

## Investigation of the Dilution/Crystallization Dynamics of RDX and HMX by Microcalorimetry

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**Abstract** Three thermokinetic equations describing the crystal growth process and two relationships between the parameters and the constants of the kinetic equations are derived. The total heat produced and the rate of heat production during the dilution/crystallization of RDX and HMX from dimethyl sulfoxide, cyclohexanone and nitric acid are measured using a Calvet microcalorimeter and a model RD-1 conduction calorimeter. The thermokinetic data of crystal growth processes of RDX and HMX are treated based on the derived equations and relationships. The results show that the exothermic dilution/crystallization processes of RDX and HMX accord with the Burton-Cabrera-Frank dislocation theory.

**Key words:** single compound explosive; crystallization dynamics; RDX; HMX; dislocation theory

## 用微量热法研究 RDX 和 HMX 的稀释/结晶动力学

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**摘 要:** 导出了描述结晶生长过程的 3 个热动力学方程和这些动力学方程的参数与常数间的 2 个关系式。用 Calvet 微热量计测定了 RDX 和 HMX 从二甲基亚砷、环己酮和硝酸中的稀释/结晶总放热量和产热速率。用导出的方程和关系式处理了 RDX 和 HMX 的放热稀释/结晶生长过程的动力学数据。结果表明, RDX 和 HMX 的放热稀释/结晶过程服从 Burton-Cabrera-Frank 位错理论。

**关键词:** 单质炸药; 结晶动力学; RDX; HMX; 位错理论

**中图分类号:** TJ 55; TQ 564

**文献标识码:** A

**文章编号:** 1007-7812(2005)01-0070-06

### Introduction

RDX and HMX are two widely used nitramine explosives and energetic ingredients of propellants. In two previous notes<sup>[1,2]</sup>, the crystallization kinetics of RDX and HMX from DM SO and cyclohexanone, and that of HMX from HNO<sub>3</sub> were reported. The aim of this work is to explore the adaptability of the thermokinetic equations to the crystal growth processes of RDX and HMX and obtaining the information about the interdependence between the parameters and the constants of differ-

ent kinetic equations

### 1 Derivation of the kinetic equations of the crystal growth process

In order to analyze the kinetics of the crystal growth process of RDX and HMX, the following general form of the crystal growth process is used

$$\begin{array}{l} A(\text{aq}) \longrightarrow A(\text{s}) + \text{heat} \\ t = 0, \quad C_0 \quad 0, 0 \quad 0 \\ t = t, \quad C \quad m, \alpha \quad H \\ t = \quad, \quad C \quad m, \alpha = 1 \quad H \end{array} \quad (1)$$

**Received Date:** 2004-03-01

**Foundation:** The science and technology foundation of Shaanxi Key Laboratory of Physico-Inorganic Chemistry (No. 29-3, 2001) and the science and technology foundation of the National Defense Key Laboratory of Propellant and Explosive Combustion of China (No. 514550101).

**Biography:** Hu Rong-zu (1938-), male, professor, research yields: thermochemistry and thermal analysis

where, assuming that in forming the crystal A (s) from A (aq),  $C$  is the solute concentration in the solution at time  $t$  (g/100 g solvent).  $C_0$  is equilibrium saturation concentration (g/100 g solvent).  $m$  and  $\alpha$  are the mass and fraction of solid deposited during a certain time, respectively.  $H$  is the heat produced during a certain time  $t$ , and when  $t=0$ ,  $C=C_0$ ,  $m=0$ ,  $\alpha=0$  and  $H=0$ , when  $t=\infty$ ,  $C=C_0$ ,  $m=m_\infty$ ,  $\alpha=\alpha_\infty=1$  and  $H=H_\infty$ .

The relationship between the energy change (i.e. the heat produced) of a reacting system and the extent (i.e. mass or fraction or concentration) of the reaction (1) may be expressed as

$$\frac{C_0 - C}{C_0 - C_0} = \frac{0 - m}{0 - m_\infty} = \frac{0 - \alpha}{0 - \alpha_\infty} = \frac{0 - H}{0 - H_\infty} \quad (2)$$

From eq (2), we obtain

$$\alpha = \frac{H}{H_\infty} \quad (3)$$

$$\frac{d\alpha}{dt} = \frac{1}{H_\infty} \frac{dH}{dt} \quad (4)$$

$$\frac{dm}{dt} = \left[ \frac{m_\infty}{H_\infty} \right] \frac{dH}{dt} \quad (5)$$

$$\text{and} \quad \frac{C_0 - C}{C_0 - C_0} = \left[ 1 - \frac{H}{H_\infty} \right] \quad (6)$$

Inserting eqs (3) and (4) into the differential kinetic equation (7) of the reaction of the  $n$ th order

$$\frac{d\alpha}{dt} = k(1 - \alpha)^n \quad (7)$$

The themokinetic equations (8) and (9) are obtained:

$$\frac{dH}{dt} = H_\infty k \left[ 1 - \frac{H}{H_\infty} \right]^n \quad (8)$$

and

$$\ln \left[ \frac{1}{H_\infty} \left[ \frac{dH}{dt} \right] \right] = \ln k + n \ln \left[ 1 - \left( \frac{H}{H_\infty} \right) \right] \quad (9)$$

$i = 1, 2, \dots, L$

where  $H_\infty$  is the total heat produced (corresponding to the global area under the themokinetic curve);  $H_t$  is the heat produced in a certain time (corresponding to the partial area under the curve);  $dH_t/dt$  is the rate of heat production at time  $t$ ;  $k$  and  $n$  are the rate constant and reaction order of the crystal growth, respectively.

When  $\ln \left[ \frac{1}{H_\infty} \left[ \frac{dH}{dt} \right] \right]$  is plotted versus  $\ln$

$\left[ 1 - \left( \frac{H}{H_\infty} \right) \right]$  by the least-squares method, this gives the value of  $n$  from the slope and  $k$  from the intercept

Equation (8) is known as the general form describing the crystal growth process

According to the Burton-Cabrera-Frank (BCF) dislocation theory<sup>[3]</sup>, for relatively high supersaturation, the rate of crystal growth at time  $t$ ,  $dm/dt$  may be expressed as

$$\frac{dm}{dt} = km(C - C_0) \quad (10)$$

The combination of eqs (5), (6) and (10) gives

$$\frac{dH}{dt} = kH(C_0 - C) \left[ 1 - \frac{H}{H_\infty} \right] = k_1 \left[ 1 - \frac{H}{H_\infty} \right] \quad (11)$$

$$\text{where} \quad k_1 = kH(C_0 - C) \quad (12)$$

If  $C_0 > C$ , we have

$$\frac{dH}{dt} = kH C_0 \left[ 1 - \frac{H}{H_\infty} \right] = k_2 \left[ 1 - \frac{H}{H_\infty} \right] \quad (13)$$

$$\text{where} \quad k_2 = kH C_0 \quad (14)$$

when  $\left( \frac{dH}{dt} \right)_i$  is plotted versus  $1 - \left( \frac{H}{H_\infty} \right)_i$  by the least-squares method, this gives the values of  $k_2$  and  $a$  in the equation (15)

$$\frac{dH}{dt} = k_2 \left[ 1 - \frac{H}{H_\infty} \right] + a \quad (15)$$

If equation (10) is written as

$$\frac{dm}{dt} = km(C - C_0) + b \quad (16)$$

The equation (17) is obtained by combining eqs (5), (6) and (16)

$$\begin{aligned} \frac{dH}{dt} &= \frac{dm}{dt} \left( \frac{H_\infty}{m} \right) = \frac{H_\infty}{m} [km(C - C_0) + b] \\ &= \frac{H_\infty}{m} [km(C_0 - C) \left( 1 - \frac{H}{H_\infty} \right) + b] \\ &= H_\infty k(C_0 - C) \left( 1 - \frac{H}{H_\infty} \right) + \frac{bH_\infty}{m} \\ &= H_\infty k C_0 \left( 1 - \frac{H}{H_\infty} \right) + \frac{bH_\infty}{m} (C_0 > C) \end{aligned} \quad (17)$$

Comparing eq (15) with eq (17), two relationships [eqs (18) and (19)] are obtained

$$k = k_2/H_\infty C_0 \quad (18)$$

and

$$b = \alpha n / H \quad (19)$$

Equations (18) and (19) relate  $k$  to  $k_2$  and  $b$  to  $a$ , respectively.

If the values of the constants  $a$  and  $b$  are small in comparison with those of  $k_2$  and  $k$ , the kinetics of the crystal growth processes can be expressed by eqs (10) and (13).

Equations (10) and (13) are known as the themokinetic equations of the crystal growth process. Equation (13) is only an especial example ( $n = 1$ ) of equation (8).

## 2 Experimental

### 2.1 Materials

RDX and HMX used as solutes were prepared by our institute. The RDX contained no detectable HMX, and HMX contained no detectable RDX. Their purities were more than 99.9%. DM SO (m. p. 16.5~19;  $r_4^{20} = 1.098 \sim 1.106$ ) and cyclohexanone (b. p. 154.0~156.0;  $r_D^{20} = 1.4500 \sim 1.4510$ ) used as solvents are of chemical and analytical purity respectively. The concentration of HNO<sub>3</sub> used as solvent was 95.68%. A 50:10% DM SO-H<sub>2</sub>O mixture and  $n\text{-C}_7\text{H}_{16}/\text{CCl}_4$  (1:1, V/V) are used as diluents, where H<sub>2</sub>O is twice distilled water;  $n\text{-C}_7\text{H}_{16}$  (b. p. 96.5~98.5;  $r_4^{20} = 0.683 \sim 0.686$ ) and CCl<sub>4</sub> (b. p. 75.5~77.5;  $r_4^{20} = 1.591 \sim 1.597$ ) are of chemical purity.

### 2.2 Experimental equipment and conditions

All measurements at 30 °C are made using a Calvet microcalorimeter, type BT 215 from SETARAM, France, which has a sensitivity of 66.5 μV · mW<sup>-1</sup> and is equipped with two 15 ml vessels. All measurements at 34 °C are made using a conduction calorimeter, type RD-1 from Sichuan University, with a precision of ±0.5% and equipped with two 60 ml vessels. The microcalorimeter is calibrated by the Joule effect and the calibration is repeated after each experiment.

The precision of enthalpy measurement is 2%. The device used for the study of the crystallization kinetics is shown in Fig. 1. (1. thin glass bulb containing diluent; 2. polytetrafluoroethylene tube; 3. glass tube containing RDX or HMX solution; 4. silicon rubber cover; 5. calorimetric cell; 6. glass rod. On depressing the rod, the bottom of the glass bulb is broken, and the solution and diluent mix together in the tube).

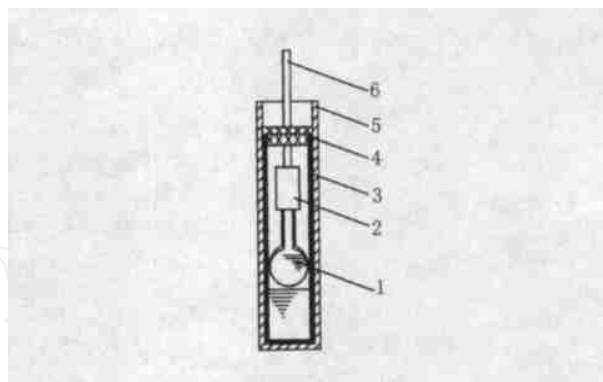


Fig. 1 Device used for measuring the crystallization kinetics

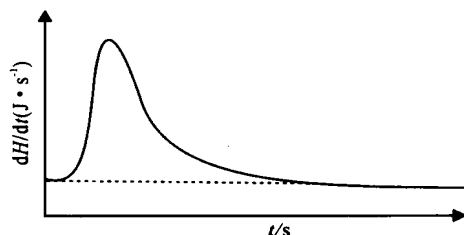


Fig. 2 Typical themogram obtained during dilution/crystallization

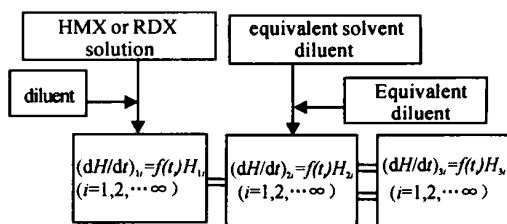


Fig. 3 Block diagram of the process of studying dilution/crystallization kinetics

A typical schematic themogram obtained during the dilution and crystallization is shown in Fig. 2, and is obtained by the testing and computing method presented as a block diagram in Fig. 3.

In Fig. 3,  $(dH/dt)_i$  is the rate of total heat

production at time  $t$ , including the rate of the heat of mixing produced between solvent and diluent,  $(dH/dt)_{2i}$ , and the rate of the heat of crystallization of the crystal,  $(dH/dt)_{3i}$  at time  $t$ ; and  $H_{1i}$  is the total heat produced during a certain time, including the heat of mixing produced between solvent and diluent,  $H_{2i}$ , and the heat of crystallization by the crystal during a certain time.

The thermograms obtained under the same conditions overlapped with each other, indicating that the reproducibility of tests was satisfactory.

### 3 Results and discussion

To verify the reliability of eqs (8), (15) and (16) and obtain information about the kinetic parameters and the constants of RDX and HM X, the original thermokinetic data tabulated in Table 1 are fitted to the eqs (8), (15) and (16) by the linear least-squares method. Results obtained, including the total heat produced, the reaction order ( $n$ ), the rate constants ( $k_2$  and  $k$ ) during the crystallization of RDX and HM X from DM SO and cyclohexanone at 30 °C and that of HM X from HNO<sub>3</sub> at 34 °C, and the constants ( $a$  and  $b$ ) in eqs (15) and

(16), are shown in Table 2.

From Tables 1 and 2, the following observations can be made:

(1) The crystal growth processes of RDX and HM X are exothermic. The exothermic process may be expressed by the isothermal differential kinetic equation (8).

(2) BCF model [eq (13)] is only an especial example ( $n=1$ ) of the general form [eq (8)] of the crystal growth process.

(3) Because  $k_2 \gg d$  in [eq (15)] and  $k \gg b$  in [eq (16)], describing the kinetics of the crystal growth processes of RDX and HM X by the eqs (15) and (16) are tenable. This indicates that the crystal growth processes of RDX and HM X from DM SO and cyclohexanone and that of HM X from HNO<sub>3</sub> without seeds of HM X accords with the BCF dislocation theory.

(4) In our experimental conditions, the crystal growth process of HM X from HNO<sub>3</sub> with seeds of HM X is out of accord with the BCF dislocation theory.

Table 1 Thermokinetic data of the crystal growth processes of RDX and HM X

Experimental conditions No. 1					Experimental conditions No. 2				
Tempe 30	Solute RDX (0.0084g)	Solvent DM SO (0.0250g)	Seed 50 1%	Diluent DM SO-H <sub>2</sub> O (0.6896g)	Tempe 30	Solute RDX (0.0084g)	Solvent DM SO (0.0250g)	Seed RDX 50 1%	Diluent DM SO-H <sub>2</sub> O (0.6896g)
$t/s$		$(dH/dt)_i/10^4 (J \cdot s^{-1})$		$(H_i)_i/10^2 J$	$t/s$		$(dH/dt)_i/10^4 (J \cdot s^{-1})$		$(H_i)_i/10^2 J$
210		6.991		2.761	210		10.00		15.69
240		6.255		5.146	240		8.841		18.58
270		6.092		7.155	270		8.251		21.13
300		5.573		9.372	300		7.372		23.47
330		5.196		11.00	330		6.640		25.61
360		4.749		12.84	360		6.050		27.61
390		4.297		14.69	390		5.460		29.54
420		4.134		16.15	420		5.012		30.96
450		3.686		17.61	450		4.711		32.76
480		3.655		19.08	480		4.263		34.18
510		3.502		20.17	510		4.100		35.19
540		3.197		21.25	540		3.937		36.40
570		3.033		22.38	570		3.494		37.61
600		2.870		23.47	600		3.188		38.66

Table 1 Thermokinetic data of the crystal growth processes of RDX and HMX

Experimental conditions No. 1					Experimental conditions No. 2				
Tempe	Solute	Solvent	Seed	Diluent	Tempe	Solute	Solvent	Seed	Diluent
30	RDX (0.0084g)	DM SO (0.0250g)	50	1% DM SO-H <sub>2</sub> O (0.6896g)	30	RDX (0.0084g)	DM SO (0.0250g)	RDX 50 (0.4000g)	1% DM SO-H <sub>2</sub> O (0.6896g)
	<i>t</i> /s	$(dH/dt)_i/10^4 (J \cdot s^{-1})$		$(H_i)_i/10^2 J$		<i>t</i> /s	$(dH/dt)_i/10^4 (J \cdot s^{-1})$		$(H_i)_i/10^2 J$
	630	2.506		24.31		630	3.025		39.66
	660	2.544		25.48		660	2.720		40.67
	690	2.523		26.40		690	2.845		41.51
	720	2.218		27.15		720	2.540		42.17
	750	2.054		28.07		750	2.234		42.97
	780	1.891		28.79		780	2.075		43.81
	810	1.728		29.33		810	2.054		44.21
	840	1.565		30.25		840	1.895		44.65
		0		42.72			0		44.73

Experimental conditions No. 3					Experimental conditions No. 4				
Tempe	Solute	Solvent	Seed	Diluent	Tempe	Solute	Solvent	Seed	Diluent
30	HMX (0.0022g)	cyclohexanon (0.1000g)	HMX (0.4771g)	n-C <sub>7</sub> H <sub>16</sub> /CCl <sub>4</sub> (1:1) (0.9555g)	34	HMX (0.3684g)	HNO <sub>3</sub> (2.8685g)		H <sub>2</sub> O (0.7910g)
	<i>t</i> /s			$(dH/dt)_i/10^5 (J \cdot s^{-1})$		<i>t</i> /min	$(dH/dt)_i/(J \cdot \text{min}^{-1})$		$(H_i)_i/J$
	210		118.2	22.18		1.25	19.54		6.109
	240		98.24	26.57		1.50	19.63		10.79
	270		88.20	30.59		2.00	19.87		19.25
	300		80.75	34.06		2.25	21.34		25.44
	330		68.16	36.78		2.50	15.77		29.62
	360		58.12	39.16		2.75	13.81		33.30
	390		46.69	41.34		3.00	13.43		37.28
	420		40.96	43.18		5.50	6.987		62.59
	450		35.19	44.60		6.50	5.565		68.53
	480		26.61	44.73		7.50	4.770		74.27
	510		22.30	46.78		8.50	3.138		78.58
	540		17.99	47.66		10.5	2.887		83.89
	570		12.26	48.37		12.5	2.092		87.70
	600		7.949	48.91		13.5	1.674		89.62
	630		3.598	49.21		14.5	1.297		90.88
			0	49.33			0		93.64

Experimental conditions No. 5					Experimental conditions No. 5				
Tempe	Solute	Solvent	Seed	Diluent	Tempe	Solute	Solvent	Seed	Diluent
34	HMX (0.3684g)	HNO <sub>3</sub> (2.8685g)	HMX (0.2089g)	H <sub>2</sub> O (0.7910g)	34	HMX (0.3684g)	HNO <sub>3</sub> (2.8685g)	HMX (0.2089g)	H <sub>2</sub> O (0.7910g)
	<i>t</i> /min			$(dH/dt)_i/(J \cdot \text{min}^{-1})$		<i>t</i> /min			$(H_i)_i/J$
	1.00		42.63	30.54		5.50		5.397	77.65
	1.25		24.02	38.45		7.50		3.556	83.81
	1.50		14.39	43.39		9.50		2.176	88.70
	1.75		13.22	46.40		12.5		1.297	94.14
	2.00		9.623	49.54				0	102.4
	2.75		8.326	56.44					

Table 2 Total heat produced and crystal growth kinetics of RDX and HMX

T / (J · g <sup>-1</sup> )	H / (J · g <sup>-1</sup> )	$\frac{dH}{dt} = H k \left[ 1 - \frac{H}{H_0} \right]^n$			$\frac{dH}{dt} = k_2 \left[ 1 - \frac{H}{H_0} \right] + a$			$\frac{dH}{dt} = km (C - C_0) + b$	
		$k \times 10^3 / s^{-1}$	n	r	$k_2 \times 10^4 / (J \cdot s^{-1})$	$a \times 10^5 / (J \cdot s^{-1})$	r	$k \times 10^3 / s^{-1}$	$b \times 10^6 / (g \cdot s^{-1})$
30	50.86	1.74	1.22	0.997	8.09	-8.01	0.997	1.60	-1.57
30	53.25	1.68	0.307	0.984	12.0	16.8	0.996	4.47	3.15
30	224.2	3.23	0.640	0.996	20.3	11.0	0.991	19.7	0.049
34	256.7	3.68	0.844	0.986	38.10	400	0.981	0.408	15.6
34	268.1	5.75	1.38	0.958	77.10	-10500	0.822	0.775	-392

(5) With the addition of seed crystals of RDX and HMX, the value of *k* in eq (16) is larger than that of *k* without seeds. This shows that the total number of nuclei in the seeded solution is greater than that in unseeded solution.

References

[1] CHEN Xi-jun, LI Zhi-bin, HU Rong-zu. Investigation of the crystallization kinetics of cyclo-trimethylenetrinitramine and cyclo-tetramethylenetrinitramine by microcalorimetry [J]. Thermochim. Acta, 1990, 173: 193-198

[2] CHEN Xi-jun, LI Zhi-bin, HU Rong-zu. Investigation of the crystallization kinetics of cyclo-tetramethylenetrinitramine from nitric acid by microcalorimetry [J]. Thermochim. Acta, 1995, 260: 243-245

[3] BURTON W K, CABRERA N, FRANK F C. The growth of crystals and equilibrium structure of their surfaces [J]. Trans Roy. Soc (London), 1951, A 243: 299-358

## 2005 年火炸药新技术学术研讨会征文通知 (补充通知)

为促进火炸药技术创新与可持续发展, 为实现我军武器装备的信息化作出贡献, 经总装备部火炸药技术专业组、火炸药燃烧国防科技重点实验室、中国兵工学会火炸药专业委员会协商, 决定共同主办“2005 年火炸药新技术学术研讨会”, 并委托中国兵器工业第二〇四研究所负责承办。会议将邀请著名专家、学者做专题报告, 并就近期国内外火炸药行业发展中的新技术、新成果、应用研究等内容进行交流。欢迎各位专家、学者、工程技术人员、高校师生积极参加。

1. 学术讨论会主题: 火炸药技术创新与可持续发展

2. 征文内容: (1) 高能量密度化合物的合成与应用; (2) 新型含能材料合成与应用; (3) 新型功能材料合成与应用; (4) 新型火炸药技术; (5) 火炸药数值模拟仿真技术; (6) 火炸药装药新技术; (7) 火炸药先进制造技术; (8) 火炸药理化分析与测试新技术; (9) 火炸药安全性与可靠性新技术; (10) 火炸药燃烧与爆炸新技术; (11) 火炸药应用基础创新研究; (12) 新概念火炸药及其应用。

3. 征文要求: (1) 会议前拟出版会议论文集, 凡内容符合征文要求的论文均可投稿, 所撰写论文应观点明确, 论据可靠, 文字流畅, 插图清楚, 每篇字数不超过 5000 字 (含论文摘要、关键词、参考文献); (2) 论文编写遵循我国正式出版物上科技论文的标准规范要求, 用 Word2000 排版; (3) 页面打印格式: A4 纸激光打印, 版心 15 × 21cm (具体要求见附页); (4) 保密审查由撰写论文单位把关; (5) 论文需要递交激光打印稿及电子稿, 请通过加密网或机要方式寄送至 204 研究所; (6) 论文征文截止日期: 2005 年 3 月 31 日。

4. 会议暂定地点、时间: 湖南长沙 2005 年 5~ 6 月

5. 稿件寄送地址: 西安市 18 号信箱科技委

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