factor $\tau = 0.7$. Though percolation calculations reported in that paper failed to explain the data, subsequent calculations using QMD model [11] successfully reproduced the data over entire mass. One is, therefore, interested to understand how nuclear dynamics behaves at this peak energy i.e. whether linear increase reported for the multiplicity of fragments remains valid for other observables or not. We here plan to investigate the degree of stopping reached and other related phenomena in heavy-ion reactions at peak center-of-mass energies. We also check system size dependence of average and maximum central density, collision dynamics as well as the time zone for hot and dense nuclear matter at peak center-of-mass energy.

This study is made within the framework of the quantum molecular dynamics model, which is described in detail in Refs. [1, 4, 11–18].

2 Results and Discussion

For the present study, we simulate the central reactions ($b = 0.0$ fm) of $^{20}\text{Ne}+^{20}\text{Ne}$, $^{40}\text{Ar}+^{45}\text{Sc}$, $^{58}\text{Ni}+^{58}\text{Ni}$, $^{86}\text{Kr}+^{93}\text{Nb}$, $^{129}\text{Xe}+^{118}\text{Sn}$, $^{86}\text{Kr}+^{197}\text{Au}$ and $^{197}\text{Au}+^{197}\text{Au}$ at the incident energies at which the maximal production of intermediate mass fragments (IMFs) occurs. These read approximately 24, 46, 69, 77, 96, 124, and 104 AMeV, respectively for the above mentioned systems [11]. Note that in lower energy region phenomena like fusion, fission and cluster decay are dominant [19]. Here we use hard (labeled as Hard) equation of state along with energy dependent Cugnon cross section (σ_{nn}^{free}) [15]. The reactions are followed till 200 fm/c. The phase-space is clusterized using minimum span-

ning tree method with binding energy check (MSTB). The MSTB method is an improved version of normal MST method [16]. Firstly, the simulated phase-space is analyzed with MST method and pre-clusters are sorted out. Each of the pre-clusters is then subjected to binding energy check [11, 16]:

$$\zeta_i = \frac{1}{N^f} \sum_{i=1}^{N^f} \left[\frac{(\mathbf{p}_i - \mathbf{P}_{N^f}^{c.m.})^2}{2m_i} + \frac{1}{2} \sum_{j \neq i}^{N^f} V_{ij}(\mathbf{r}_i, \mathbf{r}_j) \right] < E_{bind}. \quad (1)$$

We take $E_{bind} = -4.0$ MeV if $N^f \geq 3$ and $E_{bind} = 0.0$ otherwise. Here N^f is the number of nucleons in a fragment and $\mathbf{P}_{N^f}^{c.m.}$ is center-of-mass momentum of the fragment. This is known as Minimum Spanning Tree method with Binding energy check (MSTB) [11, 16]. Note that nucleons belong to a fragment if inequality (1) is satisfied. The fragments formed with the MSTB method are more reliable and stable at early stages of the reactions.

One of the important aspects in fragmentation is the stability of fragments as well as surrounding nucleons of a fragment. The change in the nucleon content of fragments between two successive time steps can be quantified with the help of persistence coefficient [17, 18].

Let the number of pairs of nucleons in cluster C at time t is $\chi_C(t) = 0.5 * N_C(N_C - 1)$. At the time Δt later, it is possible that some of the nucleons belonging to cluster C have left the cluster and are the part of another cluster or are set free or others may have entered the cluster. Now, let N_{C_D} be the number of nucleons that have been in the cluster C at time t and are at $t + \Delta t$ in cluster D. We define

$$\Phi_C(t + \Delta t) = \sum_D 0.5 * N_{C_D}(N_{C_D} - 1). \quad (2)$$

Here the sum runs over all fragments D present at time $t + \Delta t$.

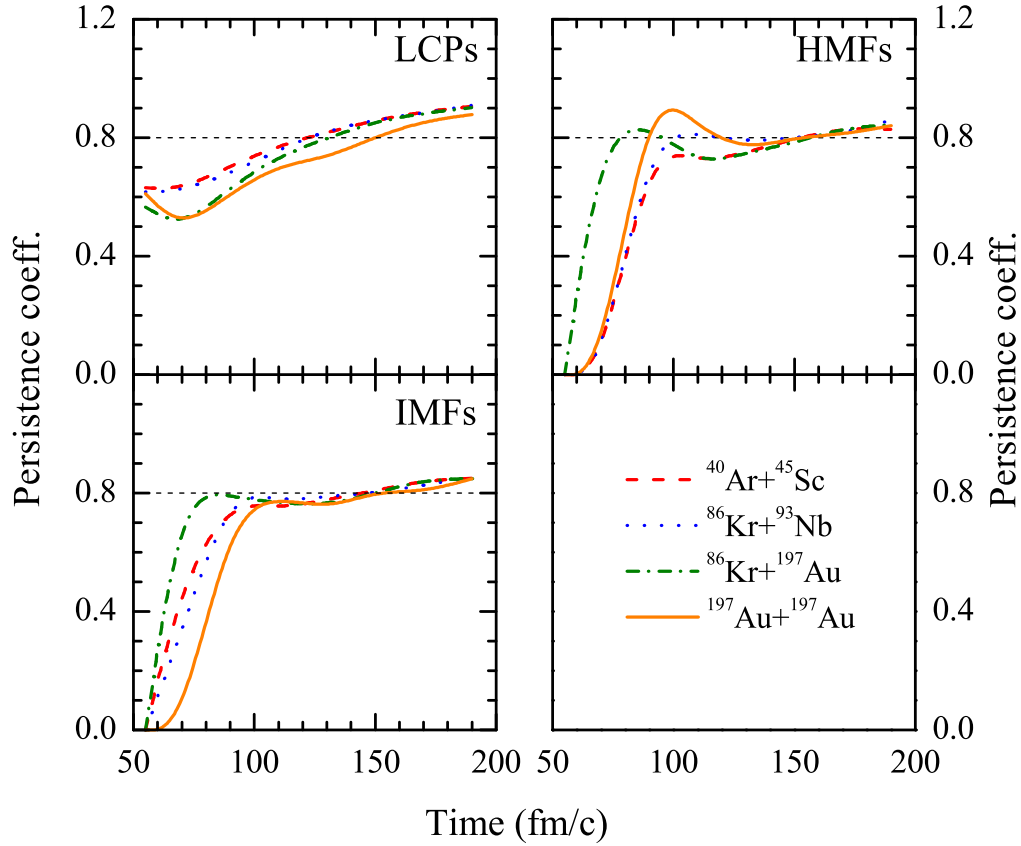


Figure 1: The persistence coefficient as a function of time for LCPs, HMFs, and IMFs. Dashed, dotted, dash-dotted and solid lines are for $^{40}\text{Ar}+^{45}\text{Sc}$, $^{86}\text{Kr}+^{93}\text{Nb}$, $^{86}\text{Kr}+^{197}\text{Au}$ and $^{197}\text{Au}+^{197}\text{Au}$, respectively.

The persistence coefficient of cluster C can be defined as [17, 18]:

$$P_C(t + \frac{\Delta t}{2}) = \Phi_C(t + \Delta t) / \chi_C(t). \quad (3)$$

The persistence coefficient averaged over an ensemble of fragments is defined as:

$$\langle P(t + \frac{\Delta t}{2}) \rangle = \frac{1}{N_{f_t}} \sum_C P_C(t + \frac{\Delta t}{2}), \quad (4)$$

where N_{f_t} is the number of fragments present at time t in a single simulation. The quantity

is then averaged over a large number of QMD simulations. The stability of a fragment between two consecutive time steps can be measured through persistence coefficient. If fragment does not emit a nucleon between two time steps, the persistence coefficient is one. On the other hand, if fragment disintegrates completely, the persistence coefficient will be zero. If we remove one nucleon from a fragment C , the persistence coefficient is $P_C(t + \Delta t/2) = (N_C - 2)/N_C$ i.e., 0.333 for $N_C = 3$ and 0.8 for $N_C = 10$. For example for mass 10, when one nucleon is emitted we have two entities at later time step consisting of free nucleon and fragment with mass 9. The $P_C(t + \Delta t/2)$ is the contribution from all such entities existing at later times. It, then, measures the tendency of the members of given cluster to remain together. In fig. 1, we display the persistence coefficient for various fragments i.e., light charged particles (LCPs) ($2 \leq A \leq 4$), intermediate mass fragments (IMFs) ($5 \leq A \leq 44$) as well as heavy mass fragments (HMFs) ($10 \leq A \leq 44$). The various lines have been defined in the caption. It is clear from fig. that the saturation value of persistence coefficient is slightly higher in case of LCPs as compared to heavier fragments. One can conclude that the final fragments are formed after 130 fm/c when this coefficient is 0.8. Before that time there is a strong exchange of nucleons between the fragments. The number of medium and intermediate size fragments increases because the largest fragment falls finally into this mass bracket. The persistent coefficient reaches its asymptotic value later due to the interaction between fragments as well as between fragments and free nucleons. Due to this interaction nucleons are sometimes absorbed or emitted from the fragments. This process changes the details but not the general structure of the fragmentation pattern.

The persistence coefficient tells about the stability of different fragments between two

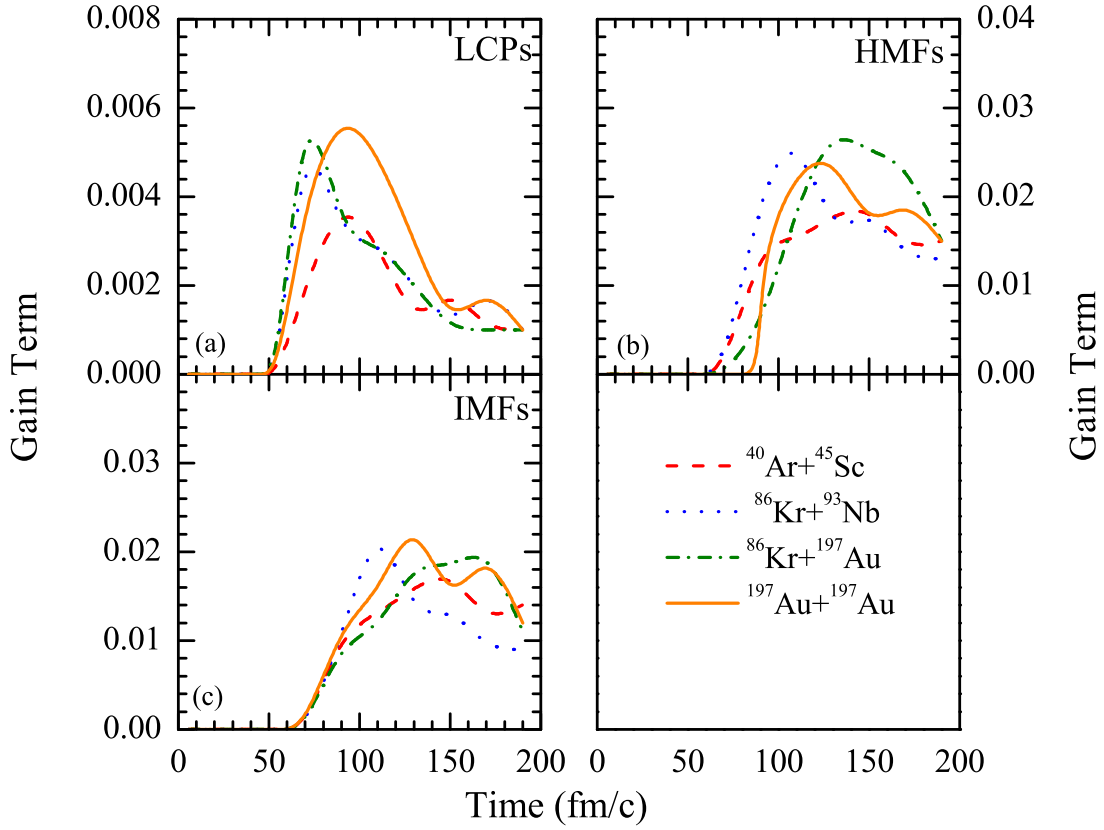


Figure 2: The Gain term as a function of time for LCPs, HMFs, and IMFs. Lines have same meaning as in fig. 1.

successive time steps. But it does not provide any information whether a fragment has swallowed some nucleons or not. To check this, we use a quantity called "Gain" [18]. The Gain represents the percentage of nucleons that a fragment has swallowed between two consecutive time steps. Let N_{α}^f be the number of nucleons belong to a fragment α at time t . Let $N_{\alpha\beta}^f$ be the number of nucleons which were in cluster α at time t and are in cluster β at time $t + \Delta t$. The Gain is defined as:

$$Gain(t + \Delta t/2) = \sum_{\alpha} \eta \times \frac{\sum_{\beta} (N_{\beta}^f - N_{\alpha\beta}^f)}{N_{\alpha}^f}; \quad (5)$$

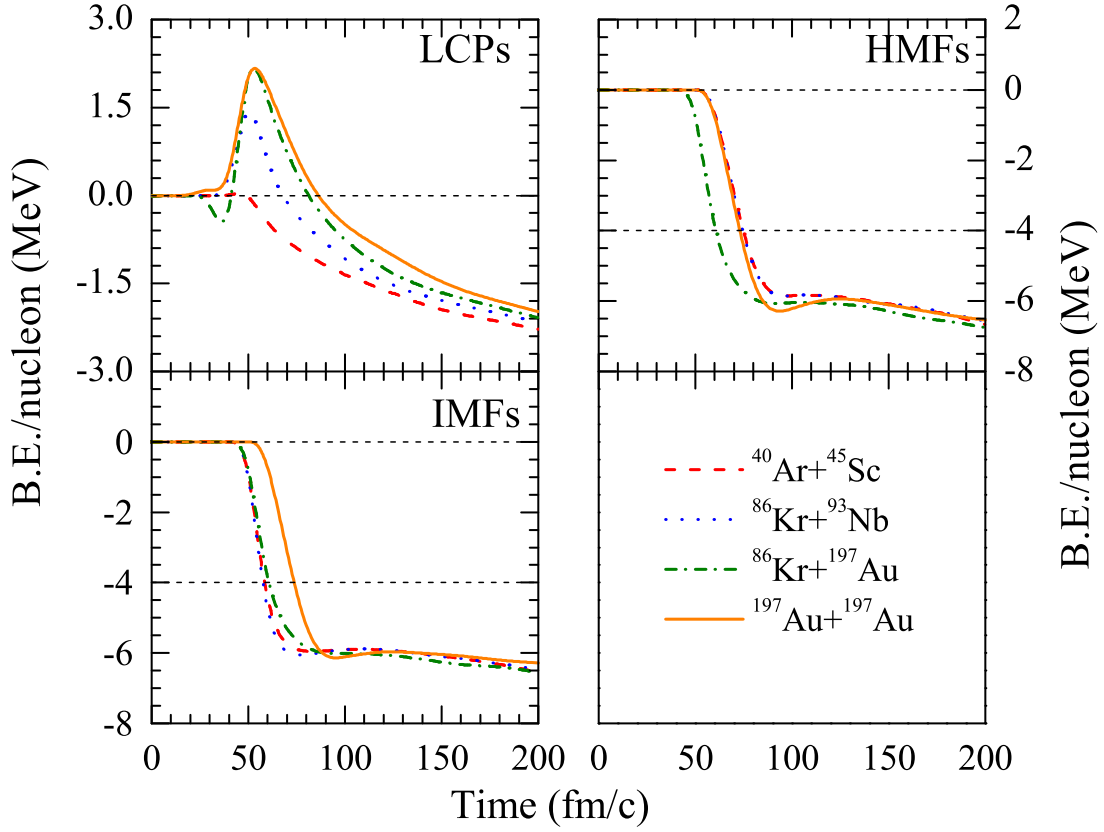


Figure 3: The time evolution of binding energy per nucleon for LCPs, HMFs, and IMFs. Lines have same meaning as in fig. 1.

$$\eta = 0.0, 0.5, \text{ and } 1.0 \text{ if } N_{\alpha\beta}^f < 0.5 N_{\beta}^f, N_{\alpha\beta}^f = 0.5 N_{\beta}^f \text{ and } N_{\alpha\beta}^f > 0.5 N_{\beta}^f, \text{ respectively.}$$

Naturally, a true Gain for a fragment α is only if its nucleons constitute at least half of the mass of new fragment β . The Gain term will tell us whether the interactions among fragments have ceased to exist or not.

In fig. 2, we display the gain term for LCPs, HMFs, and IMFs. As discussed earlier, the value of persistence coefficient is slightly higher in case of LCPs. Therefore, gain term will be smaller for LCPs as shown in fig. 2. As evident from fig., in case of heavier systems

the gain term has higher value because of the large nucleon-nucleon interactions.

To check the stability of fragments, we display in fig. 3, the binding energy per nucleon as a function of time for LCPs, HMFs and IMFs. We find that even at 200 fm/c, small fragments are still not cold and take very long time to cool down. Whereas the heavy fragments are properly bound having binding energy per nucleon around -5 to -7 MeV.

The quantities which are closely related to the degree of thermalization are relative momentum $\langle K_R \rangle$ and anisotropy ratio $\langle R_a \rangle$. The average relative momentum of two colliding fermi spheres is defined as [3, 9, 20]:

$$\langle K_R \rangle = \langle |P_P(\mathbf{r}, t) - P_T(\mathbf{r}, t)| / \hbar \rangle, \quad (6)$$

where

$$P_k(\mathbf{r}, t) = \frac{\sum_{j=1}^{A_k} P_j(t) \rho_j(\mathbf{r}, t)}{\rho_k(\mathbf{r}, t)}. \quad (7)$$

Here P_j and ρ_j are the momentum and density experienced by j^{th} particle and k stands for either target or projectile and \mathbf{r} refers to a space point in central sphere of 2 fm radius to which all calculations are made. The $\langle K_R \rangle$ is an indicator of local equilibrium because it depends on the local position r .

The second quantity is anisotropy ratio which is defined as [3, 7, 9, 20]:

$$\langle R_a \rangle = \frac{\sqrt{\langle p_x^2 \rangle} + \sqrt{\langle p_y^2 \rangle}}{2\sqrt{\langle p_z^2 \rangle}}. \quad (8)$$

The anisotropy ratio $\langle R_a \rangle$ is an indicator of global equilibrium of the system because it represents the equilibrium of the whole system and does not depend upon the local positions. The full global equilibrium averaged over large number of events will correspond to $\langle R_a \rangle = 1$.

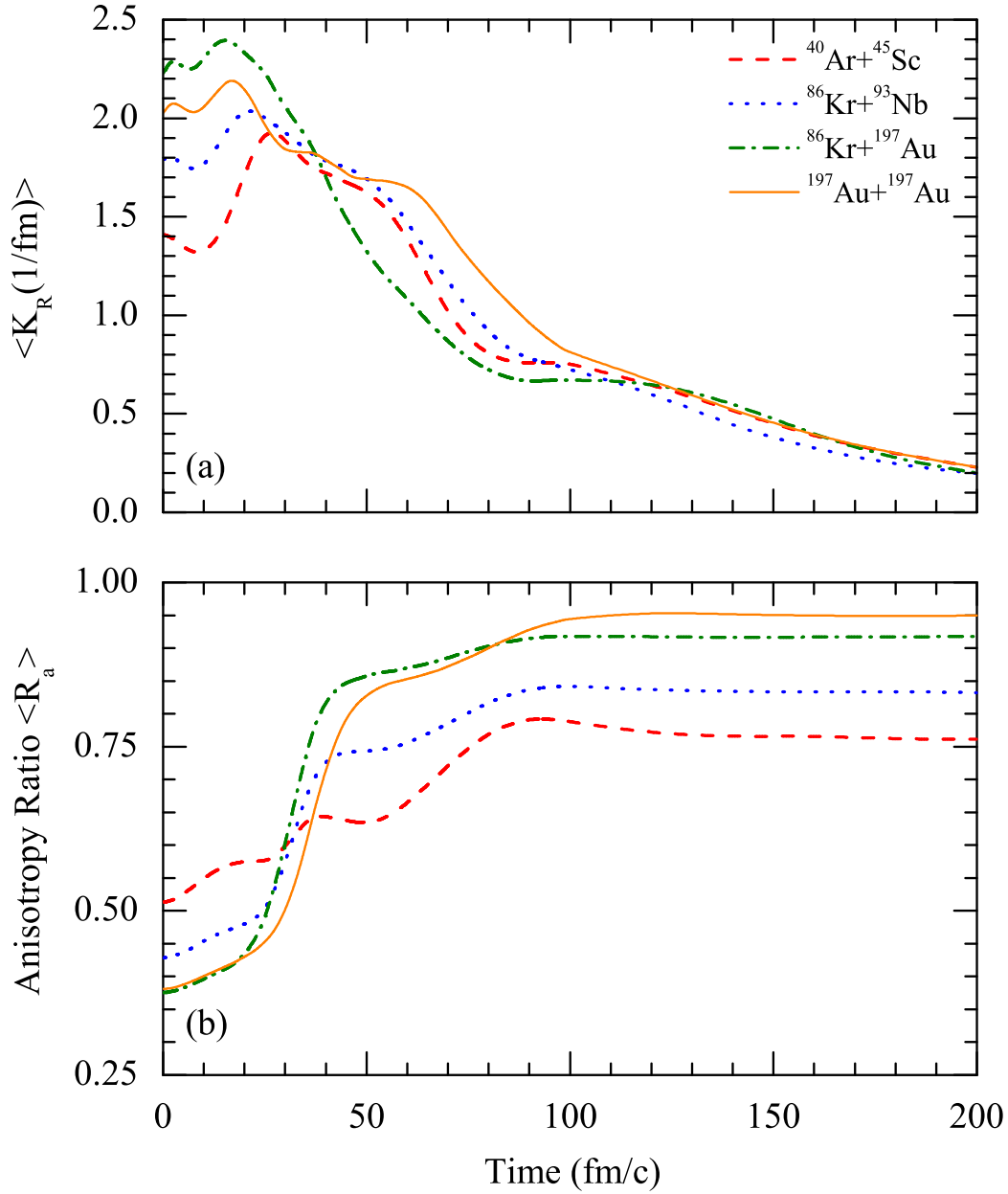


Figure 4: The time evolution of (a) relative momentum and (b) anisotropy ratio. Lines have same meaning as in fig. 1.

In figs. 4a and 4b, we display, respectively, $\langle K_R \rangle$ and $\langle R_a \rangle$ ratio as a function of time for different system masses. The initial value of relative momentum increases whereas of the anisotropy ratio decreases with mass of the system since $E_{c.m.}^{peak}$ increases with increase

in the system mass. It is interesting to see that the relative momentum is large at the start of the reaction, and finally at the end of the reaction, the value of $\langle K_R \rangle$ is nearly zero. This means that at the end of the reaction, the local equilibrium is nearly reached. However, the saturation time is nearly the same throughout the mass range. It is clear from the fig. 4b anisotropy ratio changes to a greater extent during the high density phase. Once the high density phase is over, no more changes occur in thermalization. Interestingly, the heavier nuclei are able to equilibrate more than the lighter nuclei. This is because of the fact that the number of collisions per nucleon for the $^{197}\text{Au}+^{197}\text{Au}$ reaction is larger than for the $^{40}\text{Ar}+^{45}\text{Sc}$ reaction.

The rapidity distribution is also assumed to give information about the degree of thermalization achieved in heavy-ion reactions. The rapidity distribution of i^{th} particle is defined as [7]:

$$Y(i) = \frac{1}{2} \ln \frac{\mathbf{E}(i) + \mathbf{p}_z(i)}{\mathbf{E}(i) - \mathbf{p}_z(i)}, \quad (9)$$

Here $\mathbf{E}(i)$ and $\mathbf{p}_z(i)$ are, respectively, the total energy and longitudinal momentum of i^{th} particle. Naturally, for a complete equilibrium a single Gaussian shape peak is expected. In fig. 5, we display the rapidity distribution of free-nucleons, LCPs, HMFs as well as IMFs. Rapidity distribution of all types of fragments indicate that heavier systems are better thermalized as compared to lighter ones. For lighter nuclei, we get relatively flat distribution. It is quite clear from the figs. 5(c) and 5(d) that very light nuclei ($^{40}\text{Ar}+^{45}\text{Sc}$) exhibit a peak at target/projectile rapidity indicating a non-equilibrium situation. Hence, for a complete stopping of incoming nuclei very heavy systems are required. For HMFs and IMFs, in case of $^{86}\text{Kr}+^{197}\text{Au}$, peak shifts towards left due to asymmetric reaction. The effect is more pronounced for different kinds of fragments as compared to free-nucleons.

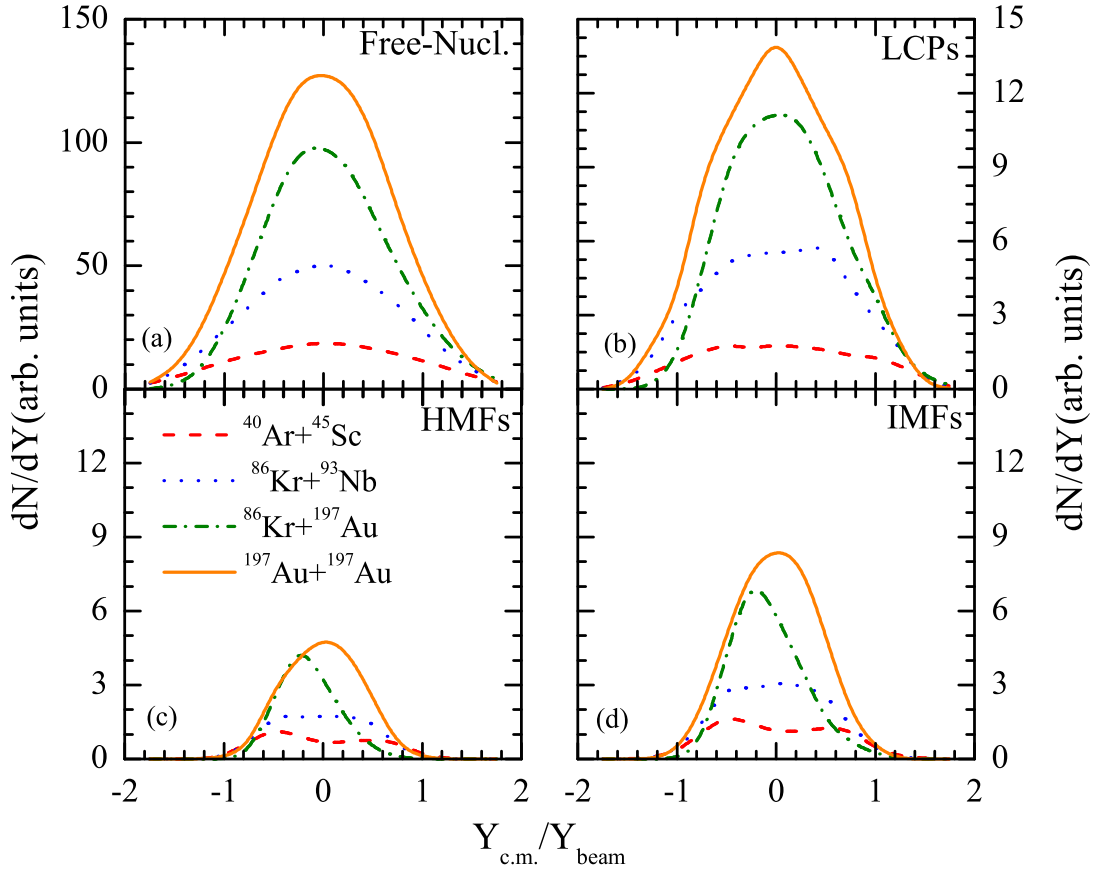


Figure 5: The rapidity distribution, dN/dY , as a function of reduced rapidity, $Y_{c.m.}/Y_{beam}$. Lines have same meaning as in fig. 1.

In fig. 6, we display the participant, spectator, and super-participant matter (obtained at 200 fm/c and defined in terms of nucleon-nucleon collisions) as a function of the total mass of the system. All nucleons that have experienced at least one collision are termed as participant matter. The remaining matter is counted as spectator matter. The nucleons having experienced more than one collision are termed as super-participant matter. As evident from the fig. 6, participant matter shows a nearly mass independent behavior ($\tau = 0.15 - 0.016$). The spectator and super-participant matter exhibit a power law dependence

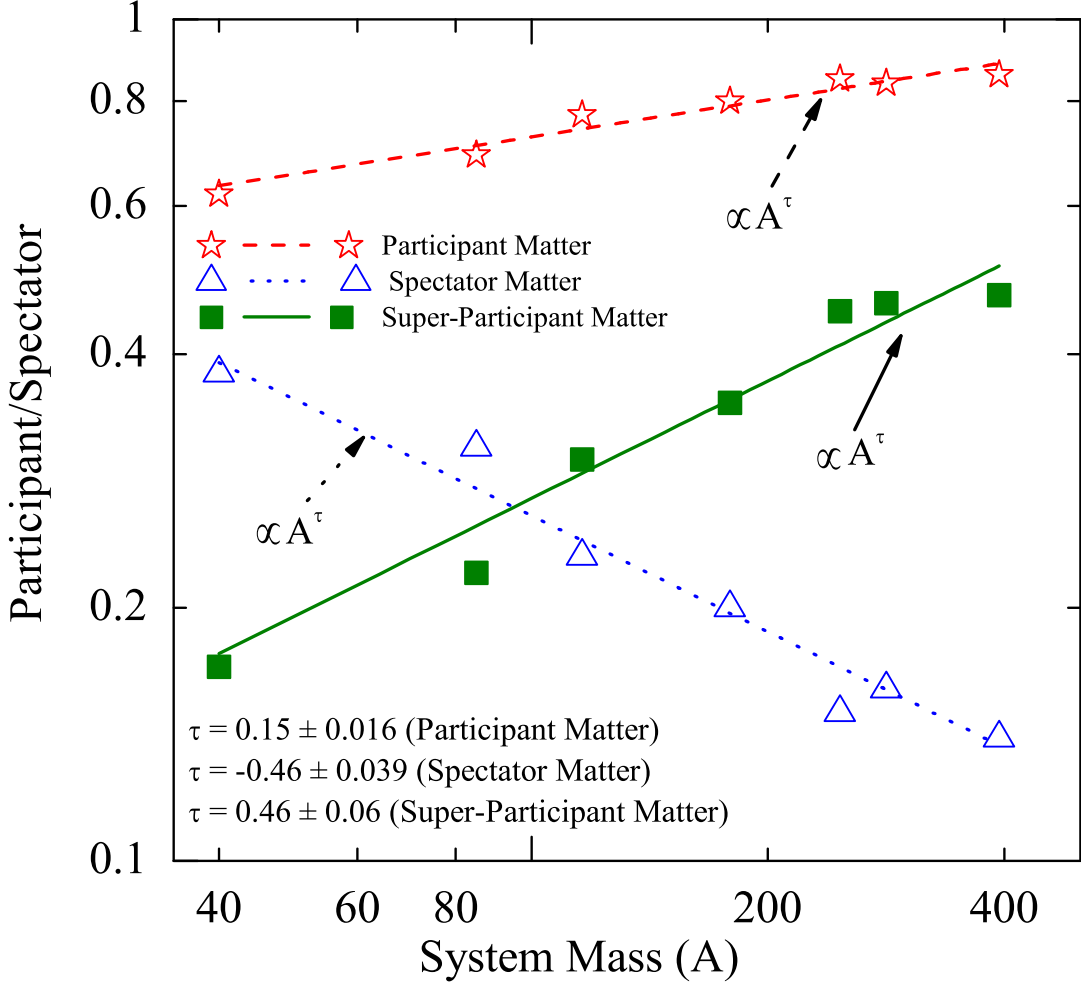


Figure 6: The participant, spectator, and super-participant matter (defined in terms of nucleon-nucleon collisions) as a function of composite mass of the system. The dashed, dotted, and solid lines represent the χ^2 fits with power law A^τ .

with $\tau = -0.46 \pm 0.039$ for spectator matter and $\tau = 0.46 \pm 0.06$ for super-participant matter.

In fig. 7, we display the system size dependence of the maximal value of average density $\langle \rho^{avg} \rangle$ (solid circles) and maximum density $\langle \rho^{max} \rangle$ (solid stars). Lines represent the power law fitting ($\propto A^\tau$). The maximal values of $\langle \rho^{avg} \rangle$ and $\langle \rho^{max} \rangle$ follow a power law ($\propto A^\tau$) with τ being 0.08 ± 0.02 for the average density $\langle \rho^{avg} \rangle$ and 0.034 ± 0.008 for maximum density $\langle \rho^{max} \rangle$ i.e., a slight increase in density occurs with increase in the size

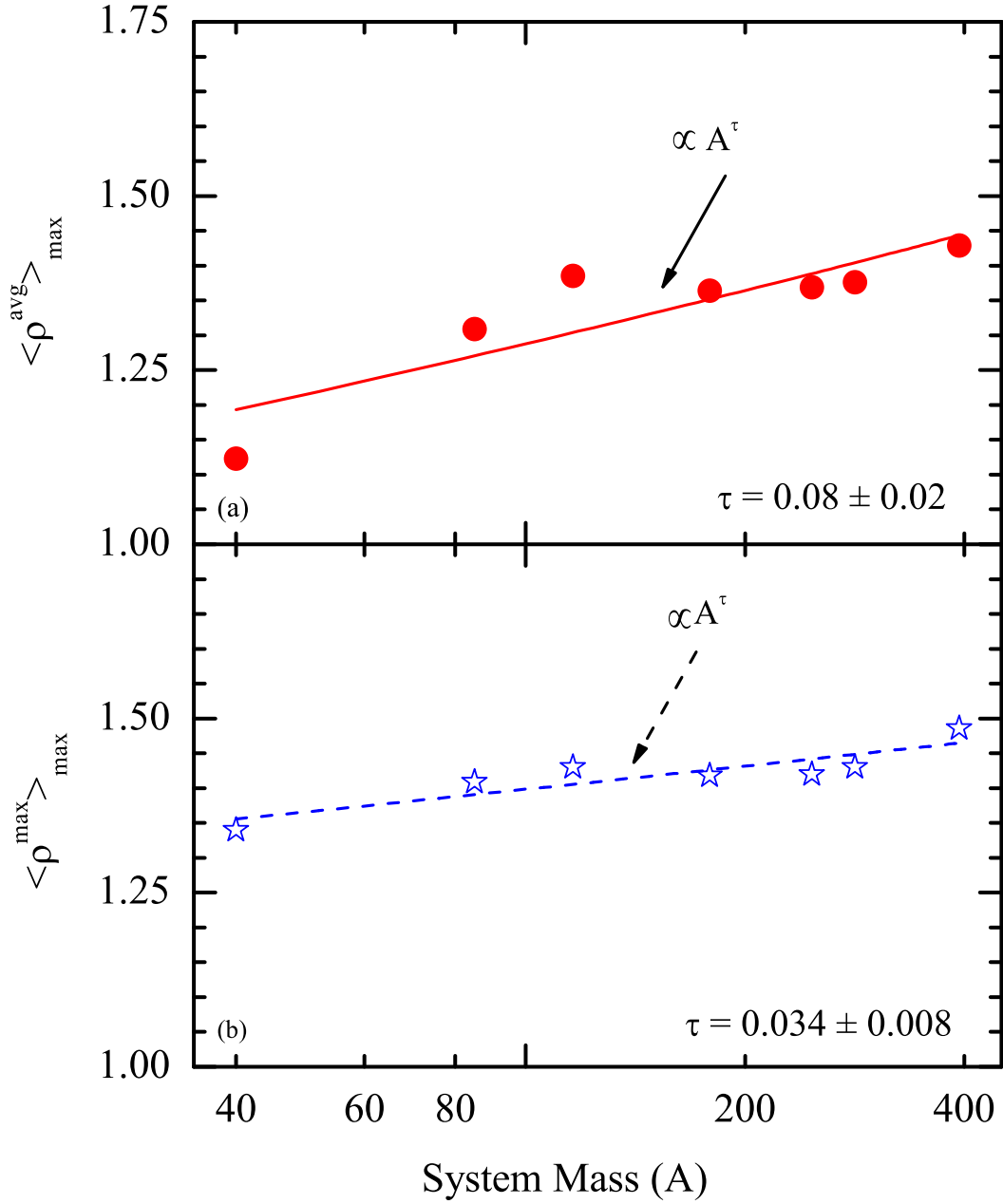


Figure 7: The maximal value of the average density $\langle \rho^{avg} \rangle_{max}$ (upper part) and maximum density $\langle \rho^{max} \rangle_{max}$ (lower part) as a function of the composite mass of the system. The solid lines are the fits to the calculated results using A^τ obtained with χ^2 minimization. The average is done over all space points on a sphere of 2 fm radius at center-of-mass.

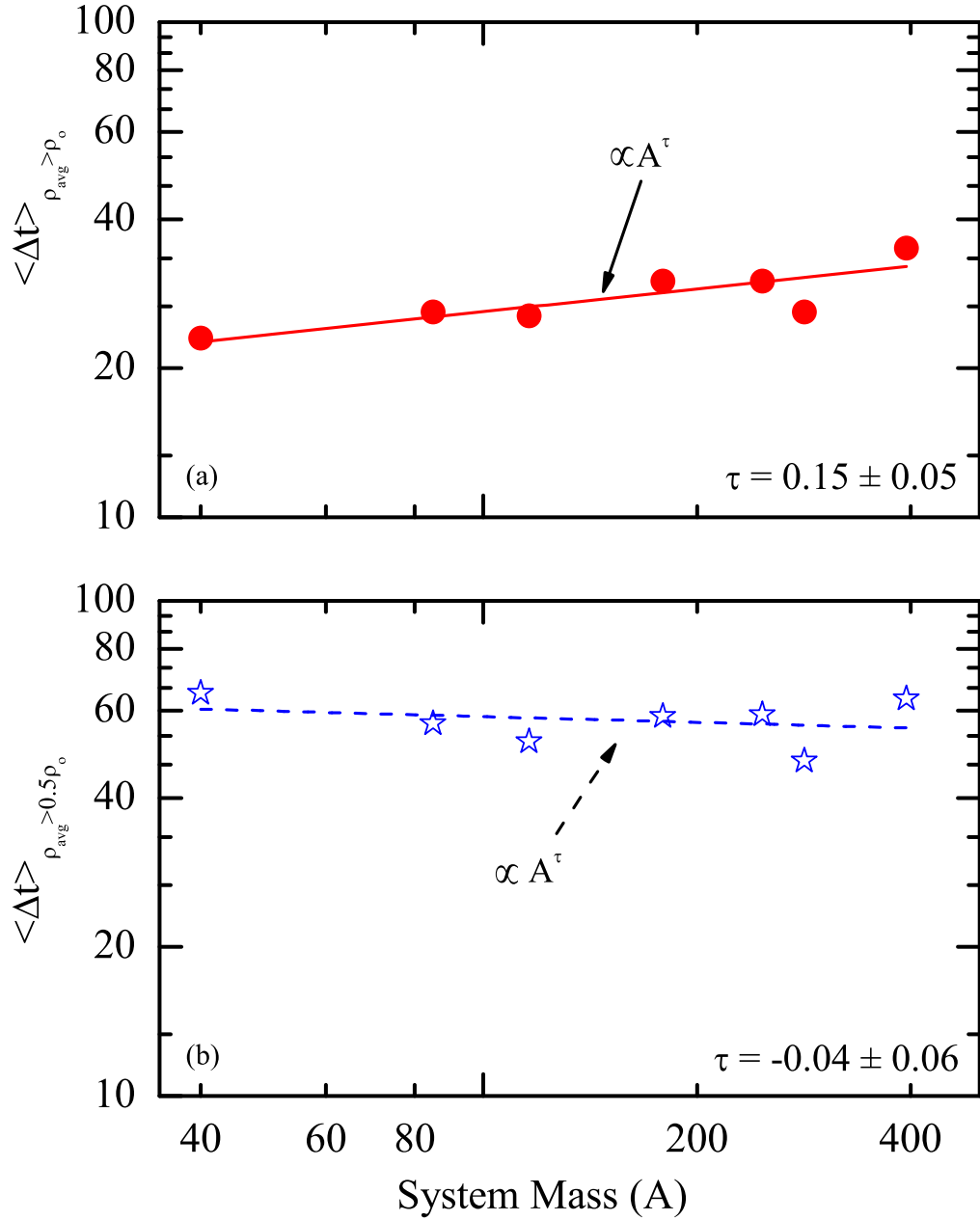


Figure 8: The time zone for $\rho_{avg} \geq \rho_o$ (upper part) and for $\rho_{max} \geq \rho_o$ (lower part) as a function of composite mass of the system. The solid lines represent the the χ^2 fits with power law A^τ .

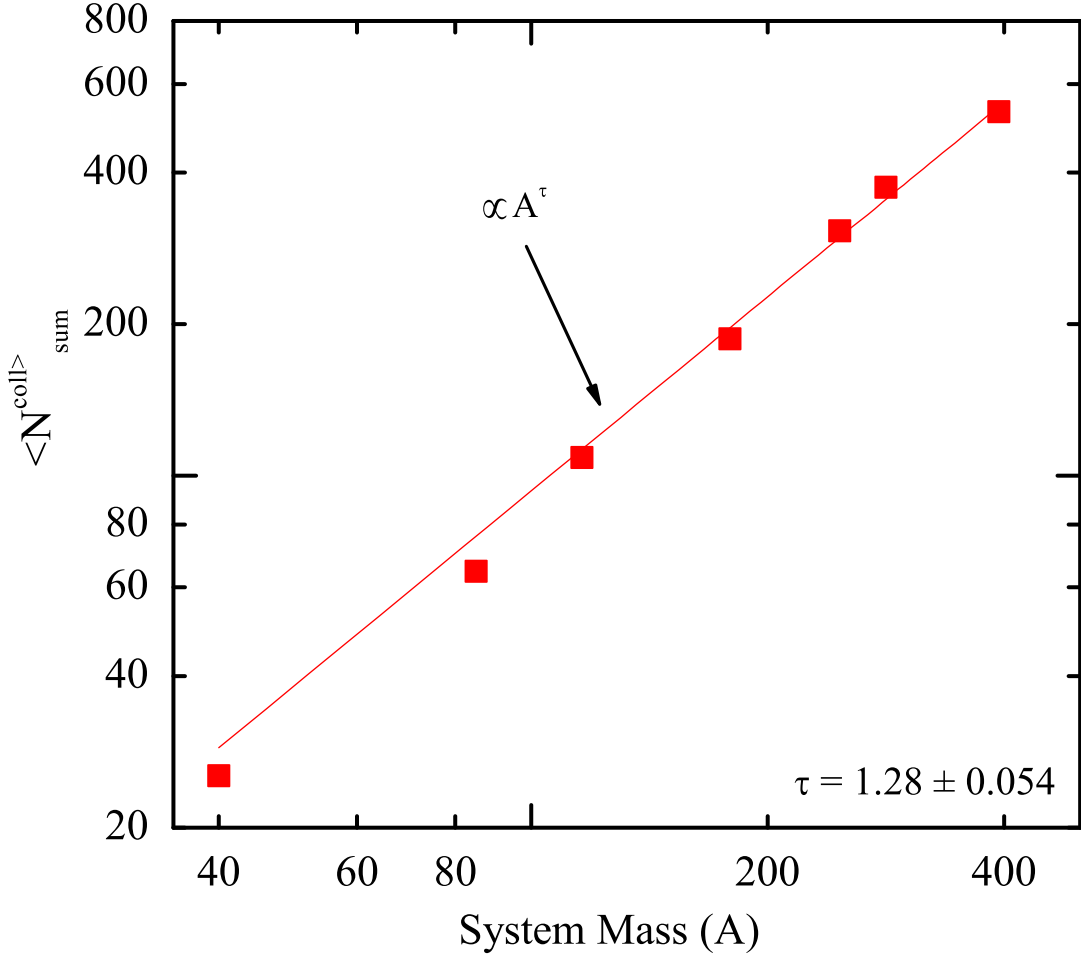


Figure 9: The total number of allowed collisions versus composite mass of the system.

The solid line represents the χ^2 fits with power law A^τ .

of the system. This is because, $E_{c.m.}^{peak}$ increases with the size of the system.

Apart from the maximal quantities, another interesting quantity is the dense zone at the peak energy. In fig. 8, we display the time interval for which $\rho_{avg} \geq \rho_o$ (solid circles) and $\rho_{avg} \geq \rho_o/2$ (open stars). Again both quantities follow a power law behavior with $\tau = 0.15 \pm 0.05$ and $\tau = -0.04 \pm 0.06$, respectively, for $\rho_{avg} \geq \rho_o$ and $\rho_{avg} \geq \rho_o/2$. This indicates that the time duration for which ρ_{avg} is greater than the normal nuclear matter density

increases with the mass of the system.

The system size dependence of the (allowed) nucleon-nucleon collisions (solid squares) is displayed in fig. 9. The results are displayed at 200 fm/c where the matter is diluted and well separated. The nucleon-nucleon collisions increase with the system size. This enhancement can be parametrized with a power law proportional to A^τ with $\tau = 1.28 \pm 0.054$. At fixed incident energy nucleon-nucleon collisions should scale as A . This has been tested by Sood and Puri [21]. Here power factor is greater than one since with increase in mass of the system $E_{c.m.}^{peak}$ also increases.

3 Summary

In the present study, we have simulated the central reactions of nearly symmetric, and asymmetric systems, for the energies at which the maximum production of IMFs occurs ($E_{c.m.}^{peak}$), using QMD model. This study is carried out by using hard EOS along with cugnon cross section and employing MSTB method for clusterization. We have studied the various properties of fragments. The stability of fragments is checked through persistence coefficient, gain term and binding energy. We observed that at 200 fm/c, small fragments are still not cold and they take very long time to cool down whereas the heavy fragments are properly bound. The information about the thermalization and stopping in heavy-ion collisions is obtained via relative momentum, anisotropy ratio, and rapidity distribution. We found that for a complete stopping of incoming nuclei very heavy systems are required. The mass dependence of various quantities (such as average and maximum central density, collision dynamics as well as the time zone for hot and dense nuclear matter) is also

presented. In all cases (i.e., average and maximum central density, collision dynamics as well as the time zone for hot and dense nuclear matter) a power law dependence is obtained.

4 Acknowledgements

This work has been supported by a grant from Department of Science and Technology (DST), Government of India, India.

References

- [1] P. B. Gossiaux and J. Aichelin, *Phys. Rev. C* **56**, 2109 (1997).
- [2] R. K. Puri *et al.*, *Nucl. Phys. A* **575**, 733 (1994); Y. K. Vermani and R. K. Puri, *Nucl. Phys. A* **847**, 243 (2010).
- [3] D. T. Khoa *et al.*, *Nucl. Phys. A* **548**, 102 (1992).
- [4] J. Aichelin, *Phys. Rep.* **202**, 233 (1991).
- [5] M. B. Tsang *et al.*, *Phys. Rev. Lett.* **71**, 1502 (1993).
- [6] C. Williams *et al.*, *Phys. Rev. C* **55**, R2132 (1997).
- [7] J. K. Dhawan *et al.*, *Phys. Rev. C* **74**, 057901 (2006).
- [8] A. D. Sood *et al.*, *Int. J. Mod. Phys. E* **15**, 899 (2006); Y. K. Vermani *et al.*, *Phys. Rev. C* **79**, 064613 (2009).

- [9] R. K. Puri *et al.*, J. Phys. G: Nucl. Part. Phys. **20**, 1817 (1994).
- [10] D. Sisan *et al.*, Phys. Rev. C **63**, 027602 (2001).
- [11] Y. K. Vermani *et al.*, J. Phys. G: Nucl. Part. Phys. **36**, 105103 (2009); S. Kaur and A. D. Sood, Phys. Rev. C **82**, 054611 (2010).
- [12] C. Hartnack *et al.*, Eur. Phys. J A **1**, 151 (1998); S. W. Huang *et al.*, Phys. Lett. B **298**, 41 (1993); Y. K. Vermani and R. K. Puri, Europhys. Lett. **85**, 62001 (2009); Y. K. Vermani *et al.*, J. Phys. G: Nucl. Part. Phys. **37**, 015105 (2010); S. Kumar *et al.*, Phys. Rev. C **78**, 064602 (2008).
- [13] S. Kumar *et al.*, Phys. Rev. C **58**, 3494 (1998); A. D. Sood *et al.*, Phys. Rev. C **79**, 064618 (2009); S. Kumar *et al.*, Phys. Rev. C **81**, 014611 (2010); *ibid* **81**, 014601 (2010); E. Lehmann *et al.*, Prog. Part. Nucl. Phys. **30**, 219 (1993); E. Lehmann *et al.*, Phys. Rev. C **51**, 2113 (1995).
- [14] J. Singh *et al.*, Phys. Rev. C **62**, 044617 (2000); G. Batko *et al.*, J. Phys. G: Nucl. Part. Phys. **20**, 461 (1994); S. W. Huang *et al.*, Prog. Part. Nucl. Phys. **30**, 105 (1993); C. Fuchs *et al.*, J. Phys. G: Nucl. Part. Phys. **22**, 131 (1996); A. D. Sood *et al.*, Phys. Lett. B **594**, 260 (2004); *ibid* Phys. Rev C **73**, 067602 (2006); S. Gautam *et al.*, J Phys. G: Nucl. Part. Phys. **37**, 085102 (2010).
- [15] S. Kumar *et al.*, Phys. Rev. C **58**, 1618 (1998); R. Chugh and R. K. Puri, Phys. Rev. C **82**, 014603 (2010).
- [16] S. Gautam and A. D. Sood, Phys. Rev. C **83**, 014603 (2011); *ibid.*, C **83**, 034606

- (2011); S. Goyal, Phys. Rev. C **83**, 047601 (2011); *ibid.*, Nucl. Phys. A **853**, 164 (2011).
- [17] R. K. Puri and J. Aichelin, J. Comp. Phys. **162**, 245 (2000); R. K. Puri *et al.*, Phys. Rev. C **54**, R28 (1996); P. B. Gossiaux *et al.*, Nucl. Phys. A **619**, 379 (1997).
- [18] R. K. Puri *et al.*, Pram. J. Phys. **59**, 19 (2002).
- [19] I. Dutt *et al.*, Phys. Rev. C **81**, 047601 (2010); *ibid* **81**, 044615 (2010); *ibid* **81**, 064609 (2010); *ibid* **81**, 064608 (2010); R. Arora *et al.*, Eur. Phys. J A **8**, 103 (2000); R. K. Puri *et al.*, Phys. Rev. C **43**, 315 (1991); *ibid* **45**, 1837 (1992); *ibid* J. Phys. G: Nucl.Part Phys. **18**, 903 (1992); *ibid* Eur. Phys. J A **3**, 277 (1998); *ibid* Eur. Phys. J A **23**, 429 (2005).
- [20] D. T. Khoa *et al.*, Nucl. Phys. A **529**, 363 (1991).
- [21] A. D. Sood *et al.*, Phys. Rev. C **70**, 034611 (2004).