

Multi Objective Multireservoir Optimization in Fuzzy Environment for River Sub Basin Development and Management

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Abstract

In this paper, a multi objective, multireservoir operation model is proposed using Genetic algorithm (GA) under fuzzy environment. A monthly Multi Objective Genetic Algorithm Fuzzy Optimization (MOGAFU-OPT) model for the present study is developed in 'C' Language. The GA parameters i.e. population size, number of generations, crossover probability, and mutation probability are decided based on optimized values of fitness function. The GA operators adopted are stochastic remainder selection, one point crossover and binary mutation. Initially the model is run for maximization of irrigation releases. Then the model is run for maximization of hydropower production. These objectives are fuzzified by assuming a linear membership function. These fuzzified objectives are simultaneously maximized by defining level of satisfaction (λ) and then maximizing it. This approach is applied to a multireservoir system in Godavari river sub basin in Maharashtra State, India. Problem is formulated with 4 reservoirs and a barrage. The optimal operation policy for maximization of irrigation releases, maximization of hydropower production and maximization of level of satisfaction is presented for existing demand in command area. This optimal operation policy so determined is compared with the actual average operation policy for Jayakwadi Stage-I reservoir.

Keywords: Optimization, Multi Objective Analysis, Multireservoir, Genetic Algorithms, Fuzzy Logic, Reservoir Operation

1. Introduction

In river basin studies, reservoir systems have their unique aspects and a variety of mechanisms are used in defining their operating rules [1]. Most of the water resources optimization problems involve conflicting objectives. The operation of a multi-purpose, multireservoir system consists of conflicting goals and requirements and consequently, several practical operating scenarios may exist. However, there are no standard operating rules, which are applicable to all situations. The successful management and operation of any reservoir system, therefore, lies in the ability to select the appropriate operating policy from amongst the available set of policies. Yeh [2] reviewed reservoir management and operation models. Optimal coordination of the many facets of reservoir systems requires the assistance of computer modeling

tools to provide information for rational management and operational decisions. Labadie [3] has reviewed state-of-the-art in optimization of multi reservoir systems.

Genetic algorithms are search algorithms based on the mechanism of natural selection and natural genetics. It is originated in mid 1970s [4,5] and has developed into an effective optimization approach. Oliveira and Loucks [6] have presented operating rules for multireservoir systems by using genetic search algorithms. Using simulation they have evaluated each policy to compute performance index for a given flow series. Wardlaw and Sharif [7] have presented several alternative formulations of a genetic algorithm for reservoir system. Multireservoir systems optimization has been studied by Sharif and Wardlaw [8]. A genetic algorithm approach has been presented by considering the existing development situation in the basin and two future water resource development

scenarios. Chang and Yang [9] have presented optimizing the rule curves for multi-reservoir operations using a genetic algorithm and HEC-5. Srinivasa Raju and Nagesh Kumar [10] have discussed application of genetic algorithms for irrigation planning. GA was used to determine optimal cropping pattern for maximizing benefits for an irrigation project. Juran Ali Ahmed and Arup kumar Sarma [11] have demonstrated genetic algorithm model for finding the optimal operating policy of a multipurpose reservoir. Multireservoir operation planning using hybrid GA and linear programming have been presented by Reis *et al.* [12]. They have proposed a new approach using GA and LP to determine operational decisions for reservoirs of a hydro system throughout a planning period, with the possibility of considering a variety of equally likely hydrologic sequences representing inflows. Jothiprakash and Ganeshan Shanthi [13] have developed GA model and applied to Pechiparai reservoir in Tamil Nadu, India to derive the optimal operational strategies. The fundamental guidelines for GA to optimal reservoir dispatching have been presented by Chang Jian-Xia *et al.* [14]. They have concluded that with three basic operators selection, crossover and mutation GA could search the optimum solution or near-optimal solution to a complex water resources problem. They have also considered alternative formulation schemes of GA. Reis *et al.* [15] have demonstrated a hybrid method using GA and linear programming to determine operational decisions for a reservoir system over the optimization period. A multi-objective Evolutionary Algorithm (MOGA) to derive a set of optimal operation policies for a multipurpose reservoir system have been presented by Janga Reddy and Nagesh Kumar [16]. One of the main goals in multiobjective optimization was to find a set of well distributed optimal solutions along the pareto front.

Anand Raj [17] has presented multicriteria methods in river basin planning. ELECTRE-I and ELECTRE-II techniques were applied for water resources planning to Krishna river basin, India. Anand Raj and Nagesh kumar [18] have presented ranking of river basin alternatives using ELECTRE. Anand Raj and Nagesh kumar [19] have presented planning for sustainable development of a river basin using fuzzy logic. Simonovic [20] discussed tools for water management. He discussed the complexity of water resources domain and the complexity of the modeling tools in an environment characterized by continuous rapid technological development. Bender and Simonovic [21] have presented a fuzzy compromise approach to water resource systems planning under uncertainty. Panigrahi and Mujumdar [22] have developed fuzzy rule based model for the operation of a single purpose reservoir. The steps involved in the development of the model include construction of membership functions for the inflow, storage, demand and the release, formulation of fuzzy rules, implication and defuzzification. They

have applied this methodology to the Malaprabha irrigation reservoir in Karnataka, India. Nagesh Kumar *et al.* [23] have presented optimal reservoir operation using fuzzy approach. Comparison of fuzzy and nonfuzzy optimal reservoir operating policies have presented by Tilmant *et al.* [24]. Srinivasa Raju and Duckstein [25] have presented multiobjective fuzzy linear programming for sustainable irrigation planning. This MOFLP model have been formulated for the evaluation of management strategy for the case study of Jayakwadi irrigation project, Maharashtra State, India. Regulwar and Anand Raj [26] have presented development of 3-D optimal surface for obtaining operation policies of a multireservoir in fuzzy environment using genetic algorithm.

With respect to the literature review, it can be said that multiobjective multireservoir optimization gives better operating policies for reservoirs under fuzzy environment. Therefore this work is undertaken for presenting operating policies for a case study to utilize the water resource optimally and also to present maximized level of satisfaction and corresponding operating policy. Also the entire range of optimal operation policies, for different levels of satisfaction i.e., λ (ranging from 0 to 1), are determined.

2. System Description

The multireservoir system in Godavari river sub basin taken for present study consists of Jayakwadi project Stage-I across river Godavari, Jayakwadi project Stage-II across river Sindaphana, Yeldari project and Siddeshwar project across river Purna, and Vishnupuri barrage across river Godavari in Maharashtra state, India. The salient features of reservoirs are presented in Table 1. The schematic representation of the physical system is shown in Figure 1. The irrigation demand and inflow is presented in Table 2.

3. Model Development

The objective of the study is to develop optimal operation policies for a multireservoir in a river sub basin. For this a monthly Multi Objective Genetic Algorithm Fuzzy Optimization (MOGAFUOPT) model is developed. The two objectives considered in this study are:

1. Maximization of irrigation releases (i.e., IR)
2. Maximization of hydro-power production (i.e., HP)

$$\text{Max } Z = \sum_i \sum_t (\text{IR})_{it} \quad \forall i=1,2,3,4 \quad (1)$$

$$\text{Max } Z = \sum_i \sum_t (\text{HP})_{it} \quad \forall t=1,2,3,\dots,12 \quad (2)$$

Where i is number of reservoirs and t is number of time steps. In the problem formulation, four reservoirs are

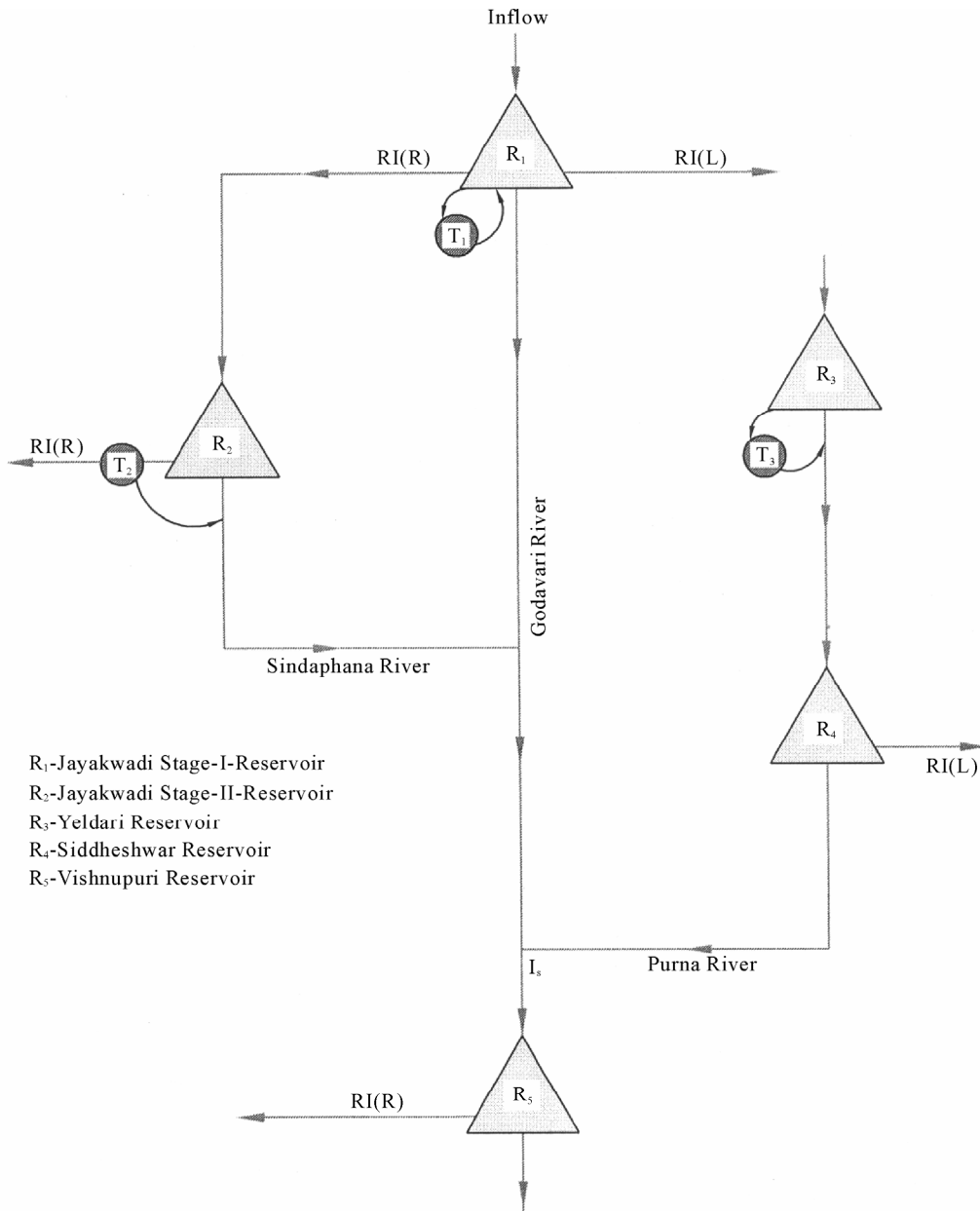


Figure 1. Schematic representation of the physical system.

Table 1. Salient features of reservoirs.

Sr. No.	Salient Features	Reservoirs				
		Jayakwadi Stage-I (R_1)	Jayakwadi Stage-II (R_2)	Yeldari (R_3)	Siddheshwar (R_4)	Vishnupuri (R_5)
1	River	Godavari	Sindaphana	Purna	Purna	Godavari
2	State/Country	Maharashtra State, India	Maharashtra State, India	Maharashtra State, India	Maharashtra State, India	Maharashtra State, India
3	Catchment Area (km ²)	21750	3840	7330	7770	13870
4	Gross Storage (Mm ³)	2909	453.64	934.44	250.85	83.85
5	Live Storage (Mm ³)	2171	311.30	809.77	80.96	81.67
6	Installed Capacity for hydro-power generation (MW)	12.0 (Pumped storage plant)	2.25 (Canal power house)	15.0	--	--
7	Irrigable command area (km ²)	1416.40	938.85	--	615.60	337.24

Table 2. Maximum irrigation demand and inflow in reservoirs in Mm³.

Month	Jayakwadi Stage-I (R ₁)		Jayakwadi Stage-II (R ₂)		Yeldari (R ₃)		Siddheshwar (R ₄)		Vishnupuri (R ₅)	
	Irrigation Demand	Inflow	Irrigation Demand	Inflow	Irrigation Demand	Inflow	Irrigation Demand	Inflow	Irrigation Demand	Inflow
Jun	18.55	148.76	7.12	20.98	0	72.83	33.10	7.71	35.91	16.42
Jul	26.70	408.25	20.83	43.46	0	141.09	35.23	2.21	22.97	35.96
Aug	25.43	610.66	37.64	96.88	0	200.36	35.23	11.97	31.69	107.32
Sep	85.79	600.0	46.02	144.17	0	160.77	93.46	9.18	31.49	246.07
Oct	267.86	287.75	132.01	75.52	0	123.10	77.60	1.29	31.95	79.00
Nov	228.74	196.46	127.05	10.24	0	49.48	74.68	0.57	22.68	9.91
Dec	210.88	125.53	89.43	4.27	0	35.58	65.14	0.89	35.09	7.93
Jan	230.34	37.65	100.68	0.37	0	32.18	65.14	1.00	38.46	1.13
Feb	85.23	21.46	30.02	0.37	0	24.23	35.50	0.39	23.65	0.00
Mar	70.06	19.56	28.98	0.16	0	23.54	37.40	1.00	14.50	0.00
Apr	85.49	25.50	35.58	0.12	0	13.15	30.50	0.40	19.06	0.00
May	58.20	46.58	25.88	0.06	0	13.86	22.30	0.40	28.07	0.00
Total	1393.2	2528.17	681.24	396.60	0	890.17	605.2	37.01	335.5	503.74

taken for optimization. The fifth reservoir is considered as downstream control and is incorporated as a constraint in the model. These objectives are subjected to the following constraints:

3.1. Turbine Release Constraints

The releases into turbines for power production, should be less than or equal to the flow through turbine capacities for all the months. Also, power production in each month should be greater than or equal to the firm power. These constraints can be written as:

$$HPR(i, t) \leq TCR(i) \quad \forall \quad i = 1, 2, 3, 4 \quad (3)$$

$$HPR(i, t) \geq FPR(i) \quad \forall \quad t = 1, 2, 3, \dots, 12 \quad (4)$$

3.2. Irrigation Release Constraints

The irrigation releases should be less than or equal to the irrigation demand on all reservoirs for all the months and should be greater than or equal to the minimum irrigation demand (ID_{min}). Mathematically this constraint is given as:

$$ID_{min}(i, t) \leq IR(i, t) \leq ID_{max}(i, t) \quad \forall \quad i = 1, 2, 3, 4 \quad (5)$$

$$\forall \quad t = 1, 2, 3, \dots, 12$$

3.3. Reservoir Storage Constraints

The storage in the reservoirs should be less than or equal to the capacity of reservoir and greater than or equal to the dead storage for all months. Mathematically this constraint is given as:

$$S_{min}(i) \leq S(i, t) \leq S_{max}(i) \quad \forall \quad i = 1, 2, 3, 4 \quad (6)$$

$$\forall \quad t = 1, 2, 3, \dots, 12$$

3.4. Hydrologic Continuity Constraints

These constraints relate to the turbine releases, irrigation releases, release for drinking and industrial water supply which is taken as a constant, reservoir storage, inflows into the reservoirs, Losses from the reservoirs for all months. The hydrologic continuity constraints for all the reservoirs is stated as:

1) Reservoir (R₁)

$$(1 + a_t(1, t))S(1, t + 1) = (1 - a_t(1, t))S(1, t) + IN(1, t) - HPR(1, t) - IR(1, t) - SPILL(1, t) - WSR(1, t) - FCR(1, t) + \alpha_1 HPR(1, t) - A_0 e_t(1, t) \quad (7)$$

$$\forall \quad t = 1, 2, 3, \dots, 12$$

2) Reservoir (R₂)

$$(1 + a_t(2, t))S(2, t + 1) = (1 - a_t(2, t))S(2, t) + IN(2, t) + \alpha_2 FCR(1, t) - HPR(2, t) - IR(2, t) - SPILL(2, t) - WSR(2, t) - A_0 e_t(2, t) \quad (8)$$

$$\forall \quad t = 1, 2, 3, \dots, 12$$

3) Reservoir (R₃)

$$(1 + a_t(3, t))S(3, t + 1) = (1 - a_t(3, t))S(3, t) + IN(3, t) - HPR(3, t) - SPILL(3, t) - WSR(3, t) - A_0 e_t(3, t) \quad (9)$$

$$\forall \quad t = 1, 2, 3, \dots, 12$$

4) Reservoir (R₄)
 $(1 + a_t(4, t))S(4, t+1) = (1 - a_t(4, t))S(4, t) + IN(4, t) + \alpha_3 SPILL(3, t)$
 $+ \alpha_4 HPR(3, t) - IR(4, t) - WSR(4, t) - SPILL(4, t) - A_0 e_t(4, t)$
 $\forall t = 1, 2, 3, \dots, 12$ (10)

5) Reservoir (R₅)
 $DSR(t) = C_1 * SPILL(1, t) + C_2 * SPILL(2, t) + C_3 * SPILL(4, t)$
 $+ DSIN(t) + \alpha_5 HPR(2, t)$ (11)

$\forall t = 1, 2, 3, \dots, 12$
 $S(i, 1) = S(i, 13)$ (12)

The transition loss for pumping turbine releases back into the reservoir for R₁, feeder canal release (FCR) from R₁ to R₂, Spills from R₃ to R₄, turbine releases (HPR) from R₃ to reach to R₄, turbine releases from R₂ to reach R₅, Spills from R₁ to reach to R₅, Spills from R₂ to reach to R₅, Spills from R₄ to reach to R₅ is taken as 10 % in the model. Water supply releases is taken as constant for reservoir R₁ as 31.63 Mm³, 3.55 Mm³ for R₂, and 2 Mm³ for R₃ and R₄ for all months.

4. Results and Discussions

For developing optimal operating policies for a multireservoir in a river sub basin a monthly MOGAFUOPT model is developed. By using MOGAFUOPT, the irrigation releases, hydropower production and level of satisfaction (λ) is maximized. For this the GA operators used are stochastic remainder selection, one point crossover and binary mutation. For selection of population size, crossover probability, mutation probability and optimal generations, a thorough sensitivity analysis is carried out. The system performance is estimated by taking crossover probability between 0.7 to 1.0 with a increment of 0.05 and mutation probabilities between 0.3 to 0.001 with a decrement of 0.1 up to 0.01 and then the decrement is taken as 0.001. The population size is varied from 20 to 150 and generation from 20 to 500. Based on the system performance the optimal population size and optimal number of generations are 130 and 500 respectively. When one of the objectives: Z₁ (irrigation releases) is maximized, giving no preference to second objective: Z₂ (hydropower production), the comparison shows that for

crossover probability 0.7 and mutation probability 0.1, the maximization (i.e., maximum value of Z₁: Z₁⁺) is achieved. The variation of maximized irrigation releases with respect to different mutation probabilities for selected crossover probability is shown in Figure 2. When Z₂ is maximized, giving no preference to Z₁, the comparison shows that for crossover probability 0.9 and mutation probability 0.1, the maximization (i.e., maximum value of Z₂: Z₂⁺) is achieved. The variation of maximized hydropower production with respect to different mutation probabilities for selected crossover probability is shown in Figure 3. In fuzzy optimization model, when λ (level of satisfaction) is maximized, the comparison shows that for crossover probability 1.0 and mutation probability 0.004, the maximization (i.e., maximization of both the objectives simultaneously) is achieved. The variation of maximized λ (level of satisfaction) with respect to different mutation probabilities for selected crossover probability is shown in Figure 4.

The MOGAFUOPT model is developed for multireservoir system as shown in Figure 1 with the objectives 1) to maximize irrigation releases and 2) to maximize hydropower production. The best and worst values for both the objectives i.e., Z₁ for irrigation releases (Z₁⁺ and Z₁⁻) and Z₂ for hydropower production (Z₂⁺ and Z₂⁻) are determined by considering one objective at a time, ignoring the other. When Z₁ is maximized, the corresponding value of Z₂ is considered to be the worst and vice versa. These values are given in Table 3. These objectives are fuzzified by considering linear membership function. The membership functions for irrigation releases and hydropower production are presented in Equations 13 and 14 respectively.

$$\mu_{Z_1}(x) = \begin{cases} 0 & Z_1 \leq 1807.97 \\ \frac{(Z_1 - 1807.97)}{(2218.36 - 1807.97)} & 1807.97 \leq Z_1 \leq 2218.36 \\ 1 & Z_1 \geq 2218.36 \end{cases} \quad (13)$$

$$\mu_{Z_2}(x) = \begin{cases} 0 & Z_2 \leq 85591654.2 \\ \frac{(Z_2 - 85591654.2)}{(117394536.3 - 85591654.2)} & 85591654.2 \leq Z_2 \leq 117394536.3 \\ 1 & Z_2 \geq 117394536.3 \end{cases} \quad (14)$$

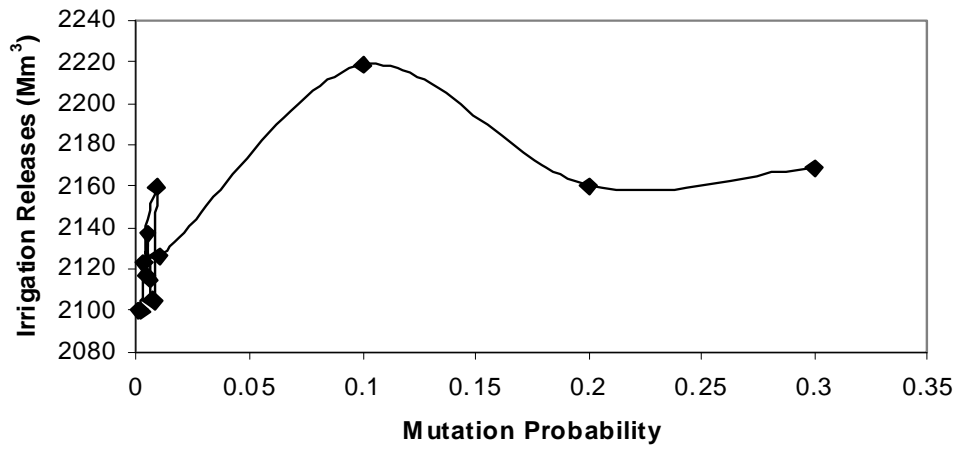


Figure 2. Variation of irrigation releases corresponding to mutation probability for crossover probability 0.7.

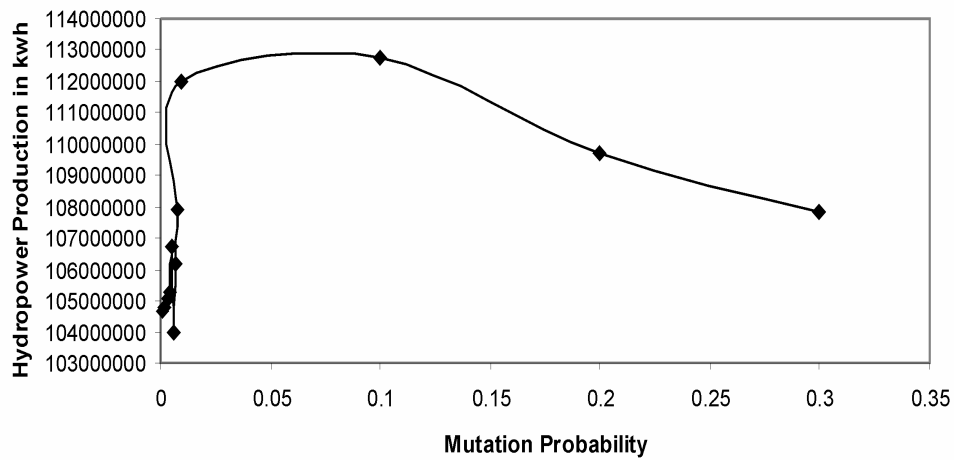


Figure 3. Variation of hydropower production corresponding to mutation probability for crossover probability 0.9.

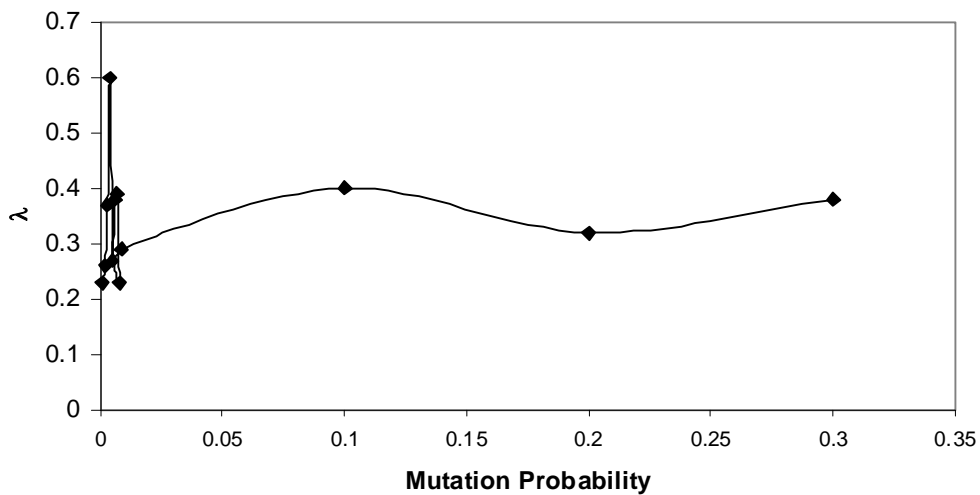


Figure 4. Variation of λ corresponding to mutation probability for crossover probability 1.0.

Table 3. Best and worst values for objective functions.

Objective Function (Maximization)	Best value Z^+	Worst value Z^-
Irrigation releases (Z_1) Mm^3	2218.36	1807.97
Hydro-power production (Z_2) mwh	117394.5	85591.7

These fuzzified objectives are simultaneously maximized by defining level of satisfaction (λ) and then maximizing it. The λ (Maximum level of satisfaction) was found to be 0.60. The irrigation releases (Z_1^*) and hydropower produced (Z_2^*) corresponding to maximum level of satisfaction are 2054.22 Mm^3 and 104755.5 mwh respectively. Monthly optimized irrigation releases from reservoirs are shown graphically in Figure 5. Monthly optimized hydropower production from reservoirs is presented in Figure 6.

Decision maker may adopt λ value as it is or he may demand different λ value. For this, λ can be changed for both the objectives as per preferences of decision maker

and run the model again to obtain respective solution. For this purpose, the whole range of operation policies with satisfaction levels ranging from 0 to 1, for both the objectives, are determined. These policies are presented in Table 4.

The comparison between existing operation policy and optimized operation policy is prepared for Jaykwadi stage-I reservoir (R_1). The results of MOGAFUOPT shows that the annual maximized irrigation releases for Jaykwadi stage-I reservoir (R_1) is 1166.20 Mm^3 . The annual maximum irrigation demand for this reservoir is 1393.2 Mm^3 as per data presented in Table 2. The historical outflow data of reservoir R_1 for 30 years is analyzed and monthly average outflow for irrigation releases is worked out. Average of 30 years outflow data is taken and it works out to be 1295.6 Mm^3 . The comparison of average existing operation policy and optimized operation policy derived by GA under fuzzy environment is promising. The historic data of existing operation policy for other reservoirs is not obtained. Hence comparison is presented for Jaykwadi stage-I reservoir (R_1) in Figure 7.

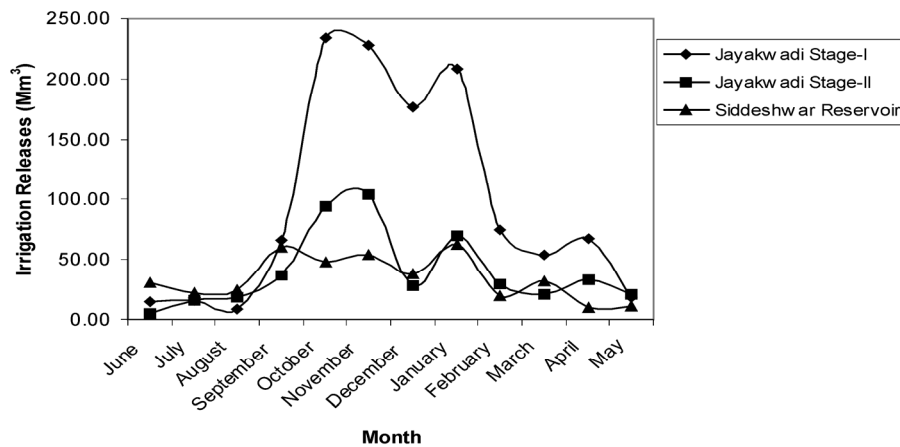


Figure 5. Monthly optimized irrigation releases from reservoirs.

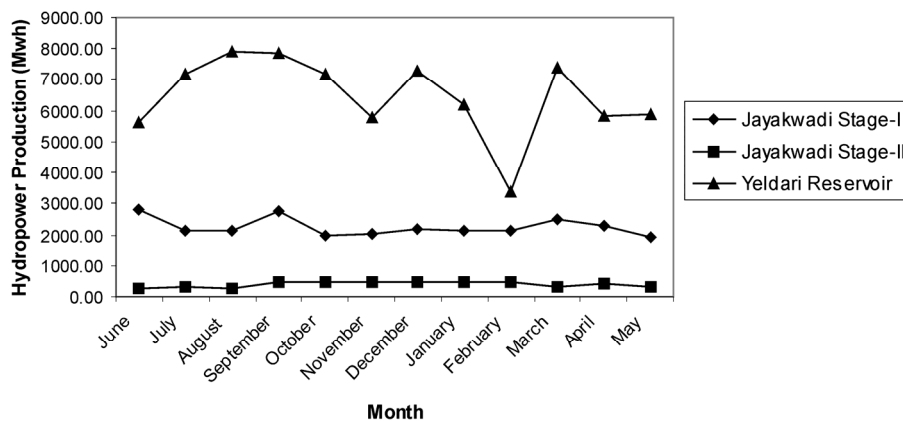


Figure 6. Monthly optimized hydropower production (mwh).

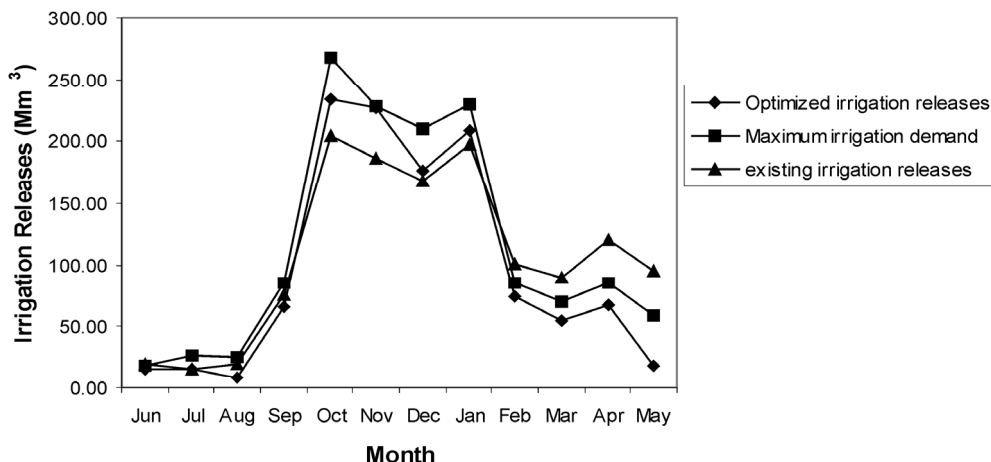


Figure 7. Comparison of irrigation releases for Jayakwadi stage-I project.

Table 4. Solutions of MOGAFUOPT for Different Values of λ .

Sr. No.	Degree of Satisfaction (λ)		Objective Value	
	λ_1	λ_2	Z_1 (Mm ³)	Z_2 (mwh)
1	0	1.00	1807.99	117394.5
2	0.1	0.81	1849.03	111304.5
3	0.2	0.77	1890.07	110187.9
4	0.3	0.70	1931.11	107869.6
5	0.4	0.68	1972.15	107285.8
6	0.5	0.66	2012.18	106526.5
7	0.6	0.60	2054.22	104755.5
8	0.7	0.50	2095.26	101575.2
9	0.8	0.40	2136.30	98394.9
10	0.9	0.30	2177.34	95214.6
11	1.0	0.20	2218.38	92034.3

5. Summary and Conclusion

Multiobjective, multireservoir optimization in fuzzy environment by using GA is explored in this study. A multireservoir system in Godavari river sub basin in Maharashtra State, India is considered. A MOGAFUOPT model is developed and applied to the case study. The objective function of the GA model was set to maximize irrigation releases, hydropower production and level of satisfaction (λ). The sensitivity analysis for deciding crossover probability, mutation probability, population size and number of generations are presented in the result for this case study. By adopting these GA parameters, irrigation releases, hydropower production and level of satisfaction are maximized and results are presented. The maximum level of satisfaction (λ^*) achieved by maximizing both the objectives simultaneously is 0.60. The corresponding irrigation releases and hydropower production are 2054.22 Mm³ and 104755.5 mwh respectively. The whole range of operation policies with satisfaction levels ranging from 0 to 1 for both the objectives are determined. Monthly optimized irrigation releases and hydropower produc-

tion from reservoirs are presented. The comparison of average existing operation policy and optimized operation policy derived by GA under fuzzy environment is promising. The application of proposed MOGAFUOPT model can be extended to the other river basins with little modifications taking physical features and the constraints of the basin into consideration. This study shows that MOGAFUOPT model has significant potential in application to multiobjective, multireservoir system in a river basin.

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Appendix: notation

The following symbols are used in this paper

DSR (t)	=Downstream requirement during month t;
DSIN (t)	= Downstream inflow during month t;
FCR(i,t)	= Feeder Canal Releases during month t from reservoirs i;
FPR(i)	= Flow for firm power release from reservoirs i;
ID _{max} (i,t)	=Maximum irrigation demand during month t from reservoirs i;
ID _{min} (i,t)	=Minimum irrigation requirement during month t from reservoirs i;
IN(i,t)	=Monthly inflow into the reservoir during month t from reservoirs i;
SPILL(i,t)	=Spills during month t from reservoirs i;
HP(i,t)	=Hydropower produced during month t from reservoir i;
IR(i,t)	=Irrigation releases during month t from reservoirs i;
HPR(i,t)	=Releases for hydropower production in month t from reservoirs i;
WSR(i,t)	=Water supply releases during month t from reservoirs i;
S(i,t)	=Storage in the reservoir during month t from reservoirs i;
S _{min} (i)	=Minimum storage capacity for i th reservoir;
S _{max} (i)	=Maximum storage capacity for i th reservoir;
T ₁ , T ₂ , T ₃	=Turbines for reservoirs R ₁ , R ₂ and R ₃ ;
TCR(i)	=Flow for maximum capacity of turbine from reservoirs i;
μ _i (x)	=Membership function;
λ	=Level of satisfaction;
λ*	=Maximum degree of overall satisfaction;
λ ₁	=Level of satisfaction for irrigation releases;
λ ₂	=Level of satisfaction for hydropower produced;
α ₁ , α ₂ , α ₃ , α ₄ , α ₅	=Constants; and
C ₁ , C ₂ , C ₃	=Constants.