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## Phase and orientational ordering of A–B–A tri-block co-polymers guest in a quenched host of low molecular weight rod molecules

Lorin Gutman<sup>a</sup>, Jianshu Cao<sup>a,\*</sup>, Timothy M. Swager<sup>b</sup>, Edwin L. Thomas<sup>c</sup>

<sup>a</sup> Department of Chemistry, Massachusetts Institute of Technology, 77 Massachusetts Avenue, Cambridge, MA 022139, USA <sup>b</sup> Department of Chemistry and Department of Materials Science and Engineering, Massachusetts Institute of Technology,

Cambridge, MA 022139, USA

<sup>c</sup> Department of Materials Science and Engineering, Massachusetts Institute of Technology, Cambridge, MA 022139, USA

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## Abstract

We investigate the effects of thermodynamical variables, intermolecular interactions and block lengths on phase and orientational ordering of guest tri-block co-polymers in a host glassy matrix of short molecular rods. The A and B blocks can align to the short rod molecules. Using a field theoretic formulation we demonstrate the occurrence of a nematic–nematic (N/N) first order transition from a guest stabilized to a guest–host stabilized region, a reentrant transition from a guest stabilized nematic region to a host only stabilized regime via an isotropic phase and the possibility to selectively stabilize the orientation of the A or/ and B blocks.

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Co-polymers and short molecular rod molecules are instrumental in the supra-molecular construction of guest-host systems. Manipulation of the guest-host interaction alignment and co-polymer composition opens new avenues for the design of technologically valuable properties [1-3]. While di-block co-polymers have been studied in the context of possible selfassembly patterns and their interactions with nanoparticles [4-6] tri-block co-polymers received less attention. When made of stiff non-adjacent blocks and a middle flexible block and incorporated in a semi-flexible polypropylene (PP) [7], tri-block copolymers can increase significantly the host toughness and mechanical stability. The effects of additives such as salts, alkali acids, polymers and ionic surfactants on the cloud points in hydrophilic/hydrophobic

\* Corresponding author. E-mail address: jianshu@mit.edu (J. Cao). tri-block co-polymers has been studied recently [8]. In bio- medicine tri-block co-polymers made of *PLGA-PEG-PLGA* are instrumental in enhancement of gene transfection efficiency of various cationic polymeric carriers and as additives in non-virial gene transfection [9].

Manipulation of molecular alignment is important in optical materials used in dichroic polarizers and to holographic data storage. Experiments demonstrated [14–16] that manipulation of molecular features of a B trypticene block in an A–B–A tri-block co-polymer immersed in a host of short rods can have dramatic effects on guest alignment and shifting times. Effects of composition on ordering in flexible tri-block co-polymers have been addressed [10], yet, to our knowledge the effects of dissimilarity in block rigidity and the effect of a host of short rods molecules on the orientational ordering of the different tri-block segment types was not studied. Herein we investigate the phase diagram and orientational ordering of a guest

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of A–B–A tri-block co-polymers mixed with short molecular rods. A typical guest–host system is depicted in Fig. 1. The simplest microscopic Hamiltonian for the A–B–A tri-block/short rod mixture that captures these interaction alignment features is

$$\begin{split} H &= \sum_{i=1}^{N} \left( \int_{0}^{L_{A}} + \int_{L_{A}+L_{B}}^{L} \right) \frac{\beta \epsilon_{A}}{2} \dot{\mathbf{u}}^{2}(n_{i}) \, \mathrm{d}n_{i} \\ &+ \int_{L_{A}}^{L_{A}+L_{B}} \frac{\beta \epsilon_{B}}{2} \dot{\mathbf{u}}^{2}(n_{i}) \, \mathrm{d}n_{i} - \frac{w_{\mathrm{r,r}}}{2} \sum_{k,l=1}^{M,M} \delta(\mathbf{r}_{k} - \mathbf{r}_{l}) \\ &\times (1 - (\mathbf{u}_{k} \times \mathbf{u}_{l})^{2}) - w_{\mathrm{r,A}} \sum_{i,k=1}^{N,M} \left( \int_{0}^{L_{A}} + \int_{L_{A}+L_{B}}^{L} \right) \\ &\times \mathrm{d}n_{i} \delta(\mathbf{r}(n_{i}) - \mathbf{r}_{k}) (1 - (\mathbf{u}(n_{i}) \times \mathbf{u}_{k})^{2}) \\ &- w_{\mathrm{r,B}} \sum_{i,k=1}^{N,M} \int_{L_{A}}^{L_{A}+L_{B}} \mathrm{d}n_{i} \delta(\mathbf{r}(n_{i}) - \mathbf{r}_{k}) (1 - (\mathbf{u}(n_{i}) \times \mathbf{u}_{k})^{2}) \\ &- \frac{w_{\mathrm{A,A}}}{2} \sum_{i,j=1}^{N,N} \left( \int_{0}^{L_{A}} + \int_{L_{A}+L_{B}}^{L} \right) \, \mathrm{d}n_{i} \left( \int_{0}^{L_{A}} + \int_{L_{A}+L_{B}}^{L} \right) \\ &\times \mathrm{d}n'_{j} \delta\left( \mathbf{r}(n_{i}) - \mathbf{r}\left(n'_{j}\right) \right) \left( 1 - \left( \mathbf{u}(n_{i}) \times \mathbf{u}\left(n'_{j}\right) \right)^{2} \right) - \frac{w_{\mathrm{A,B}}}{2} \\ &\times \sum_{i,j=1}^{N,N} \left( \int_{0}^{L_{A}} + \int_{L_{A}+L_{B}}^{L} \right) \, \mathrm{d}n_{i} \int_{L_{A}}^{L_{A}+L_{B}} \, \mathrm{d}n'_{j} \delta\left( \mathbf{r}(n_{i}) - \mathbf{r}\left(n'_{j}\right) \right) \\ &\times \left( 1 - \left( \mathbf{u}(n_{i}) \times \mathbf{u}\left(n'_{j}\right) \right)^{2} \right) - \frac{w_{\mathrm{B,B}}}{2} \sum_{i,j=1}^{N,N} \int_{L_{A}}^{L_{A}+L_{B}} \, \mathrm{d}n_{i} \\ &\times \int_{L_{A}}^{L_{A}+L_{B}} \, \mathrm{d}n'_{j} \delta\left( \mathbf{r}(n_{i}) - \mathbf{r}\left(n'_{j}\right) \right) \left( 1 - \left( \mathbf{u}(n_{i}) \times \mathbf{u}(n'_{j}\right) \right)^{2} \right)$$

where i, j are chain indexes, k, l are indexes for the short molecular rods, M is the number of short rods and N is the number of polymer chains.  $\mathbf{r}(n_i)$  is the spatial location of the *n*th segment on the *i*th chain,  $\mathbf{u}(n_i)$  is the tangent vector at  $n_i$  on the backbone of the *i*th polymer chain.  $\mathbf{r}_k$  is the spatial location of the kth rod,  $\mathbf{u}_k$  is the director of the kth rod,  $L_A$ ,  $L_B$  and L are the A block, B block and polymer lengths, respectively. First and second terms in Eq. (1) are interaction potentials among adjacent segments which reside in the A and B semi-flexible blocks and  $\beta \epsilon_A/2$ ,  $\beta \epsilon_B/2$  are the local bending penalties. Third, fourth and fifth terms in Eq. (1) represents the rod-rod, rod-A segment and rod-B segment microscopic alignment, respectively. Last three terms are the A-A, A-B and B-B interactions, respectively. Most generally the short range anisotropic potential among molecular species o, m has the form:  $\frac{w_{o,m}}{2} \sum_{o,m} \delta(\mathbf{r}_o - \mathbf{r}_m) (1 - (\mathbf{u}_o \times \mathbf{u}_m)^2)$ . Positive  $w_{o,m}$  indicate a reduction in the o/m inter-molecular free volume from alignment of the molecular directors.



Fig. 1. Schematic representation of two symmetric tri-block copolymers in a guest-host tri-block/short rod molecular mixture: in (a) the middle block is a polypticene polymer. The connected thin lines of the A blocks are long hydrocarbons while host matrix short rod components are the anthracene molecules. (b) is an implicit representation of (a).

First, we express Eq. (1) with microscopic densities –  $\rho_{\rm m}(\mathbf{r})$  and orientational tensors –  $\sigma_{\rm m}(\mathbf{r})$  given by:

$$\hat{\rho}_{A}(\mathbf{r}) = \sum_{i} \left( \int_{0}^{L_{A}} + \int_{L_{A}+L_{B}}^{L} \right) dn_{i} \delta(\mathbf{r} - \mathbf{r}(n_{i}));$$

$$\hat{\rho}_{B}(\mathbf{r}) = \sum_{i} \int_{L_{A}}^{L_{A}+L_{B}} dn_{i} \delta(\mathbf{r} - \mathbf{r}(n_{i}));$$

$$\rho_{r}(\mathbf{r}) = \sum_{k} \delta(\mathbf{r} - \mathbf{r}_{k});$$

$$\hat{\sigma}_{A}^{st}(\mathbf{r}) = \sum_{i} \left( \int_{0}^{L_{A}} + \int_{L_{A}+L_{B}}^{L} \right) dn_{i} \delta(\mathbf{r} - \mathbf{r}(n_{i})) \mathbf{u}^{s}(n_{i}) \mathbf{u}^{t}(n_{i});$$

$$\hat{\sigma}_{B}^{st}(\mathbf{r}) = \sum_{i} \int_{L_{A}}^{L_{A}+L_{B}} dn_{i} \delta(\mathbf{r} - \mathbf{r}(n_{i})) \mathbf{u}^{s}(n_{i}) \mathbf{u}^{t}(n_{i});$$

$$\hat{\sigma}_{r}^{st}(\mathbf{r}) = \sum_{k} \delta(\mathbf{r} - \mathbf{r}_{r,k}) \mathbf{u}_{k}^{s} \mathbf{u}_{k}^{t}.$$
(2)

The index values of m and o, i.e., r, A and B, stand for LC rods and co-polymer A and B blocks. s, t indexes

represent the x, y, z space components. We impose now delta function constraints on the partition function of the guest-host system and exchange the discrete microscopic orientational tensors with continuous orientational tensors for LC rods and A and B segments. The LC rod endpoints are free and a local constraint is required on rod orientational fluctuations. The partition function for the guest-host system is given by

$$Z[\mathbf{u}(n_i), \mathbf{u}_k] = \left[ \iint \prod_{i=1}^N D\mathbf{r}(n_i) \prod_{\mathbf{m}=\mathbf{A},\mathbf{B},\mathbf{r}} \iint D\sigma_{\mathbf{m}}(\mathbf{r}) \right] \\ \times \left[ \prod_{k=1}^M \int d\mathbf{r}_k \int d\mathbf{u}_k \right] \exp(-H[\sigma_{\mathbf{m}}(\mathbf{r})]) \\ \times \prod_{i,n_i,\mathbf{r}} \delta[\sigma_{\mathbf{A}}(\mathbf{r}) - \hat{\sigma}_{\mathbf{A}}(\mathbf{r})] \delta[\sigma_{\mathbf{B}}(\mathbf{r}) - \hat{\sigma}_{\mathbf{B}}(\mathbf{r})] \\ \times \delta[\mathbf{u}(n_i)^2 - 1] \prod_{k,\mathbf{r}} \delta[\sigma_{\mathbf{r}}(\mathbf{r}) - \hat{\sigma}_{\mathbf{r}}(\mathbf{r})] \delta[\mathbf{u}_k^2 - 1].$$
(3)

 $\hat{\sigma}_{m}(\mathbf{r})$  are given in Eq. (2); the  $\hat{\sigma}_{m}(\mathbf{r})$  delta function constraints are expressed with auxiliary fields  $\psi_{m}(\mathbf{r})$ . A global constraint set on chain director fluctuations of the A and B blocks is sufficient due to chain connectivity (viz. [17] for further details).

$$Z[\mathbf{u}(n_{i}),\mathbf{u}_{k}] = \left[ \iint \prod_{i=1}^{N} D\mathbf{r}(n_{i}) \prod_{m=A,B,r} \iint D\psi_{m}(\mathbf{r}) \\ \times \iint D\sigma_{m}(\mathbf{r}) \right] \left[ \prod_{k=1}^{M} \int d\mathbf{r}_{k} \int d\mathbf{u}_{k} \right] \\ \times \exp(-H[\hat{\sigma}_{m}(\mathbf{r})]) \\ \times \prod_{i,n_{i},\mathbf{r}} \exp\left(i \int d\mathbf{r}\psi_{p}(\mathbf{r}):[\sigma_{p}(\mathbf{r}) - \hat{\sigma}_{p}(\mathbf{r})]\right) \\ \times \int \prod_{p=A,B} d\lambda_{p} \exp(-i\lambda_{p}[\mathbf{u}(n_{i})^{2} - 1]) \\ \times \prod_{k,r} \int d\lambda_{r,k} \exp\left(i \int d\mathbf{r}\psi_{r}(\mathbf{r}):[\sigma_{r}(\mathbf{r}) - \hat{\sigma}_{r}(\mathbf{r})]\right) \\ \times \exp\left[-i\sum_{k} \left(\lambda_{r,k} \left(\mathbf{u}_{k}^{2} - 1\right)\right)\right],$$
(4)

where k is the index of the rods. The orientational tensor matrix for the molecular species -m = r, p, in principal axis representation has the form:

$$\sigma_{\rm m} = \begin{pmatrix} a_{\rm m} - b_{\rm m} & 0 & 0\\ 0 & a_{\rm m} + b_{\rm m} & 0\\ 0 & 0 & 2a_{\rm m} \end{pmatrix}.$$
 (5)

Herein, we address the orientational phase diagram and the relation among uniaxial ordering guest-host described by the average order parameter  $\langle S \rangle_m$  with m = A, B, r:  $\langle S \rangle_{\rm m} = .5 \frac{V}{N_{\rm m}} \sum_{\alpha} \langle 3(\mathbf{v}_{\rm m}^{\alpha} \cdot \mathbf{n}_{\rm m})^2 - 1 \rangle$ .  $\mathbf{v}_{\rm m}^{\alpha}$  is the unit vector which points along the long axis of molecule  $\alpha$  of type m located at  $\mathbf{r}^{\alpha}$ ;  $N_{\rm m}$  is the number of molecules of type m present in the system. For uniaxial ordering, the orientational order parameter,  $\langle S \rangle_{\rm m}$ , is related to the principal axis components of the orientational tensor in the following way  $\langle S \rangle_{\rm m} = -3a_{\rm m}/\rho_{\rm m}$ .  $1 > \langle S \rangle_{\rm m} > 0$  signals uniaxial nematic ordering while  $-0.5 < \langle S \rangle_{\rm m} < 0$  signals discotic ordering. In Einstein notation (alike indexes are summed over),  $\sigma_{\rm m}^{t,t} = \rho_{\rm m}$ . The tri-block entropy is calculated now exactly for finite chains by noting that:

$$S_{\text{tri-block}} = \mathbf{d}\mathbf{u}_0 \int \mathbf{d}\mathbf{u}_{L_A} \int \mathbf{d}\mathbf{u}_{L_B} \int \mathbf{d}\mathbf{u}_L G_1(\mathbf{u}_{L_A} - \mathbf{u}_0; L_A)$$

$$\times G_2(\mathbf{u}_{L_B} - \mathbf{u}_{L_A}; L_B - L_A) G_1(\mathbf{u}_L - \mathbf{u}_{L_B}; L - L_B),$$
(6)

where G is the propagator for an harmonic oscillator in imaginary time adapted to the present polymer problem. We carry out the integrals exactly in Eq. (6) and obtain

$$S_{\text{tri-block}} = \left[ \frac{A_2^{0.5}}{C_1 \sqrt{A_1 (C_1 - C_1^{-1}) + A_2 C_2}} \right] \\ \times \left[ \frac{\sqrt{\pi}}{\sqrt{A_1 (C_1 - C_1^{-1}) + A_2 C_2 + \frac{A_2^2 C_1}{A_1 (1 - C_1^2) - A_2 C_2 C_1}}} \right]$$
(7)

with

$$A_{1} = \frac{2e_{A}(\lambda_{A} + \psi_{A})^{0.5}}{2\sinh\left[L_{A}\left(\frac{2(\lambda_{A} + \psi_{A})}{e_{A}}\right)^{0.5}\right]};$$

$$A_{2} = \frac{2e_{B}(\lambda_{B} + \psi_{B})^{0.5}}{2\sinh\left[L_{B}\left(\frac{2(\lambda_{A} + \psi_{B})}{e_{B}}\right)^{0.5}\right]};$$

$$C_{1} = \cosh\left[L_{A}\left(\frac{2\lambda_{A} + \psi_{A}}{e_{A}}\right)^{0.5}\right];$$

$$C_{2} = \cosh\left[L_{B}\left(\frac{2\lambda_{B} + \psi_{A}}{e_{B}}\right)^{0.5}\right].$$
(8)

The expression above is exact for finite length blocks. Here, we consider long blocks; in fact for blocks of  $\approx 15-20$  segments, the long chain limit is very close to the exact result. With a Legendre transforms we obtain the free energy dependence on  $\langle S \rangle_{\rm r}$ ,  $\langle S \rangle_{\rm A}$  and  $\langle S \rangle_{\rm B}$ . Herein, we investigate the situations where the interaction alignment among the A and B blocks is negligible. The free energy for the guest-host system, we investigate is: / **C**\

 $\langle \mathbf{C} \rangle$ 

$$\begin{split} F(\langle S \rangle_{\rm r}, \lambda_{\rm A}, \lambda_{\rm B}, \langle S \rangle_{\rm A}, \langle S \rangle_{\rm B}) \\ &= \frac{w_{\rm r,r}(1-\rho_{\rm p})^2}{3} \left( \langle S \rangle_{\rm r}^2 + \langle S \rangle_{\rm r} + 1 \right) \\ &- 0.572365(1-\rho_{\rm p}) - (1-\rho_{\rm p}) \\ &\times \log \left[ \frac{\operatorname{Erfi}\left[ \sqrt{w_{\rm r,r}(1-\rho_{\rm p})\langle S \rangle_{\rm r}} \right]}{w_{\rm r,r}(1-\rho_{\rm p})\langle S \rangle_{\rm r}} \right] \\ &\times \left( \frac{\rho_{\rm p}qx}{1+qx} \left( -\lambda_{\rm B} + \left( \left( \frac{\rho_{\rm p}qx}{1+qx} \left( -1 + \langle S \rangle_{\rm B}^2 \right) w_{\rm B,B} \right) / 3 \right) \right) \right) \\ &+ \frac{1}{\sqrt{2}} \left( \frac{1}{e_{\rm B}} \right)^{0.5} \left( \left( \lambda_{\rm B} - \left( 2(1-\rho_{\rm p})(-1+\langle S \rangle_{\rm r}) w_{\rm B,r} \right) + \left( \frac{\rho_{\rm p}qx}{1+qx} (-1+\langle S \rangle_{\rm B}) w_{\rm B,B} \right) \right) / 3 \right)^{0.5} \right) \\ &+ 2 \left( \lambda_{\rm B} + \left( (1-\rho_{\rm p})(2+\langle S \rangle_{\rm r}) w_{\rm B,r} \right) + \left( \frac{\rho_{\rm p}qx}{1+qx} (2+\langle S \rangle_{\rm B}) w_{\rm B,B} \right) / 3 \right)^{0.5} \right) \\ &+ \left( \frac{\rho_{\rm p}}{1+qx} \left( -\lambda_{\rm A} + \left( \left( \frac{\rho_{\rm p}}{1+qx} \left( -1+\langle S \rangle_{\rm A}^2 \right) w_{\rm A,A} \right) \right) / 3 \right) \\ &+ \frac{1}{\sqrt{2}} \left( \frac{1}{e_{\rm A}} \right)^{0.5} \left( \left( \lambda_{\rm A} - \left( 2(1-\rho_{\rm p})(-1+\langle S \rangle_{\rm r}) w_{\rm A,r} \right) + \left( \frac{\rho_{\rm p}}{1+qx} (-1+\langle S \rangle_{\rm A}) w_{\rm A,A} \right) \right) / 3 \right)^{0.5} \right) \right) \right) \\ &+ 2 \left( \lambda_{\rm p,A} + \left( (1-\rho_{\rm p})(2+\langle S \rangle_{\rm r}) w_{\rm A,r} \right) + \left( \frac{\rho_{\rm p}}{1+qx} (2+\langle S \rangle_{\rm A}) w_{\rm A,A} \right) \right) / 3 \right)^{0.5} \right) \right) \right) \right)$$

Erfi in Eq. (9) is the imaginary error function [18]. The first four terms represent the free energy of the short rod quenched host. Other terms are free energy terms of the tri-blocks and also tri-block host interactions.  $\langle S \rangle_{\rm r}, \langle S \rangle_{\rm A}$  and  $\langle S \rangle_{\rm B}$  are rod, A and B block orientational order parameters, respectively. qx is the block length quotient for the A and B blocks. It is given by  $qx = L_B/2L_A$ .

The limit  $1 - \rho_p \rightarrow 0$  of Eq. (9) and  $qx \rightarrow 0$  recovers the free energy of a many-chains LCPs solution obtained in Eq. (32) of reference [17], and the minimal value for uniaxial ordering  $\langle S \rangle_p^c = 0.25$ . The  $\rho_p \to 0$  limit of Eq. (9) recovers the Mayer-Saupe [11-13] result for the magnitude of the orientational ordering at of the N–I transition of short rods, i.e.,  $\langle S \rangle_r^c = 0.42$ . Our result  $w_{\rm r,r}^{\rm c} = 6.78$  is consistent with the infinitely stiff limit of long worm like chains [19] of  $w \cong 7$ . The host is below the glass transition thus the free energy of the guest-host system is minimized analytically with respect to the fields  $\langle S \rangle_r$ , first, in the absence of the tri-block-LC rod interaction. The  $\langle S \rangle_{\rm r}$  obtained is used in the total free energy –  $F(\langle S \rangle_{\rm r}, \lambda_{\rm A}, \langle S \rangle_{\rm A}, \lambda_{\rm B}, \langle S \rangle_{\rm B})$ . Now, the free energy is optimized with respect to  $\lambda_A$ ,  $\langle S \rangle_A$ ,  $\lambda_B$ ,  $\langle S \rangle_B$  in the pres-



Fig. 2. Effect of the block length quotient qx on the middle block segment ordering;  $\beta e_A = 0$ ,  $\beta e_B = 7$ ,  $w_{r,r} = 0$ ,  $w_{B,B} = 7$ ,  $w_{A,A} = 0$ ,  $\rho_{\rm p} = 0.9.$ 

ence of orientational ordering of the LC rods. The unit length chosen in all calculations, the monomer hard sphere diameter, renders chain microscopic interactions and characteristics, L,  $\beta \epsilon$ , w, v,  $\rho$  dimensionless. In Fig 2, we present results for the effect of the block length quotient qx on orientational ordering of the B segment in a mixture of A–B–A tri-blocks; the A block is flexible and the B block is stiff. Fig. 2 demonstrates the existence of a lower bound for the critical block length quotient value,  $qx^{c} = 0.316$ . Below that value of qx (for the given parameters used in Fig. 2), orientational ordering of segments which reside in the stiff block B is precluded. For qx larger than  $qx^{c}$ ,  $\langle S \rangle_{B}$  increases fast but levels off slowly. In fact,  $\langle S \rangle_{\rm B}$  reaches the homo-polymer orientational ordering  $\langle S \rangle$  value at very large qx. That is a direct manifestation of the nature of liquid crystallinity in polymers; the segments are connected at the endpoints with other segments and the connectivity has a significant contribution to overall polymer alignment of the blocks.

Fig. 3 displays the variation of orientational ordering with rigidity of the A and the B block, qx, and tri-block density. In the figure, the matrix of short rods orders around  $\rho_r = 0.54$ . For longer B blocks a transition from a guest stabilized nematic ordering to a guest + host stabilized nematic ordering occurs as a spike nematic transition. It is marked by a discontinuity in the orientational order parameter of the B segments. In Fig. 3, the transition depicted at three block length quotient values qx = 8, 2, 1 occurs at the density threshold  $\rho_{\rm p} \simeq 0.455$ . At larger fractions of A segments, i.e., qx = 0.5, a different physical picture emerges. Below  $\rho_{\rm p} \simeq 0.6$  the presence of a short B block cannot sustain the guest stabilized orientational ordering and a



Fig. 3. Effects of block length quotient, the A and B block rigidity, and the matrix ordering on orientational ordering of the B segments;  $\beta e_A = 0$ ,  $\beta e_B = 7$ ,  $w_{r,r} = 12.5$ ,  $w_{A,A} = 0$ ,  $w_{B,B} = 7$ ,  $w_{B,r} = 3$ .

transition to an isotropic phase occurs. At lower polymer densities i.e.,  $\rho_p = 0.54$ , the glassy host orders via a typical Mayer-Saupe nematic transition. The host ordering stabilizes a non-zero average orientation of the B segments. This host stabilized nematic ordering of the B segments at low qx values occurs via a step transition from the isotropic phase. In this case the average nematic B segment director orients parallel to the host director. Thus, the reentrant transition occurs from a guest stabilized nematic phase with the average director pointed in some arbitrary direction, via an isotropic phase, to a host stabilized nematic phase with the average molecular director of the B segments aligned with the host director of the short rods. Fig. 3 suggests that the density width of the isotropic phase is controlled by the matrix ordering threshold and the tri-block copolymer quotient qx.

In Fig. 4, we present the phase diagram for A–B–A triblocks that reside in a LC rod glass for qx = 1 at dissim-



Fig. 4. Orientational phase diagram of the A and B segments – triblock density effects;  $\beta e_A = 6$ ,  $\beta e_B = 10$ , qx = 1,  $w_{r,r} = 12.5$ .

ilar bending rigidities of A and B segments, i.e.,  $e_A \neq e_B$ . At interaction alignment values  $w_{r,r}$  above the dashed line, the LC rod molecules are ordered. The A and B segments align their average director parallel to the host and an A + B nematic phase occurs. Below the thin solid line, the tri-block co-polymer resides in the isotropic phase; above the thin line a guest stabilized isotropic/nematic transition with  $\langle S \rangle_B \neq 0$  occurs. In that regime of interaction alignment  $w_{A,A}$ , the bending rigidity of the A segment  $-e_A$  is low, and  $\langle S \rangle_A = 0$ . Above the thick solid line, the A segments order and a transition to an A + B guest stabilized nematic phase takes place.

Fig. 5 illustrates the orientational phase dependence on  $qx^c$ . At low values of alignment interaction parameters,  $\langle S \rangle_A = 0$ ,  $\langle S \rangle_B = 0$ ;  $\langle S \rangle_A \neq 0$ ;  $\langle S \rangle_B = 0$ , for long A blocks and relatively low values of  $w_{A,A}$ . Note, the critical  $w_{B,B}^c$  required for orientational ordering of the B segments is lower in  $qx^c \to \infty$  limit then the value of  $w_{A,A}^c$ value in the limit of  $qx^c \to 0$  for the case where the A block is less rigid then the B block. Ultimately, above  $w_{r,r} \approx 11.35$  the host stabilizes the A + B segment orientational ordering.

In this work we demonstrated the occurrence of a nematic-nematic (N/N) first order transition from a guest stabilized to a guest-host stabilized region and the possibility of a reentrant transition from a guest stabilized nematic region to a host only stabilized regime via an isotropic phase. Selective NMR deuteration can be used to measure  $\langle S \rangle_{\rm r}$  and  $\langle S \rangle_{\rm A}$  and  $\langle S \rangle_{\rm B}$  separately. The Hamiltonian parameters  $w_{r,r}$ ,  $w_{p,p}$  and  $w_{r,p}$  dependence on temperature and density can be obtained from a best fit of the theoretical  $\langle S \rangle_{\rm r}$  and  $\langle S \rangle_{\rm B}$  to their derived values from NMR measurements.  $e_A$  and  $e_B$  can be obtained from a separate small angle light scattering data of the individual long blocks. The presents analysis suggests new ways to systematically manipulate and selectively stabilize the orientational ordering of the A or/ and B blocks via a judicious choice of A and B block



Fig. 5. Orientational phase diagram of the A and B block segments – quotient block length effects;  $e_A = 6$ ,  $e_B = 10$ ,  $\rho_p = 0.4$ .

length quotient qx, A and B segment rigidities and intersegment and guest-host interactions and to design guest-host materials with novel liquid crystalline properties.

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